

Roll No. 

Total No. of Pages : 03

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M.Tech. (EE) (2018 Batch) (Sem.-2)

**ADVANCE CONTROL SYSTEM**

Subject Code : MTEE-203A-18

M.Code : 76102

Time : 3 Hrs.

Max. Marks : 60

**INSTRUCTIONS TO CANDIDATES :**

1. Attempt any FIVE questions out of EIGHT questions.
2. Each question carries TWELVE marks.

**SECTION-A**

Q1 Obtain the state space representation of the system shown below :

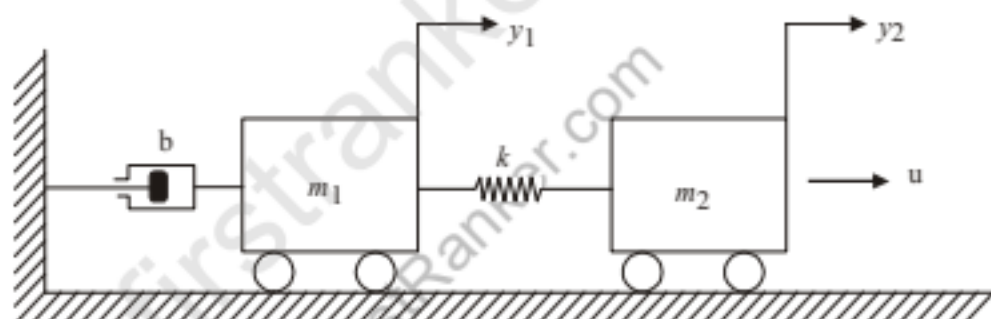


Fig.1

Q2 Consider the following state space representation of a system:

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 6 \end{bmatrix} u$$

$$y = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

Obtain the eigen values of the matrix A. Also develop the system in diagonal canonical form.

Q3 Define Observability. For the system defined by :

$$\dot{X} = AX + BU$$

Derive the condition for complete state Observability.

Q4 Discuss the properties of Lyapunov function. Discuss any two methods for finding out the Lyapunov function.

Q5 Consider the system given by:

$$\dot{X} = AX + BU$$

$$y = CX$$

$$A = \begin{bmatrix} -1 & 0 & 1 \\ 1 & -2 & 0 \\ 0 & 0 & -3 \end{bmatrix}, B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, C = [1 \quad 1 \quad 0]$$

Transform the system equations into observable and controllable canonical form.

Q6 Discuss the concept of an observer in control theory. Consider a system defined by :

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1.244 & 0.3956 & -3.145 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1.244 \end{bmatrix} u$$

$$y = [1 \quad 0 \quad 0] \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

Given the set of desired poles of the observer to be

$$s = -5 + j5\sqrt{3}, \quad s = -5 - j5\sqrt{3}, \quad s = -10$$

design a full order observer.

Q7 Determine the optimal control signal  $U$  for the system defined by:

$$\dot{X} = AX + BU$$

$$\text{Where } A = \begin{bmatrix} 0 & 1 \\ 0 & -1 \end{bmatrix} \text{ and } B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

Such that the following performance index is minimized:

$$J = \int_0^{\infty} (X^T X + U^2) dt$$

Q8 Write a short note on :

- (a) Similarity transformation
- (b) Kalman filter

**NOTE : Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.**