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17MATDIP31

Third Semester B.E. Degree Examination, Dec.2019/Jan.2020
Additional Mathematics - I

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Find the modulus and amplitude of

$$3+i$$

$$2+i$$

(07 Marks)

If $x = \cos^\circ + i \sin^\circ$, then show that $\frac{x}{x_r} = i \tan n^\circ$.

(07 Marks)

- c. Simplify $\frac{(\cos 30 + i \sin 30)^4 (\cos 40 + i \sin 40)^5}{(\cos 40 + i \sin 40)^3 (\cos 50 + i \sin 50)^4}$

(06 Marks)

OR

- 2 a. Find the sine of the angle between $A = 2i + 2j - k$ and $B = 6i - 3j + 2k$.

(07 Marks)

- b. Find the value of X , so that the vectors $a = 2i - 3j + k$, $b = i + 2j - 3k$ and $c = i + j$ are coplanar.

(07 Marks)

- c. Prove that $a \times (b \times c) + b \times (c \times a) + c \times (a \times b) = 0$.

(06 Marks)

Module-2

- 3 a. Find the n^{th} derivative of $e^x \cos(bx + c)$.

(07 Marks)

- b. If $y = a \cos(\log x) + b \sin(\log x)$ prove that $x^2 y'' + (2n+1)xy' + (n^2 + 1)y = 0$.

(07 Marks)

- c. If $u = \sin^{-1} \frac{x-y}{x+y}$, prove that $x \frac{du}{dx} + y \frac{du}{dy} = \tan u$.

(06 Marks)

OR

- 4 a. Find the pedal equation of $r = \cos n\theta$.

(07 Marks)

- b. Expand $\log_e(I+x)$ in ascending powers of x as far as the term containing x^4 .

(07 Marks)

- c. If $x = r \cos \theta$, $y = r \sin \theta$, find $\frac{\partial(x,y)}{\partial(r,\theta)}$

(06 Marks)

Module-3

- 5 a. Evaluate $\int_1^y (1 + xy^2) dx dy$

(07 Marks)

- b. Evaluate $\int_{-\pi}^{\pi} \sin^4 x \cos^3 x dx$

(07 Marks)

- c. Evaluate $\int_{-\pi/2}^{\pi/2} x^4 dx$

(06 Marks)

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OR

6 a. Evaluate $\int_{-3}^4 \int_{\text{Sky}} e^y dy dx$ (07 Marks)

b. Evaluate $\int x \sin^8 x dx$ (07 Marks)

c. Evaluate $\int_{-1}^2 \int_{-1}^1 \int_{-1}^1 (x^2 + y^2 + z^2) dx dy dz$ (06 Marks)

Module-4

7 a. If particle moves on the curve $x = 2t$, $y = t^2 - 4t$, $z = 3t - 5$ where t is the time. Find the velocity and acceleration at $t = 1$. (07 Marks)

b. Find the angle between the tangents to the curve $r = t^2 - 2t j - t^3 k$ at the point $t = \pm 1$. (07 Marks)

c. If $\mathbf{r}' = (3x^2 y - z)i + (xz^3 + y^4)j - 2x^3 z^2 k$ find $\text{grad}(\text{div } \mathbf{r})$ at $(2, -1, 0)$. (06 Marks)

OR

8 a. Find the directional derivative of $(I) = 4xz^3 - 3x^2 y^2 z$ at $(2, -1, 2)$ along $2i - 3j + 6k$ (07 Marks)

b. Find the unit normal to the surface $x^2 y + 2xz = 4$ at $(2, -2, 3)$. (07 Marks)

c. Show that $\mathbf{f} = (2xy^2 + yz)i + (2x^2 y + xz + 2yz^2)j + (2y^2 z + xy)k$ is irrotational. (06 Marks)

Module-5

9 a. Solve $\frac{dy}{dx} = \sin(x + y)$ (07 Marks)

b. Solve $\frac{dy}{dx} + y \cot x = \cos x$ (07 Marks)

c. Solve $(x - y + 1)dy - (x + y - 1)dx = 0$ (06 Marks)

OR

10 a. Solve $(1 + e^{-4})dx + e^y \left(\begin{array}{c|cc} 1 & x \\ \hline Y & \end{array} \right) dy = 0$. (07 Marks)

b. Solve $(x^3 \cos^2 y - x \sin 2y) dx = dy$. (07 Marks)

c. Solve $(3x^2 y^4 + 2xy)dx + (2x^3 y^3 - x^2)dy = 0$ (06 Marks)