Roll No.
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# B.Tech.(Aerospace Engg.) (2012 Onwards)/B.Tech.(ANE) (Sem.-4) <br> NUMERICAL ANALYSIS <br> Subject Code : ANE-204 <br> M.Code : 60512 

Time : 3 Hrs.
Max. Marks : 60

## INSTRUCTIONS TO CANDIDATES :

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

## SECTION-A

1. Answer briefly :
(a) Find the absolute error if $\mathrm{X}=0.00545828$ is truncated to three decimal digits.
(b) What is the order of convergence in Newton-Raphson method?
(c) Find a double root of the equation $x^{3}-5 x^{2}+8 x-4=0$ which is near 1.8 .
(d) What is Lagrange's interpolation formula?
(e) Find $y^{\prime}(0)$ from the following table:

| $x:$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y:$ | 4 | 8 | 15 | 7 | 6 | 2 |

(f) Solve the equations $x+y=2$ and $2 x+3 y=5$ using Gauss elimination method.
(g) What is the difference between direct and iterative method of solving simultaneous linear equations method?
(h) if $\frac{d y}{d x}=x+y, y(0)=1$, and $y^{(1)}=1+x+x^{2} / 2$ then what is the value of $y^{(2)}(x)$ using Picard's method?
(i) Write Milne's corrector formula.
(j) What is the standard 5-point formula to solve the Laplace equation $\mathrm{U}_{x x}+\mathrm{U}_{y y}=0$ ?

## SECTION-B

2. If $\mathrm{r}=\mathrm{h}\left(4 \mathrm{~h}^{5}-5\right)$, find the percentage error in r at $\mathrm{h}=1$ if the error in h is 0.04 .
3. Apply iteration method to find the negative root of the equation $x^{3}-2 x+5=0$ correct to four decimal places.
4. Find $f(22)$ from the Gauss forward formula :

| $x:$ | 20 | 25 | 30 | 35 | 40 | 45 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x):$ | 354 | 332 | 291 | 260 | 231 | 204 |

5. Find the maximum and minimum value of $y$ from the following table :

| $x:$ | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: |
| $y:$ | 2 | -0.25 | 0 | -0.25 | 2 | 15.75 | 56 |

6. Apply factorization method to solve the equations :
$3 x+2 y+7 z=4 ; 2 x+3 y+z=5 ; 3 x+4 y+z=7$.

## SECTION-C

Q7. Using Runge Kutta method of order 4, find y for $x=0.1,0.2,0.3$ given that $\frac{d y}{d x}=x y+y^{2}, y(0)=1$. Continue the solution at $\mathrm{x}=0.4$ using Milne's method.

Q8. Find the largest eigen value and the corresponding eigen vector of the matrix,

$$
\left(\begin{array}{ccc}
25 & 1 & 2 \\
1 & 3 & 0 \\
2 & 0 & -4
\end{array}\right) \text {. Take }\left[\begin{array}{lll}
1 & 0 & 0
\end{array}\right]^{\mathrm{t}} \text { as initial eigen vector. }
$$

Q9. Solve the Laplace equation $u_{x i}+\mathfrak{u}_{y y}=0$ in the domain of the following figure by Jacobi's method.


Fig. 1
NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.

