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### OR

- 4 a. Let  $a_n = \begin{vmatrix} 1, & a \end{vmatrix} = 2$ ,  $a_2 = 3$  and  $a_n = an_i + an_2 + a_3$  for n 3. Prove that  $a_n 5 3$ " for all (05 Marks)
  - b. If L0, LI, L2, ..... are Lucas numbers, then prove that  $L = \begin{vmatrix} c & 1 + Jj^n & -1/5 \\ 0 & 2 \end{vmatrix}^n$

(05 Marks)

c. In how many ways can one distribute eight identical bulls into four distinct containers so that (i) no container is left empty? (ii) the fourth container contains an odd number cf (06 Marks)

### Module-3

- 5 a. Let f, g, h be functions from R to R defined by  $f(x) = x^2$ , g(x) = x + 5,  $h(x) = Vx^2 + 2$ , verify that(hog)of=ho(gofi. (05 Marks)
  - b. Let f : R ----> R be defined by
    - f(x)  $\begin{vmatrix} 3x 5 & \text{for } x > 0 \\ -3x + 1 & \text{for } x5 0 \end{vmatrix}$  then find
  - (i) f(-1) | (ii) f(5/3) (iii) f<sup>-1</sup>(3) (iv) f<sup>-1</sup>(-6) (iv) f<sup>-1</sup>([-5, 5]). (05 Marks)
    c. Define partially ordered set. Draw the Hasse diagram representing the positive divisors of 36. (06 Marks)

OR

6 a. Determine the following relations are functions or not. If relation is function, find its range (i) {(x, y)/x, yez, y = 3x+1 }; (ii) {(x, y)/x, yez, y =  $x^2+3$  } (iii)1(x, y)/x, yeR,  $y^2 = x$ ; (iv) {(x, y)/x, yEQ,  $x^2+y^2=1$  } (05 Marks)

- b. State the Pigeonhole principle and generalization of the pigeonhole principle. Prove that if 30 dictionaries in a library contains a total of 61,327 pages, then at least one of the dictionaries must have at least 2045 pages. (05 Marks)
- c. Let  $A = \{1, 2, 3, 4, 6\}$  and R be a relation on A defined by aRb if and only if a is a multiple of b. Represent the relation R as matrix and draw its digraph. (06 Marks)

#### $\underline{Module_{-}4}$

- 7 a. Determine the number of positive integers n, such that 1 5\_ n 5 300, and n is
  - (i) not divisible by 5, 6, 8
  - (ii) divisible by at least one of 5, 6, 8
  - b. Four persons P1,1<sup>3</sup>, P3, P4 who arrive late for a dinner party, find that only one chair at each of five tables T1, T2, T3, T4, T5 is vacant. P1 will not sit T1 or T2, P2 will not sit at T2, P3 will not sit at T3 or T4 and P4 will not sit at T4 or Ts. Find the number of way they can occupy the vacant chairs. (05 Marks)
  - c. Solve the recurrence relation: =  $3a_1$ , + 5 x 7<sup>-1</sup> for n ?\_ 0, give that  $a_n = 2$ .

(06 Marks)

(05 Marks)

### OR

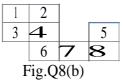
8 a. Find the number of permutations of the digits 1 through 9 in which the blocks 36. 78, 672 do not appear.
 (06 Marks)



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b. Find the rook polynomial for the board in the Fig.Q8(b). Using expansion formula and product formula. (06 Marks)



c. If are = 0, al = 1, a2 = 4 and a3 = 37, satisfy the recurrence relation an+' + ca, = 0 for n 0, determine the constants h and a and then solve the relation for an

determine the constants b and c and then solve the relation for an .

(04 Marks)

# Module\_5

- 9 a. Define complete graph and complete bipartite graph. Hence draw
  - (i) Kuratowaski's first graph  $K_5$ ,
  - (ii) Kuratowaski's second graph кзз
  - (iii) 3-regular graph with 8 vertices.
  - b. Discuss the solution of Kongsberg bridge problem. (05 Marks)
  - c. Obtain an optimal prefix code for the message LETTER RECEIVED. Indicate the code.

(06 Marks)

(05 Marks)

## OR

- 10 a. State Handshaking property, how many vertices will a graphs have, if they contain
  - (i) 16 edges and all vertices of degree 4?
  - (ii) 21 edges, 3 vertices of degree 4 and other vertices of degree 3?
  - (iii) 12 edges, 6 vertices of degree 3 and other vertices of degree less than 3. (05 Marks)
  - b. Define isomorphism of two graphs. Show that following pair of graphs are isomorphic. [Refer Fig.Q10(b)].

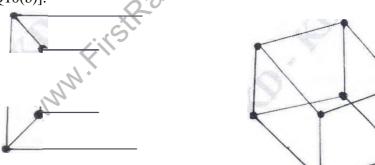


Fig.Q10(b)

(05 Marks) (06 Marks)

c. Define tree and prove that tree with n vertices has n - 1 edges.