Code No: F3104
R09

# JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD MCA I Semester Examinations, June/July - 2018 PROBABILITY AND STATISTICS 

Time: 3hrs

Max.Marks:60

## Answer any five questions <br> All questions carry equal marks

1.a) A sub-committee of 6 members is to be formed out of a group consisting of 7 men and 4 women. Calculate the probability that the sub-committee will consist of (i) exactly 2 women and (ii) at least one women.
b) A, B and C wash $50 \%, 30 \%$ and $20 \%$ of the cars in a service station respectively. They fail to clean the glass in $5 \%, 7 \%$ and $3 \%$ of the cars respectively. The glass of a washed car is checked. What is the probability that the glass has been cleaned?
[6+6]
2.a) A random variable $X$ takes the values $1,2,3, \ldots$. and $P(X=n)=1 / 2^{n}, n=1,2,3, \ldots$. Find (i) $P(X$ is odd) (ii) $P(X \leq 5)$ (iii) $P(X$ is divisible by 5$)$.
b) A fair dice is rolled 5 times. Find the probability that 1 shows twice, 3 shows twice and 6 shows once.
3.a) Determine the binomial distribution for which the mean is 4 and variance is 3 . Also find $P(X=15)$.
b) Let $X$ be normally distributed with mean 8 and standard deviation 4. Find
i) $P(5 \leq X \leq 10)$
ii) $P(10 \leq X \leq 15)$
iii) $P(X \geq 15)$.
[6+6]
4.a) An insurance company has 25,000 automobile policy holders. If the yearly claim of a policy holder is a random variable with mean 320 and standard deviation 540, approximate the probability that the total yearly claim exceeds 8.3 million.
b) Let $X_{1}, X_{2}, X_{3}, \ldots \ldots \ldots . . . . X_{n}$ is an random sample from the population with respect to density function. $f(X)=\left\{\begin{array}{l}e^{-(x-Q)} \text { for } x>Q \\ 0 \text { otherwise }\end{array}\right.$. Show that $\bar{X}$ is an unbiased estimator of $Q$. Suggest an unbiased estimator of $Q$.
5.a) A random sample of 200 tins of coconut oil gave an average weight of 4.95 kgs with a standard deviation of 0.21 kg . Do we accept the hypothesis of net weight 5 kgs per tin at $1 \%$ level?
b) A sample of 10 house owners is drawn and the following values of their incomes are obtained. Mean Rs. 6,000; standard deviation Rs 650. Test the hypothesis that the average income of house owners of the town is Rs. 5,500.
[6+6]
6.a) Time taken by workers in performing a job are given below.

| Method I | 20 | 16 | 26 | 27 | 23 | 22 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Method II | 27 | 33 | 42 | 35 | 32 | 34 | 38 |

Test whether there is any significant difference between the variances at $5 \%$ level of significance of time distribution.
b) A sample analysis of examination results of 500 students was made. It was found that 220 students have failed, 170 have secured a third class, 90 have secured a second class and the rest, a first class. Do these figures support the general belief that the above categories are in the ratio $4: 3: 2: 1$ respectively?
7.a) Fit a straight line to the following data:

| Year: | 1969 | 1970 | 1971 | 1972 | 1973 | 1974 | 1975 | 1976 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sales(in lakhs <br> of Rs.): | 38 | 40 | 65 | 72 | 69 | 60 | 87 | 95 |

b) A fair die is rolled n times. Let $X$ be the number of 1's observed. let $Y$ be the number 2's be observed. Find $\operatorname{Cov}(X, Y)$ and $\rho(X, Y)$.
8. Find the rank correlation coefficient for the following data:

| $x$ | 92 | 89 | 87 | 86 | 86 | 77 | 71 | 63 | 53 | 50 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ | 86 | 83 | 91 | 77 | 68 | 85 | 52 | 82 | 37 | 57 |

