Code: 13A54101

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B.Tech I Year (R13) Supplementary Examinations December 2019

MATHEMATICS - I

(Common to all branches)

Time: 3 hours Max. Marks: 70

PART - A

(Compulsory Question)

Answer the following: (10 X 02 = 20 Marks)

- (a) Solve (x² y²)dx = 2xydy.
- (b) Solve the differential equation : (D⁴ 2D³ + 2D² 2D + 1) y = 0
- (c) Solve the differential equation: (x²D² 3xD+1) y = 0.
- (d) If $U = \log(x^3 + y^3 + z^3 3xyz)$ then find $\frac{\partial U}{\partial x} + \frac{\partial U}{\partial y} + \frac{\partial U}{\partial z}$.
- (e) If $x = r \cos \theta$, $y = r \sin \theta$ then find $\frac{\partial(x, y)}{\partial(r, \theta)}$?
- (f) If $f(x, y) = x^3 + 3xy^2 3x^2 3y^2 + 4$ then find critical points.
- Evaluate $\int_{0}^{1} \int_{0}^{1} \frac{1}{\sqrt{(1-x^2)(1-y^2)}} dxdy$.
- (h) Evaluate $\int_{0}^{a} \int_{0}^{x} \int_{0}^{x+y+z} e^{x+y+z} dxdydz$.
- Find $Curl \overline{F}$ for $\overline{F} = z\overline{i} + x\overline{j} + y\overline{k}$
- State Gauss divergence theorem.

PART – B (Answer all five units, 5 X 10 = 50 Marks)

- (a) Solve (D⁴ + 2D² + 1)y = e^x cos x
 - (b) Find the orthogonal trajectories of the family of confocal conics $\frac{x^2}{a^2} + \frac{y^2}{b^2 + \lambda} = 1$, where λ is a parameter.

OR

- (a) Solve (D² 2D + 1)y = x e^x sin x.
 - (b) Using method of variation of parameter Solve (D² + 4)y = tan 2x.

[UNIT - II]

- (a) Verify Rolle's theorem for the function $f(x) = \frac{\sin x}{x^2}$ in $[0, \pi]$.
 - (b) Find the coordinates of the centre of curvature at (at², 2at) on the parabola y² = 4ax.

- (a) Find the maximum and minimum values of $x^3 + 3xy^2 15x^2 15y^2 + 72x$.
 - (b) Find C of Cauchy's Mean Value theorem for f(x) = sin x, g(x) = cos x in a, b.

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UNIT - III

- 6 (a) Trace the curve y² (a x) = x² (a + x).
 - (b) Find the surface area of the solid of revolution of one loop of the curve $r^2 = a^2 \cos 2\theta$ about the initial line.

OR

- 7 (a) Evaluate $\int_{0}^{1} \int_{0}^{\sqrt{1+x^2}} \frac{dydx}{1+x^2+y^2}$.
 - (b) By changing the order of integration , evaluate $\int_{0}^{4a} \int_{\frac{x^{2}}{4a}}^{2\sqrt{ax}} dy dx$.

UNIT - IV

- 8 (a) Find the Laplace transform of: (i) $\left\{\frac{\sin 3t.\cos t}{t}\right\}$. (ii) $\left\{t^2\sin 2t\right\}$.
 - (b) Apply Convolution theorem to find $L^{-1}\left\{\frac{1}{(s+1)(s^2+1)}\right\}$.

OR

- 9 (a) Find the Laplace transform of e-3t (2 cos 5t 3 sin 5t)...
 - (b) Solve the D.E y'' 2y' 8y = 0, y(0) = 3, y'(0) = 6. Using Laplace transform.

UNIT - V

- 10 (a) Find the directional derivative of $xyz^2 + xz$ at (1, 1, 1) in the direction of i + 2j + 3k.
 - (b) Verify Green's theorem for $\int_C [(xy+y^2)dx + x^2 dy]$ where C is bounded by y=x and $y=x^2$.

OR

Verify Gauss divergence theorem for $\overline{F} = 4xy\overline{i} - \overline{y}^2\overline{j} + 4z\overline{k}$ where S is the surface of the cube bounded by x = 0, x = 1; y = 0, y = 1; z = 0, z = 1.

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