

CBCS SCHEME

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15CS54

Fifth Semester B.E. Degree Examination, Dec.2019/Jan.2020 Automata Theory and Computability

Time: 3 hrs.

Max. Marks: 80

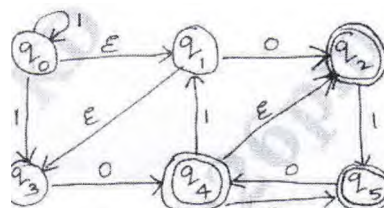
Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

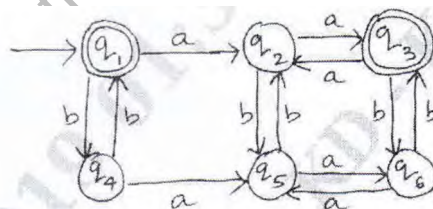
- 1 a. Briefly describe the applications of Theory of computation. (04 Marks)
- b. Define DFSM. Build DFSM for the following languages.
 - i) $L = \{a, b\}^* : \text{every } a \text{ in } w \text{ is immediately followed by } b\}$
 - ii) $L = \{a, b\}^* : w \text{ does not contain substring } aab\}$. (08 Marks)
- c. Describe Machine based hierarchy of language classes. (04 Marks)

OR

- 2 a. For the following NDFSM, use ndfsmtdfsm to construct an equivalent DFSM. Begin by showing the value of ϵ for each state q : (08 Marks)

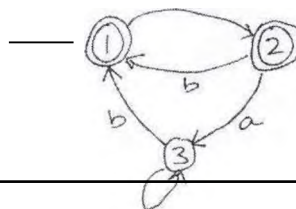


- b. Let M be the following DFSM. Use minDFSM to minimize M . (08 Marks)

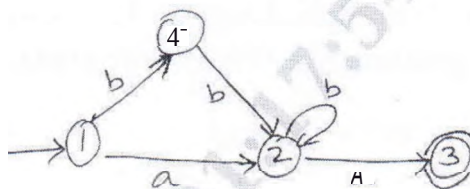


Module-2

- 3 a. Define Regular Expression. Write regular expression for the following :
 - i) $L = \{w \in \{a, b\}^* : w \text{ does not end in } ha\}$
 - ii) $L = \{0^n 9^m : n \geq 1, m \geq 0\}$ w corresponds to the decimal encoding, without leading 0's, of an odd natural number} . (06 Marks)
- b. Consider the FSM M . Use the fsmtoereg heuristic algorithm to construct a regular expression that describes $L(M)$. (05 Marks)



- c. Consider the FSM M. Use fsmtoregex algorithm to construct a regular expression that describes $L(M)$. (05 Marks)



OR

- 4 a. Show that regular languages are closed under complement and set difference. (06 Marks)
b. State and prove pumping lemma theorem for regular languages. And show that the language $L = \{anbn : n > 0\}$ is not regular. (10 Marks)

Module 3

- 5 a. Define CFG. Design CFG for the languages.
i) $L = \{a^i 1^j 1^{2i} : j = 3i + 1\}$ ii) $L = \{K r^n 1^n : n \geq 1\}$. (08 Marks)
b. Define Chomsky Normal form. Convert the following CFG to CNF.

$$S \rightarrow aACa$$

$$A \rightarrow aIB$$

$$B \rightarrow C1c$$

$$C \rightarrow cIE$$
(08 Marks)

OR

- 6 a. Define Ambiguity. Consider the grammar $E \rightarrow EE \mid E * E \mid E - E \mid E x y$. Find the leftmost, rightmost derivations and parse trees for the string " $+ * - xyxy$ ". (07 Marks)
b. Define PDA. Design a PDA to accept the following language.
 $L = \{ww^R : w \in \{a, b\}^*\}$. Draw the transition diagram for the constructed PDA. (09 Marks)

Module 4

- 7 a. Design a TM to accept the language $L = \{a^n b^n : n > 1\}$. Obtain the transition table and transition diagram. Also show the instantaneous description for the string "aabb". (11 Marks)
b. Explain the working principle of TM with diagram. (05 Marks)

OR

- 8 a. State and prove pumping theorem for CFL's shown that the language $L = \{b^n c^n : n > 0\}$ is not context free. (10 Marks)
b. Explain the hierarchy within the class of CFL's (hierarchy of languages). (03 Marks)
c. Show that CFL's are closed under reverse. (03 Marks)

Module 5

- 9 a. Explain Multitape TM, with diagram. (05 Marks)
b. Prove that every language accepted by a multitape TM is acceptable by some standard TM. (06 Marks)
c. Explain the model of Linear Bounded Automata. (05 Marks)

OR

- 10 Write short notes on :
a. Undecidable languages.
b. Halting problem of TM.
c. Post correspondence problem.
d. Church — Turing Thesis. (16 Marks)