

Roll No. 

Total No. of Pages : 02

Total No. of Questions : 09

B.Tech.(Automation &amp; Robotics) (2011 &amp; Onwards) (Sem.-3)

**MATHEMATICS – III**

Subject Code : BTAR-301

M.Code : 63001

Time : 3 Hrs.

Max. Marks : 60

**INSTRUCTIONS TO CANDIDATES :**

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

**SECTION-A****1. Write briefly :**

- a) What is the laplace transform of unit impulse function?
- b) Find Laplace transform of  $\frac{e^{-t} \sin t}{t}$
- c) Find the inverse Laplace Transform of  $\left(\log \frac{s+1}{s-1}\right)$
- d) Show that  $P_n(1) = 1$
- e) Prove that  $J_n(x) = \frac{x}{2n} [J_{n-1}(x) + J_{n+1}(x)]$
- f) Define analytic function.
- g) Show that the transformation  $w = \frac{2z+3}{z-4}$  maps the circle  $x^2 + y^2 - 4x = 0$  into straight line  $4u + 3 = 0$
- h) For conformal transformation  $w = z^2$  prove that angle of rotation at  $z = 1 + i$  is  $\pi/4$ .
- i) Find the nature and location of singularities of  $\frac{z - \sin z}{z^2}$
- j) Find the sum of residues of  $f(z) = \frac{\sin z}{z \cos z}$  at its poles inside the circle  $|z| = 2$ .

**SECTION-B**

2. Evaluate  $L\left(\sqrt{t} - \frac{1}{\sqrt{t}}\right)^3$
3. Find the inverse Laplace transform of  $\frac{5s+3}{(s-1)(s^2+2s+5)}$
4. Solve in series the equation
- $$9x(1-x)y'' - 12y' + 4y = 0$$
5. If  $u - v = (x - y)(x^2 + 4xy + y^2)$  and  $f(z) = u + iv$  is an analytic function of  $z = x + iy$ , find  $f(z)$  in terms of  $z$ .
6. Verify Cauchy's theorem by integrating  $e^{iz}$  along the boundary of triangle with the vertices at the points  $1 + i, -1 + i, -1 - i$ .

**SECTION-C**

7. Define Harmonic function. Show that the function
- $$u = e^{-2xy} \sin(x^2 - y^2)$$
- is harmonic. Find the conjugate function  $v$  and express  $u + iv$  as an analytic function of  $z$ .
8. Obtain the Fourier series for  $f(x) = \begin{cases} \pi x, & 0 \leq x \leq 1 \\ \pi(2-x), & 1 \leq x \leq 2 \end{cases}$
9. Expand  $\frac{1}{[(z-1)(z-2)]}$  in region
- $$|z| < 1, 1 < |z| < 2, |z| > 2, 0 < |z-1| < 1$$

**NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.**