

CBCS SCHEME

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17EC52

Fifth Semester B.E. Degree Examination, Dec.201 171.ili.2020 Digital Signal Processing

Time: 3 hrs.

Max. Marks: 100

Note: Answer ant' FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Show that finite duration sequence of length L can be reconstructed from the equidistant N samples of its Fourier transform, where $N \geq L$. (06 Marks)
- b. Compute the 6 - point DFT of the sequence $x(n) = 11, 0, 3, 2, 3, 0$. (08 Marks)
- c. Find the N-point DFT of the sequence $x(n) = a^n, 0 \leq n \leq N-1$. (06 Marks)

OR

- 2 a. Determine the 6-point sequence $x(n)$ having the DFT
 $X(K) = \{ 12, -3-j0, 0, 0, 0, -3+jJ \}$. (08 Marks)
- b. Derive the equation to express z - transform of a finite duration sequence in terms of its N-point DFT. (06 Marks)
- c. Compute the circular convolution of the sequences $x_1(n) = \{ 1, 2, 2, 1 \}$ and $x_2(n) = \{ 1, -1, -2, -2, -1 \}$. (06 Marks)

Module-2

- 3 a. State and prove the modulation property (multiplication in time-domain) of DFT. (06 Marks)
- b. The even samples of an eleven-point DFT of a real sequence are : $X(0) = 8, X(2) = -2 + j3, X(4) = 3 - j5, X(6) = 4 + j7, X(8) = -5 - j9$ and $X(10) = -1 - j2$. Determine the odd samples of the DFT. (06 Marks)
- c. An LTI system has impulse response $h(n) = \{ 2, 1, -1 \}$. Determine the output of the system for the input $x(n) = \{ 11, 2, 3, 3, 2, 11 \}$ using circular convolution method. (08 Marks)

OR

- 4 a. State and prove circular time reversal property of DFT. (06 Marks)
- b. Determine the number of real multiplications, real additions, and trigonometric functions required to compute the 8-point DFT using direct method. (04 Marks)
- c. Find the output $y(n)$ of a filter whose impulse response is $h(n) = \{ 1, 2, 1 \}$ and the input is $x(n) = \{ 3, -1, 0, 1, 3, 2, 0, 1, 2, 11 \}$ using overlap - add method, taking $N = 6$. (10 Marks)

Module-3

- 5 a. Compute the 8-point DFT of the sequence $x(n) = \cos(\pi n/4), 0 \leq n \leq 7$, using DIT-FFT algorithm. (10 Marks)
- b. Given $x(n) = \{ 11, 2, 3, 4 \}$, compute the DFT sample $X(3)$ using Goestzel algorithm. (06 Marks)
- c. Determine the number of complex multiplications and complex additions required to compute 64-point DFT using radix.2 FFT algorithm. (04 Marks)

17EC5:

OR

- 6 a. Determine the sequence $x(n)$ corresponding to the 8-point DFT $X(K) = (4, 1-j2.414, 0, 1-j0.414, 0, 1+j0.414, 0, 1+j2.414)$ using DIF-FFT algorithm. (10 Marks)
- b. Draw the signal flow graph to compute the 16-point DFT using DIT-FFT algorithm. (04 Marks)
- c. Write a short note on Chirp—z transform. (06 Marks)

Module-4

- 7 a. Draw the direct form I and direct form II structures for the system given by :

$$H(z) = \frac{z^{-1} - 3z^{-2}}{1 + 4z^{-1} + 2z^{-2} - 0.5z^{-3}} \quad (08 \text{ Marks})$$

- b. Design a digital Butterworth filter using impulse—invariance method to meet the following specifications :

$$0.8 \leq |H(e^{j\omega})| \leq 1, \quad 0 \leq \omega \leq 0.2\pi$$

$$|H(e^{j\omega})| \leq 0.2, \quad 0.2\pi \leq \omega \leq 0.5\pi$$

Assume $T = 1$.

(12 Marks)

OR

- 8 a. Draw the cascade structure for the system given by :

$$H(z) = \frac{(z-1)(z-3)(z^2 + 5z + 6)}{(z^2 + 6z + 5)(z^2 - 6z + 8)} \quad (08 \text{ Marks})$$

- b. Design a type-1 Chebyshev analog filter to meet the following specifications :

$$H(j\omega) \geq -5 \text{ dB}, \quad 0 \leq \omega \leq 1404 \text{ rad/sec}$$

$$H(j\omega) \leq -60 \text{ dB}, \quad 8268 \text{ rad/sec} \leq \omega < \infty$$

(12 Marks)

Module-5

- 9 a. Realize the linear phase digital filter given by :

$$H(z) = 1 + \frac{1}{2}z^{-1} + \frac{1}{3}z^{-2} + \frac{2}{5}z^{-3} + \frac{1}{3}z^{-4} + \frac{1}{2}z^{-5} + z^{-6} \quad (06 \text{ Marks})$$

- b. List the advantages and disadvantages of FIR filter compared with IIR filter. (04 Marks)
- c. Determine the values of $h(n)$ of a detail low pass filter having cutoff frequency $\omega_c = \pi/2$ and length $M = 11$. Use rectangular window. (10 Marks)

OR

- 10 a. An FIR filter is given by : $y(n) = \frac{1}{5}x(n) + \frac{3}{4}x(n-1) + \frac{1}{3}x(n-2) + \frac{1}{3}x(n-3)$. Draw the Lattice structure. (06 Marks)

- b. Determine the values of filter coefficients $h(n)$ of a high—pass filter having frequency response :

$$H_d(e^{j\omega}) = 1, \quad \frac{\pi}{4} \leq \omega \leq \frac{3\pi}{4}$$

$$H_d(e^{j\omega}) = 0, \quad \text{elsewhere}$$

Choose $M = 11$ and use Hanning windows.

(10 Marks)

- c. Write the time domain equations, widths of main lobe and maximum stop band attenuation of Bartlett window and Hanning window. (04 Marks)