

CBCS SCHEME

USN

15ME61

Sixth Semester S.E. Degree Examination, Dec.24-94n.2020 Finite Element Method

Time: 3 hrs.

Max. Marks: 80

Note: Answer FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. List the type of elements with neat sketch. (06 Marks)
- b. A simply supported beam subjected to point load at the centre. Derive an equation for maximum deflection using trigonometrically function by RR method. (10 Marks)

OR

- 2 a. List the advantages and disadvantages of FEM. (03 Marks)
- b. Explain Elasticity matrix [D] for stress and plain strain. (04 Marks)
- c. Explain simplex, complex and multiplex elements. (09 Marks)

Module-2

- 3 a. Derive the shape function, in natural coordinate system for:
 - (i) Constant strain triangle. (08 Marks)
 - (ii) I D bar element.
- b. Using two point Gaussian quadrature formula evaluate and compare with exact solution:

$$(i) \quad I = \int_{-1}^{+1} (1 + 2\xi^2 + 3\xi^4) d\xi$$

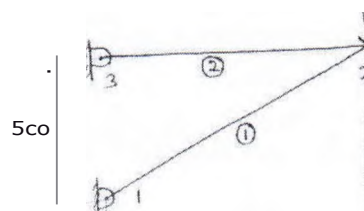
$$(ii) \quad I = \int_{-2}^{+2} (4 - \eta^2)^2 d\eta \quad (08 \text{ Marks})$$

OR

- 4 a. For the stepped bar shown in Fig. Q4 (a), determine the nodal displacement, element stresses and reaction at supports.
 $E_1 = 70 \text{ GPa}$; $E_2 = 200 \text{ GPa}$; $P = 200 \text{ kN}$; $A_1 = 2400 \text{ mm}^2$; $A_2 = 600 \text{ mm}^2$ (08 Marks)

Fig. Q4 (a)

- b. A plane truss shown in Fig. Q4 (b), determine nodal displacements, stresses in each element and reaction at supports.
 $E = 200 \text{ GPa}$; $A_1 = 1200 \text{ mm}^2$; $A_2 = 1000 \text{ mm}^2$; $P = 50 \text{ kN}$ (08 Marks)



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Module-3

- 5 a. Derive the Hermite function of a beam element. (08 Marks)
b. For the beam element shown in figure Q5 (b), determine the displacement and slope at the free end. Take $E = 70 \text{ GPa}$, $I = 4 \times 10^{-6} \text{ m}^4$ (08 Marks)

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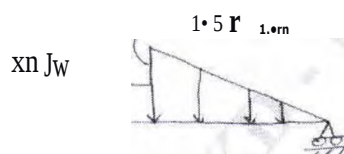
0.5 m

r

Fig. Q5 (b)

OR

- 6 a. Derive the stiffness matrix for a torsion element. (06 Marks)
b. Find the deflection and slopes at the nodes for the aluminium beam shown in Fig. Q6 (b). (10 Marks)



$E = 70 \text{ GPa}$
 $I = 2 \times 10^{-6} \text{ m}^4$

Fig. Q6 (b)

Module-4

- 7 a. With brief explanation obtain the rate equation that describes the rate of energy flow for the following conditions:
(i) Conduction (ii) Convection (iii) Radiation (06 Marks)
b. Derive the shape function of a 1 D bar element with temperature T_1 and T_2 at the nodes. (10 Marks)

OR

- 8 a. Determine the temperature distribution in the rectangular fin shown in Fig. Q8 (a). Neglect convection heat transfer and assume heat generated inside the fin as 500 W/m^3 (08 Marks)

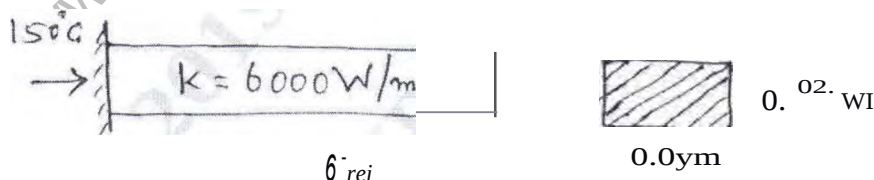


Fig. Q8 (a)

- b. Derive the stiffness matrix for fluid flow in 1 D bar element. (08 Marks)

Module-5

- 9 Derive the shape function for axisymmetric triangular element. (16 Marks)

OR

- 10 Derive the consistent mass matrix for the following:

- (i) 1 D bar element.
(ii) 1 D truss element.

(16 Marks)