

FACULTY
Pharm. D. (6 YDC) I-Year (Main & Backlog) Examination, July 2019
Subject: Remedial Mathematics
Time: 3 Hours
Max. Marks: 70
Note: Answer all questions from Part A, Answer any Five questions from Part B.
PART-A (10x2 = 20 Marks)

1. If $A = \begin{bmatrix} 1 \\ 3 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 6 & 7 \end{bmatrix}$ find AS
2. Find the value of $\begin{vmatrix} \tan x & \sec x \\ \sec x & \tan x \end{vmatrix}$
3. Find the value of 'a' if the distance between the points $(a, 2)$ and $(3, 4)$ is $\sqrt{8}$ units.
4. Find the centre and the radius of the circle $2x^2 + 2y^2 - 8x - 12y - 3 = 0$
5. Evaluate $\int \sec x \, dx$
6. Find the order and degree of the differential equation $1 + \left(\frac{dy}{dx}\right)^2 = 7\left(\frac{d^2y}{dx^2}\right)^3$
7. Find $\lim_{x \rightarrow 2} (3x^3 + 2x^2 + x)$
8. Solve $\frac{dy}{dx} = (x + y)^2$
9. Find the Laplace transform of $\{e^{at}\}$
10. If $z = 2xy + y^3 - 3$, find $\frac{\partial z}{\partial x}$ and $\frac{\partial z}{\partial y}$

PART-B (5x10=50)

11. (a) If $A = \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix}$ show that $A^2 - 5A = 14I$
 (b) Show that $\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^2 & b^2 & c^2 \end{vmatrix} = (a-b)(b-c)(c-a)$ 10M
12. (a) $\sin \theta = 3/5$ and θ is acute, find the value of $2\tan \theta + 3\sec \theta + 4\csc \theta$
 (b) Eliminate θ from $x = a \cos \theta$, $y = a \sin \theta$ show that $x^2 + y^2 = a^2$ 10M
13. (a) Find the equation of the circle passing through the points $(1, 1)$ $(-2, 2)$ $(-6, 0)$
 (b) Find the equation of the parabola whose Focus is $(-1, 1)$ and directrix is $x + y + 1 = 0$ 10M

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14. (a) If $u = \frac{x^3 + y^3}{x - y}$ then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \sin 2u$

(b) Find $\frac{dy}{dx}$ if $y = \frac{x^2 - 3x + 5}{x^2 + 3x + 5}$ 10M

15. (a) Evaluate $\int \frac{1}{1 + \cot x} dx$

(b) Evaluate $\int x^3 e^{2x} dx$ 10M

16. (a) Solve $(x+1) \frac{dy}{dx} + 1 = 2e^{-y}$

(b) $x^2 \frac{dy}{dx} = x^2 + xy + y^2$ 10M

17. (a) Find the Laplace transforms of $e^{-3t}(2 \cos 5t - 3 \sin 5t)$

(b) Find the Laplace transforms of $e^{-4t} + 3e^{-2t}$ 10M

18. (a) Find the equation of the circle whose centre is $(-3, 1)$ and passing through the centre of the circle $x^2 + y^2 + 2x - 4y + 4 = 0$

(b) Show that $\lim_{x \rightarrow 2} \frac{\tan(x-2)}{x^2 - 4} = \frac{1}{4}$ 10M
