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Total No. of Questions : 18

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B.Tech. (ME) (2012 Onwards) (Sem.-5)

MATHEMATICS-III

Subject Code : BTAM-500

M.Code: 70601

Time: 3 Hrs.

Max. Marks : 60

INSTRUCTIONS TO CANDIDATES :

- 1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt ANY FOUR questions.
- 3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt ANY TWO questions.

## **SECTION-A**

## Write briefly :

- 1. Expand  $f(x) = |\sin x|$  in Fourier series.
- 2. Find Laplace transform of  $\sin h t \cos^2 t$ .
- 3. Find Laplace transform of  $\frac{e^{-at}}{t}$
- 4. Find inverse Laplace transform of  $\frac{e^{-s}}{(s-3)^3}$
- 5. Express  $x^4 + 2x^3 6x^2 + 5x 3$  in terms of Legendre polynomials.
- 6. For Legendre polynomial  $P_n(x)$ , show that  $P'_n(1) = \frac{n(n+1)}{2}$
- 7. Form a partial differential equation by eliminating arbitrary functions from the relation z = y f(x) + x g(y).
- 8. Solve x p + yq = 3z.
- 9. Show that the function  $f(z) = |z|^4$  satisfies the Cauchy-Riemann equations only at region.
- 10. State Cauchy Integral Theorem.

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## **SECTION-B**

11. Find the Fourier series expansion of the function  $f(x) = x^2$ ,  $-\pi < x < \pi$ . Deduce that

$$\frac{\pi^2}{6} = \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots$$

- 12. State and prove Convolution theorem for Laplace transform.
- 13. For Bessel's function  $J_n(x)$ , show that  $J_0^2 + 2(J_1^2 + J_2^2 + J_3^2 + ....) = 1$
- 14. Solve by Charpit's method  $q + xp = p^2$ .
- 15. Evaluate  $\oint_C \frac{dz}{(z^2+4)^2} = \frac{\pi}{16}, C: |z-i|=2$

## **SECTION-C**

- 16. a) Using Laplace transform, solve y' + 2y = 1 H(t 1), y(0) = 2, where H (t) is Heaviside's unit step function.
  - b) Find inverse Laplace transform of  $\frac{1}{s^2(s+1)}$ .
- 17. a) Using Frobenius method, find two linearly independent solutions of the equation  $2x^2y'' + xy' (x^2 + 1)y = 0$ .
  - b) A rod of length l with insulated side is initially at a uniform temperature  $u_0$ . Its ends are suddenly cooled at 0°C and kept at that temperature. Find the temperature function u(x, t).
- 18. a) Find all Taylor and Laurent series expansions of  $f(z) = \frac{1}{z(z-1)}$  about the point z=0.
  - b) Compute the residues at all the singular points of  $f(z) = \frac{z^2}{(z^2 + 1)^2}$ .

NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.

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