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# GUJARAT TECHNOLOGICAL UNIVERSITY <br> B. Pharm. - SEMESTER-1 • EXAMINATION - SUMMER -2018 

Subject Code: 210006
Subject Name: Elementary (Remedial) Mathematics Time: 02:30 PM TO 05:30 PM Instructions:

1. Attempt any five questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
Q. 1 (a) Solve $x(x+5)(x+7)(x+12)=-150$
(b) Solve the following system of linear equations using Cramer's rule
$x+y+z=4,2 x-3 y+4 z=33$ and $3 x-2 y-2 z=2$
(c) Solve the following simultaneous equations
$\mathrm{x} 2+\mathrm{y} 2=185 ; \mathrm{x}+\mathrm{y}=19$
Q. 2 (a) Solve by Matrix Inversion method.
$-3 x_{1}+6 x_{2}-11 x_{3}=14$
$3 x_{1}-4 x_{2}+6 x_{3}=-5$
$4 x_{1}-8 x_{2}+13 x_{3}=-17$
(b) Using theorems prove that
$\left|\begin{array}{ccc}x & y & z \\ x^{2} & y^{2} & z^{2} \\ x^{3} & y^{3} & z^{3}\end{array}\right|=\mathrm{xyz}(\mathrm{x}-\mathrm{y})(-\mathrm{z})(\mathrm{z}-\mathrm{x})$
(c) A two digit number is four times the sum and three times the product of its
digits. Find the number.
Q. 3 (a) Calculate the mean and standard deviation from the following data

| Age | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> members | 3 | -61 | 132 | 153 | 140 | 51 | 2 |

(b) Calculate the mode and median for the following data.

05

| Class | $\theta-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 10 | 14 | 19 | 17 | 13 |

(c) The number N of bacteria in a culture grew at the rate proportional to N .
The value of N was initially 100 and increased to 332 in one hour. What will be
the value of N after 1.5 hours?
Q. 4 (a) Do as directed
(i) Find the value of $\tan 22^{1 \% / 2}$ (ii) Evaluate $\tan \frac{13 \pi}{12}$
(b) $\operatorname{Cos} \theta+\operatorname{Sin} \theta=\sqrt{2} \operatorname{Cos} \theta$, show that $\operatorname{Cos} \theta-\operatorname{Sin} \theta=\sqrt{2} \operatorname{Sin} \theta \quad \mathbf{0 5}$
(c) Prove that $\cos ^{4} \mathrm{~A}-\sin ^{4} \mathrm{~A}=1-2 \sin ^{2} \mathrm{~A} \quad 05$
Q. 5 (a) If $\sin \alpha=\frac{1}{\sqrt{5}}$ and $\cos \beta=\frac{3}{\sqrt{10}}$ and if $0<\alpha, \beta<\frac{\pi}{2}$, then prove that $\alpha+\beta=\frac{\pi}{4}$. 06
(b) Solve $\left(x y^{2}+x\right) d x+\left(y x^{2}+y\right) d y=0 \quad 05$
(c) A population grows at the rate of $8 \%$ per year. How long does it take for the 05 population to double?
Q. 6 (a) If $x^{y}=e^{x-y}$, prove that $d y / d x=\log x /(\log e x) 2 \quad 06$
(b) Evaluate: $\int \frac{3 x-5}{x^{2}-x-2}$
(c) Solve: $\left(x^{2}-y^{2}\right) d y=2 x y d x$ ..... 05
Q. 7 (a) In a group of students there are 4 girls and 6 boys. In how many ways a ..... 06 committee of five members can be formed such that I. There are at least 3 girls II. There are at the most 3 boys in the committee.
(b) Find the equation of the line passing through the points $(2,3)$ and $(5,-2)$. ..... 05
(c) Find the area of the triangle whose vertices are (4, 4), (3, -2$),(-3,16)$. ..... 05

