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10MAT21

Second Semester B.E. Degree Examination, Dec.2014/Jan.2015

Engineering Mathematics -

Time: 3 hrs.

Max. Marks:100

- Note:** 1. Answer any FIVE full questions, choosing at least two from each part.
 2. Answer all objective type questions only on OMR sheet page 5 of the answer booklet.
 3. Answer to objective type questions on sheets other than OMR will not be valued.

PART — A

1 a. Choose the correct answers for the following : (04 Marks)

- i) A differential equation of the first order but of higher degree, solvable for x, has the solution as:
 A) $F(y, p, c) = 0$ B) $F(x, p, c)$ C) $F(x, y, c) = 0$ D) $C_1, C_2 = 0$
- ii) If $xy + C = C^2x$ is the general solution of a differential equation then its singular solution is
 A) $y = x$ B) $y = -x$ C) $4x^2y + 1 = 0$ D) $4x^2y - 1 = 0$
- iii) The general solution of Clairant's equation is,
 A) $y = Cf(x) + f(C)$ B) $y = Cx + f(C)$ C) $x = Cf(y) + f(C)$ D) $x = Cy + g(C)$
- iv) The general solution of $p^2 - 7p + 12 = 0$ is,
 A) $(y - 3x - c)(y - 4x - c) = 0$ B) $(y - c)(x - c) = 0$ C) $(3x - c)(4x - c) = 0$ D) $(y + 3x + c)(y - 4x - c) = 0$

 b. Solve : $xp^2 - (2x + 3y)p + 6y = 0$. (05 Marks)

 c. Solve : $y = 3x + \log p$ (05 Marks)

 d. Obtain the general solution and the singular solution of the equation $xp^3 + yp^2 + 1 = 0$ as Clairant's equation. (06 Marks)

2 a. Choose the correct answers for the following : (04 Marks)

- i) The particular integral of $(D^2 + a^2)y = \sin ax$ is,
 A) $\frac{-x \cos ax}{2a}$ B) $\frac{x \cos ax}{2a}$ C) $\frac{x \sin ax}{2a}$ D) $\frac{-x \sin ax}{2a}$
- ii) The solution of the differential equation $(D^4 - 5D^2 + 4)y = 0$ is,
 A) $y = C_1 e^x + C_2 e^{-x} + C_3 e^{2x} + C_4 e^{-2x}$
 B) $y = (C_1 + C_2 x + C_3 x^2 + C_4 x^3) e^{2x}$
 C) $y = C_1 \cos x + C_2 \sin x + C_3 \cos 2x + C_4 \sin 2x$
 D) None of these
- iii) The particular integral of $(D - 1)^2 y = 3ex$ is,
 A) $-\frac{xex}{2}$ B) $\frac{3}{2} x^2 e^x$ C) $\frac{3}{2} x^2 ex$ D) $\frac{2}{3} x^2 ex$
- iv) The roots of auxiliary equation of $D' (D^2 + 2D)^2 y = 0$ are:
 A) 0,0,0,0,2,2 B) 0,0,0,0,-2,-2 C) 0,0,2,2,-2,-2 D) 2,2,2,2,0,0

- b. Solve : $(D^2 - 2D + 1)y = xex + x$ (05 Marks)
- c. Solve : $\frac{dx}{dy} - 4D + 4)y = e^2x + \cos 2x + 4$. (05 Marks)
- d. Solve : $\frac{dx}{dt} - 7x + y = 0, \frac{dy}{dt} - 2x - 5y = 0$. (06 Marks)

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3 a. Choose the correct answers for the following :

(04 Marks)

- i) The complementary function of $x^2 y'' - 3xy' + 4y = x$ is:
 A) $(C_1 + C_2 \log x)x^2$ B) $(C_1 + C_2 x)e^{2x}$
 C) $C_1 + C_2 x$ D) $\frac{1}{x} + \frac{C_2}{x^4}$
- ii) By the method of variation parameters, the value of 'W' is called,
 A) Euler's function B) Wronskian of the function
 C) Demorgan's function D) Cauchy's function
- iii) The equation $(2x+1)^2 y'' - 6(2x+1)y' + 16y = 8(2x+1)^2$ by putting $g = 2x+1$ with $D = \frac{dz}{dx}$ reduces to
 A) $(D^2 + 4D + 4)y = 3e^{2z}$ B) $(D^2 - 4D + 4)y = 2e^{2z}$
 C) $(D^2 - 4D + 4)y = 0$ D) None of these
- iv) To find the series solution for the equation $2x^2 y'' - xy' + (1-x^2)y = 0$, we assume the solution as,

$$A) y = \sum_{n=0}^{\infty} a_n x^n \quad S) y = \sum_{n=0}^{\infty} a_n x^{n+1} \quad T) y = \sum_{n=0}^{\infty} a_n x^{n+1/2} \quad U) y = \sum_{n=0}^{\infty} a_n x^{n+1/2}$$

- b. Solve : $(D^2 + a^2)y = \sec ax$ by method of variation of parameters. (05 Marks)
- c. Solve $(3x+2)^2 y'' + 3(3x+2)y' - 36y = 8x^2 + 4x + 1$ (05 Marks)
- d. Solve : $y'' + xy' + y = 0$ in series solution. (06 Marks)

a. Choose the correct answers for the following :

(04 Marks)

- i) $2z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$, d'arbitrary constants is a solution of:
 A) $2z = p^2 x + qy$ B) $2z = px + q^2 y$ C) $2z = px + qy$ D) None of these
- ii) The auxiliary equations of Lagrange's linear equation $Pp + Qq = R$ are:
 A) $\frac{dx}{P} = \frac{dy}{Q} = \frac{dz}{R}$ B) $\frac{dx}{p} = \frac{dy}{q} = \frac{dz}{R}$ C) $\frac{dx}{x} = \frac{dy}{y} = \frac{dz}{z}$ D) $\frac{dx}{x} + \frac{dy}{y} + \frac{dz}{z} = 0$
- iii) General solution of the equation $\frac{a^2 z}{ax^2} = x + y$ is,
 A) $\frac{x^3}{6} + \frac{x}{2} + f(y) + g(y)$ B) $\frac{x^3}{6} - \frac{x}{2} + f(y) + yg(y)$
 C) $\frac{x^3}{6} + \frac{x^2 y}{2} + xf(y) + g(y)$ D) $\frac{x^3}{6} + \frac{x^2 y}{2} + xf(y) + yg(y)$
- iv) Suitable set of multipliers to solve $x^2(y-z)p + y^2(z-x)q = z^2(x-y)$ is,
 A) (0, 1, 1) B) (x, y, z) C) (0, 1, 1) D) $\frac{1}{x}, \frac{1}{y}, \frac{1}{z}$

- b. Form a partial differential equation by eliminating arbitrary function from the relation,
 $(1)(xy+z^2, x+y+z)=0$ (05 Marks)
- c. Solve : $(y^2 + z^2)p + x(yq - z) = 0$ (05 Marks)
- d. Solve by the method of separation of variables $\frac{82z}{x^2} - 2\frac{az}{ax} + \frac{az}{ay} = 0$ (06 Marks)

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PART—B

a. Choose the correct answers for the following :

(04 Marks)

i) $\int_0^2 \int_0^x f(x-y) dy dx =$

A) 3

B) 4

C) 5

D) 6

ii) $\int_0^1 \int_0^1 \int_0^1 f(x) y^2 z dz dy dx =$

A) 36

B) 16

C) 26

D) 46

iii) The integral $\int_0^2 x^2 dx$ is,

A) $\Gamma(-\frac{1}{2})$

B) $\Gamma(-\frac{1}{2})$

C) $\Gamma(\frac{1}{2})$

D) $\Gamma(-\frac{3}{2})$

iv) The value of $p(5, 3) + p(3, 5)$ is:

A) $\frac{2}{35}$

B) $\frac{3}{4}$

C) $\frac{3}{35}$

D) $\frac{4}{35}$

 b. Evaluate $\int_0^1 \int_0^{1-x} xy(x+y) dy dx$ taken over the area between $y = 1-x$ and $y = x$. (M5 marks)

c. Evaluate $\int_0^1 \int_0^{1-x} \int_0^{1-x-y} 1(x+y+z) dz dy dx$

(05 Marks)

d. Show that $\int_0^{\pi} \sin \theta d\theta = 2$

(06 Marks)

6 a. Choose the correct answers for the following :

(04 Marks)

i) Gauss Divergence theorem is a relation between:

A) a line integral and a surface integral

B) a surface integral and a volume integral

C) a line integral and a volume integral

D) two volume integrals

 ii) $\oint_C M dx + N dy$ is also equal to,

A) $\int_0^c (aM - aN) dx dy$

B) $\int_0^c (aM + aN) dx dy$

C) $\int_0^c (aM - aN) dx dy$

D) $\int_0^c (aM + aN) dx dy$

 iii) Using the following integral, work done by a force F can be calculated:

A) Surface integral B) Volume integral C) Both (A) and (B) D) Line integral

 iv) If $F = x^2 i + xy j$ then the value of $\oint_C F \cdot dr$ from $(0, 0)$ to $(1, 1)$ along the line $y = x$ is,

A) $2/3$

B) $3/2$

C) $1/3$

D) $1/2$

 b. Find the area between the parabola, $y^2 = 4x$ and $x^2 = 4y$ with the help of Green's theorem in a plane. (05 Marks)

 c. Evaluate $\oint_C xy dx + xy^2 dy$ by Stoke's theorem where C is the square in the $x-y$ plane with vertices $(1, 0)$, $(-1, 0)$, $(0, 1)$ and $(0, -1)$ (05 Marks)

 d. Evaluate $\oint_C F \cdot dr$ given $F = xi + yj + zk$ over the sphere $x^2 + y^2 + z^2 = a^2$ by using Gauss divergence theorem. (06 Marks)

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(04 Marks)

a. Choose the correct answers for the following :

 i) If $L\{f(t)\} = F(s)$ then $L\{t f(t)\}$ is,

- A) $\int_0^\infty F(s) ds$ B) $\int_0^\infty F(s) ds$ C) $\int_0^\infty F(s) ds$ D) $\int_0^\infty F(s) ds$

 ii) If $L\left\{\frac{\cos at - \cos bt}{t}\right\} = \frac{1}{2} \log \frac{(s^2 + b^2)}{(s^2 + a^2)}$ then $L\left\{\frac{\sin 2t}{t}\right\} =$

- A) $\frac{1}{4} \log \frac{(s^2 + 4)}{(s^2 + 1)}$ B) $\frac{1}{2} \log \frac{(s^2 + 1)}{(s^2 + 4)}$ C) $\frac{1}{4} \log \frac{(s^2 + 4)}{(s^2 + 1)}$ D) $\frac{1}{2} \log \frac{(s^2 + 1)}{(s^2 + 4)}$

 iii) $L\{e^{3t} H(t-4)\} =$

- A) $\frac{e^{12-4s}}{s+3}$ B) $\frac{e^{12-4s}}{s-3}$ C) $\frac{e^{12-4s}}{s+3}$ D) $\frac{e^{12-4s}}{s-3}$

 iv) $L\{4^t 6(t-a)\} =$

- A) $(-a) e^{-as}$ B) $a e^{-as}$ C) $a e^{-as}$ D) e^{-as}

 b. Find the Laplace transform of $t^5 e^{4t} \cosh 3t$.

(05 Marks)

 c. Find $\int_0^\infty t e^{-t} \sin 3t dt$

(05 Marks)

 d. Given $f(t) = \begin{cases} E, & 0 < t < a \\ -E, & a < t < 2a \end{cases}$ where $g(t+a) = g(t)$, show that $L\{f(t)\} = \frac{E}{s} \tanh \frac{as}{4}$. (06 Marks)

8 a. Choose the correct answer for the following :

(04 Marks)

 i) $L\left\{\frac{1}{t}\right\} =$

- A) e^{-t} B) e^{-t} C) e^{-t} D) e^{-t}

 ii) $L\left\{\frac{1}{(s-4)^2}\right\} =$

- A) $t e^{4t}$ B) $t e^{4t}$ C) $t e^{4t}$ D) $t e^{4t}$

 iii) $L^{-1}\left\{\frac{s}{s^2+5}\right\} =$

- A) $\sin \sqrt{5} t$ B) $\frac{1}{\sqrt{5}} \cos \sqrt{5} t$ C) $\frac{1}{5} \cos 5t$ D) $\cos \sqrt{5} t$

 iv) $L^{-1}\left\{\frac{1}{s^2 + a^2}\right\} =$

- A) $t \sin at$ B) $t \cos at / 2a$ C) $t \sin at / 2a$ D) $t \cos at$

 b. Find $L^{-1}\left\{\frac{s^2+4}{s(s+4)(s-4)}\right\}$. (05 Marks)

 c. Find $L^{-1}\left\{\frac{1}{(s-1)(s^2+0)}\right\}$ by using convolution theorem. (05 Marks)

 d. Solve by using Laplace transform $y''(t) + y(t) = 0$; $y(0) = 2$, $y(\pi/2) = 1$ (06 Marks)