

Roll No. 

--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--

Total No. of Pages : 03

Total No. of Questions : 09

B.Tech (Automation &amp; Robotics) (2011 &amp; Onwards) (Sem.-5)

**NUMERICAL METHODS IN ENGINEERING**

Subject Code : ME-309

M.Code : 70482

Time : 3 Hrs.

Max. Marks : 60

**INSTRUCTIONS TO CANDIDATES :**

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt ANY FOUR questions.
3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt ANY TWO questions.

**SECTION-A****1. Write briefly :**

- i) Write Newton's formula for interpolation.
- ii) Find the condition number of the function  $f(x) = \sin x$ .
- iii) Define a cubic spline interpolant with clamped boundary.
- iv) Determine the Lagrange interpolating polynomial passing through the points (1, 1), (2, 4) and (3, 9).
- v) Find the  $l_\infty$  norm of the vector  $(1, -5, 9)^t$ .
- vi) Explain least square curve fitting.
- vii) Compute  $\int_0^2 x e^x dx$  using Simpson's rule.
- viii) Use the forward-difference formula to approximate the derivative of  $f(x) = \ln x$  at  $x_0 = 1.8$  using  $h = 0.1$ .

- xi) What is the order of convergence when Newton Raphson's method is applied to the equation  $x^2 - 6x + 9 = 0$  to find its multiple root.
- x) Out of chopping of numbers and rounding off of numbers, which one introduce less error?

### SECTION-B

2. Use forward-difference method with steps sizes  $h = 0.1$  and  $k = 0.01$  to approximate the solution to the heat equation :

$$\frac{\partial u}{\partial t}(x, t) - \frac{\partial^2 u}{\partial x^2}(x, t) = 0, \quad 0 < x < 1, t \geq 0,$$

with boundary conditions

$$u(0, t) = v(1, t) = 0, t > 0,$$

and initial condition

$$u(x, 0) = \sin(\pi x), 0 \leq x \leq 1.$$

3. Apply Taylor's method of order 2 with  $N = 10$  to initial value problem

$$y' = y - t^2 + 1, 0 \leq t \leq 2, y(0) = 0.5$$

4. The following data is given

1.0	1.3	1.6	1.9	2.2
0.7651977	0.6200860	0.4554022	0.2818186	0.1103623

Use Lagrange's formula to approximate  $f(1.5)$ .

5. Use the data points  $(0, 1)$ ,  $(1, e)$ ,  $(2, e^2)$  and  $(3, e^3)$  to form a natural spline  $S(x)$  that approximates  $f(x) = e^x$ .
6. Find the largest interval in which  $p^*$  must lie to approximate  $p$  with relative error at most  $10^{-4}$  for  $p = (17)^{\frac{1}{3}}$ .

**SECTION-C**

7. Derive Secant's formula for solving the equation  $f(x) = 0$  (specifying the assumptions made). Use the secant method to solve the equation  $x = \cos x$  starting with an initial guesses 0.5 and  $\frac{\pi}{4}$ .
8. Use Gauss elimination method with partial pivoting to solve the following linear system of equations.

$$\pi x_1 + \sqrt{2}x_2 - x_3 + x_4 = 0,$$

$$ex_1 - x_2 + x_3 + 2x_4 = 1,$$

$$x_1 + x_2 - \sqrt{3}x_3 + x_4 = 2,$$

$$-x_1 - x_2 + x_3 - \sqrt{5}x_4 = 3.$$

9. Determine the values of  $h$  that will ensure an approximation error of less than  $10^{-4}$  when approximating  $\int_0^2 e^{2x} \sin 3x dx$  and employing :
- a) Composite trapezoidal rule.
  - b) Composite Simpson's rule.

**NOTE : Disclosure of identity by writing mobile number or making passing request on any page of Answer sheet will lead to UMC case against the Student.**