## Code No: 861AD

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD
MCA I Semester Examinations, October/ November - 2020 COMPUTER ORIENTED STATISTICAL METHODS
Time: 2 Hours
Max.Marks:75

## Answer any five questions <br> All questions carry equal marks

1.a) A random variable X has the following probability function.

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $f(x)$ | $k$ | $k$ | $k$ | $2 k$ | $3 k$ | $k^{2}$ | $2 k^{2}$ | $7 k^{2}+k$ |

Determine (i) $k$
(ii) Evaluate $p(x<6), p(x \geq 6)$ and $p(0<x<5)$
(iii) Mean and Variance
b) In a poker hand consisting of 5 cards, find the probability of holding 2 aces and 3jacks.
2.a) In a certain assembly plant, three machines, $B_{1}, B_{2}$, and $B_{3}$, make $30 \%, 45 \%$, and $25 \%$, respectively, of the products. It is known from past experience that $2 \%, 3 \%$ and $2 \%$ of the products made by each machine, respectively, are defective. Now, suppose that a finished product is randomly selected. What is the probability that it is defective? If it is defective find the probability that it is from
i) $B_{1}$
ii) $B_{2}$
iii) $B_{3}$
b) State and prove Bayes theorem.
3. Two ball point pens are selected at random from a box that contains 3 blue pens, 2 red pens, and 3 green pens. If $X$ is the number of blue pens selected and $Y$ is the number of red pens selected, find
a) The joint probability function $f(x, y)$,
b) $P[(X, Y) \in A]$, where $A$ is the region $\{(x, y) \mid x+y \leq 1\}$.
c) The covariance of X and Y .
4. Fit the binomial distribution

| x | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| f | 2 | 14 | 20 | 34 | 22 | 8 |

5.a) If X is a normal variate with mean 30 and standard deviation of 5. Find the probabilities that i) $26 \leq X \leq 40$,
ii) $X \geq 45$,
iii) $X \leq 22$.
b) Find i) $P(t<2.365)$ when $v=7$ degrees of freedom
ii) $P(t>1.318)$ when $v=24$ degrees of freedom
iii) $P(-1.356<t<2.179)$ when $v=12$ degrees of freedom.
6. An experiment was performed to compare the abrasive wear of two different laminated materials. Twelve pieces of material 1 were tested by exposing each piece to a machine measuring wear. Ten pieces of material 2 were similarly tested. In each case, the depth of wear was observed. The samples of material 1 gave an average wear of 85 units with a sample standard deviation of 4 , while the samples of material 2 gave an average of 81 with a sample standard deviation of 5 . In testing for the difference in the abrasive wear of the two materials, we assumed that the two unknown population variances were equal. Were we justified in making this assumption? Use a 0.10 level of significance.
7. A pair of dice are through 360 times and the frequency of each sum is indicated below

| Sum | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 8 | 24 | 35 | 37 | 44 | 65 | 51 | 42 | 26 | 14 | 14 |

Would you say that the dice are fair on the bâsis of the chi-square test at 0.05 level of significance?
8. Calculate the linear regression of Y on X from the data given below. Taking deviation from actual means of X and Y . Estimate the likely demand when price is Rs. 20. [15]

| X | 10 | 12 | 13 | 14 | 16 | 15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 40 | 38 | 43 | 45 | 37 | 43 |

