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Q. 1 – Q. 5 carry one mark each.

Q.1 An apple costs Rs. 10. An onion costs Rs. 8.

Select the most suitable sentence with respect to grammar and usage.

- (A) The price of an apple is greater than an onion.
- (B) The price of an apple is more than onion.
- (C) The price of an apple is greater than that of an onion.
- (D) Apples are more costlier than onions.
- Q.2 The Buddha said, "Holding on to anger is like <u>grasping</u> a hot coal with the intent of throwing it at someone else; you are the one who gets burnt."

Select the word below which is closest in meaning to the word underlined above.

- (A) burning (B) igniting (C) clutching (D) flinging
- Q.3 **M** has a son **Q** and a daughter **R**. He has no other children. **E** is the mother of **P** and daughter-inlaw of **M**. How is **P** related to **M**?
 - (A) \mathbf{P} is the son-in-law of \mathbf{M} . (B) \mathbf{P} is the grandchild of \mathbf{M} .
 - (C) \mathbf{P} is the daughter-in law of \mathbf{M} . (D) \mathbf{P} is the grandfather of \mathbf{M} .

Q.4 The number that least fits this set: (324, 441, 97 and 64) is _____.

- (A) 324 (B) 441 (C) 97 (D) 64
- Q.5 It takes 10 s and 15 s, respectively, for two trains travelling at different constant speeds to completely pass a telegraph post. The length of the first train is 120 m and that of the second train is 150 m. The magnitude of the difference in the speeds of the two trains (in m/s) is ______.
 - (A) 2.0 (B) 10.0 (C) 12.0 (D) 22.0

Q. 6 – Q. 10 carry two marks each.

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Q.6 The velocity V of a vehicle along a straight line is measured in m/s and plotted as shown with respect to time in seconds. At the end of the 7 seconds, how much will the odometer reading increase by (in m)?



Q.7 The overwhelming number of people infected with rabies in India has been flagged by the World Health Organization as a source of concern. It is estimated that inoculating 70% of pets and stray dogs against rabies can lead to a significant reduction in the number of people infected with rabies.

Which of the following can be logically inferred from the above sentences?

- (A) The number of people in India infected with rabies is high.
- (B) The number of people in other parts of the world who are infected with rabies is low.
- (C) Rabies can be eradicated in India by vaccinating 70% of stray dogs.
- (D) Stray dogs are the main source of rabies worldwide.
- Q.8 A flat is shared by four first year undergraduate students. They agreed to allow the oldest of them to enjoy some extra space in the flat. Manu is two months older than Sravan, who is three months younger than Trideep. Pavan is one month older than Sravan. Who should occupy the extra space in the flat?

	(A) Manu	(B) Sravan	(C) Trideep	(D) Pavan
Q.9	Find the area bour	nded by the lines 3x+2y=	=14, 2x-3y=5 in the first	quadrant.
	(A) 14.95	(B) 15.25	(C) 15.70	(D) 20.35



Q.10 A straight line is fit to a data set (ln x, y). This line intercepts the abscissa at ln x = 0.1 and has a slope of -0.02. What is the value of y at x = 5 from the fit?

(A) -0.030 (B) -0.014 (C) 0.014 (D) 0.030

END OF THE QUESTION PAPER

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Mathematics - MA

List of Symbols, Notations and Data

i.i.d. : independent and identically distributed

 $N(\mu, \sigma^2)$: Normal distribution with mean μ and variance σ^2 , $\mu \in (-\infty, \infty)$, $\sigma > 0$

E(X): Expected value (mean) of the random variable X

$$\Phi(t) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{t} e^{-\frac{x^2}{2}} dx$$

[x]: the greatest integer less than or equal to x

 \mathbb{Z} : Set of integers

 \mathbb{Z}_n : Set of integers modulo *n*

 \mathbb{R} : Set of real numbers

 \mathbb{C} : Set of complex numbers

 \mathbb{R}^n : *n*-dimensional Euclidean space

Usual metric *d* on \mathbb{R}^n is given by $d((x_1, x_2, ..., x_n), (y_1, y_2, ..., y_n)) = (\sum_{i=1}^n (x_i - y_i)^2)^{1/2}$

 ℓ_2 : Normed linear space of all square-summable real sequences

C[0,1]: Set of all real valued continuous functions on the interval [0,1]Ranker.com

 $\overline{B(0,1)} := \{(x,y) \in \mathbb{R}^2 : x^2 + y^2 \le 1\}$

 M^* : Conjugate transpose of the matrix M

 M^T : Transpose of the matrix M

Id : Identity matrix of appropriate order

 $\mathcal{R}(M)$: Range space of M

 $\mathcal{N}(M)$: Null space of M

 W^{\perp} : Orthogonal complement of the subspace W



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GATE 2016		Mathematics - MA
Q. 1 -	- Q. 25 carry one mark each	
Q.1	Let $\{X, Y, Z\}$ be a basis of \mathbb{R}^3 .	Consider the following statements P and Q:
	(P): $\{X + Y, Y + Z, X - Z\}$ is a	a basis of \mathbb{R}^3 .
	(Q): $\{X + Y + Z, X + 2Y - Z,$	$X - 3Z$ is a basis of \mathbb{R}^3 .
Which of the above statements hold TRUE?		ts hold TRUE?
	(A) both P and Q	(B) only P

- (C) only Q (D) Neither P nor Q
- Q.2 Consider the following statements P and Q:
 - (P): If $M = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 4 \\ 1 & 3 & 9 \end{bmatrix}$, then M is singular.
 - (Q) : Let *S* be a diagonalizable matrix. If *T* is a matrix such that *S* + 5 *T* = *Id*, then *T* is diagonalizable.

Which of the above statements hold TRUE?

(A) both P and Q

(C) only Q

(B) only P (D) Neither P nor Q

- Q.3 Consider the following statements P and Q:
 - (P): If *M* is an $n \times n$ complex matrix, then $\mathcal{R}(M) = (\mathcal{N}(M^*))^{\perp}$.
 - (Q) : There exists a unitary matrix with an eigenvalue λ such that $|\lambda| < 1$.

Which of the above statements hold TRUE?

- (A) both P and Q
- (C) only Q

(B) only P(D) Neither P nor Q



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GATE 20	016	Mathematics - MA
Q.4	Consider a real vector space <i>V</i> of dimension $T: V \rightarrow V$. If dimension $(T(V)) < n$ and <i>T</i> which of the following statements is TRUE?	<i>n</i> and a non-zero linear transformation $T^2 = \lambda T$, for some $\lambda \in \mathbb{R} \setminus \{0\}$, then
	(A) determinant(T) = $ \lambda ^n$ (B) There exists a non-trivial subspace V_1 of (C) T is invertible (D) λ is the only eigenvalue of T	f <i>V</i> such that $T(X) = 0$ for all $X \in V_1$
Q.5	Let $S = [0, 1) \cup [2, 3]$ and $f : S \rightarrow \mathbb{R}$ be a $f(S)$ is connected. Which of the following st	strictly increasing function such that catements is TRUE?
	 (A) <i>f</i> has exactly one discontinuity (B) <i>f</i> has exactly two discontinuities (C) <i>f</i> has infinitely many discontinuities (D) <i>f</i> is continuous 	
Q.6	Let $a_1 = 1$ and $a_n = a_{n-1} + 4$, $n \ge 2$. Then $\lim_{n \to \infty} \left[\frac{1}{a_1 a_2} + \frac{1}{a_2 a_3} \right]$ is equal to	$+ \cdots + \frac{1}{a_{n-1}a_n} \Big]$
Q.7	Maximum $\{x + y : (x, y) \in \overline{B(0,1)}\}$ is equal	to
Q.8	Let $a, b, c, d \in \mathbb{R}$ such that $c^2 + d^2 \neq 0$. Then $a u_x + b u_y = e^3$ u(x, y) = 0 on	hen, the Cauchy problem $x+y$, $x, y \in \mathbb{R}$, c x + d y = 0
	has a unique solution if	

(A) $a c + b d \neq 0$ (B) $a d - b c \neq 0$ (C) $ac - bd \neq 0$ (D) $a d + b c \neq 0$



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Q.9 Let u(x, t) be the d'Alembert's solution of the initial value problem for the wave equation

$$u_{tt} - c^2 u_{xx} = 0$$

$$u(x,0) = f(x), \ u_t(x,0) = g(x),$$

where *c* is a positive real number and *f*, *g* are smooth odd functions. Then, u(0,1) is equal to _____

Q.10 Let the probability density function of a random variable *X* be

$$f(x) = \begin{cases} x & 0 \le x < \frac{1}{2} \\ c(2x-1)^2 & \frac{1}{2} < x \le 1 \\ 0 & \text{otherwise.} \end{cases}$$

Then, the value of *c* is equal to _____

Q.11 Let *V* be the set of all solutions of the equation y'' + a y' + b y = 0 satisfying y(0) = y(1), where *a*, *b* are positive real numbers. Then, dimension(*V*) is equal to

Q.12 Let $y'' + p(x) y' + q(x)y = 0, x \in (-\infty, \infty)$, where p(x) and q(x) are continuous functions. If $y_1(x) = sin(x) - 2cos(x)$ and $y_2(x) = 2sin(x) + cos(x)$ are two linearly independent solutions of the above equation, then |4p(0) + 2q(1)| is equal to ______

Q.13 Let $P_n(x)$ be the Legendre polynomial of degree n and $I = \int_{-1}^{1} x^k P_n(x) dx$, where k is a non-negative integer. Consider the following statements P and Q: (P): I = 0 if k < n. (Q): I = 0 if n - k is an odd integer.

Which of the above statements hold TRUE?

(A) both P and Q(B) only P(C) only Q(D) Neither P nor Q



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ATE 20	16	Mathematics - MA			
Q.14	Consider the following statements P and Q:				
	(P): $x^2y'' + xy' + (x^2 - \frac{1}{4})$	y = 0 has two linearly independent Frobenius serie			
	solutions near $x = 0$.				
	(Q): $x^2y'' + 3\sin(x)y' + y = 0$ has two linearly independent Frobenius series				
	solutions near $x = 0$.				
	Which of the above statements hold TRUE?				
	(A) both P and Q	(B) only P			
	(C) only O	(D) Neither P nor Q			

- Q.15 Let the polynomial x^4 be approximated by a polynomial of degree ≤ 2 , which interpolates x^4 at x = -1, 0 and 1. Then, the maximum absolute interpolation error over the interval [-1, 1] is equal to ______
- Q.16 Let (z_n) be a sequence of distinct points in $D(0,1) = \{z \in \mathbb{C} : |z| < 1\}$ with $\lim_{n\to\infty} z_n = 0$. Consider the following statements P and Q:
 - (P) : There exists a unique analytic function f on D(0,1) such that $f(z_n) = sin(z_n)$ for all n.

(Q) : There exists an analytic function f on D(0,1) such that $f(z_n) = 0$ if n is even and $f(z_n) = 1$ if n is odd.

Which of the above statements hold TRUE?

- (A) both P and Q(B) only P(C) only Q(D) Neither P nor Q
- Q.17 Let (\mathbb{R}, τ) be a topological space with the cofinite topology. Every infinite subset of \mathbb{R} is
 - (A) Compact but NOT connected
 - (B) Both compact and connected
 - (C) NOT compact but connected
 - (D) Neither compact nor connected



GATE 201	16							Mathematic	cs - MA
Q.18	Let $c_0 =$	$\{(x_n):$	$x_n \in$	\mathbb{R} , $x_n \rightarrow$	• 0 } and <i>M</i>	$= \{(x_n) \in$	$c_0: x_1 +$	$x_2 + \cdots +$	$x_{10} = 0$
			10-1	`	_				

- Then, dimension $\binom{c_0}{M}$ is equal to _____
- Q.19 Consider $(\mathbb{R}^2, \|\cdot\|_{\infty})$, where $\|(x, y)\|_{\infty} = \max \|\|\cdot\|_{\infty}$. Let $f : \mathbb{R}^2 \to \mathbb{R}$ be defined by $f(x, y) = \frac{x+y}{2}$ and \tilde{f} the norm preserving linear extension of f to $(\mathbb{R}^3, \|\cdot\|_{\infty})$. Then, $\tilde{f}(1,1,1)$ is equal to ______

Q.20 $f : [0,1] \rightarrow [0,1]$ is called a shrinking map if |f(x) - f(y)| < |x - y| for all $x, y \in [0,1]$ and a contraction if there exists an $\alpha < 1$ such that $|f(x) - f(y)| \le \alpha |x - y|$ for all $x, y \in [0,1]$.

Which of the following statements is TRUE for the function $f(x) = x - \frac{x^2}{2}$?

- (A) f is both a shrinking map and a contraction
- (B) f is a shrinking map but NOT a contraction
- (C) f is NOT a shrinking map but a contraction
- (D) *f* is Neither a shrinking map nor a contraction
- Q.21 Let \mathbb{M} be the set of all $n \times n$ real matrices with the usual norm topology. Consider the following statements P and Q:
 - (P) : The set of all symmetric positive definite matrices in \mathbb{M} is connected.
 - (Q) : The set of all invertible matrices in ${\mathbb M}$ is compact.

Which of the above statements hold TRUE?

(A) both P and Q(B) only P(C) only Q(D) Neither P nor Q



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Mathematics - MA

Q.22 Let $X_1, X_2, X_3, ..., X_n$ be a random sample from the following probability density function for $0 < \mu < \infty$, $0 < \alpha < 1$,

$$f(x; \mu, \alpha) = \begin{cases} \frac{1}{\Gamma(\alpha)} (x - \mu)^{\alpha - 1} e^{-(x - \mu)}; & x > \mu \\ 0 & \text{otherwise} \end{cases}$$

Here α and μ are unknown parameters. Which of the following statements is TRUE?

- (A) Maximum likelihood estimator of only μ exists
- (B) Maximum likelihood estimator of only α exists
- (C) Maximum likelihood estimators of both μ and α exist
- (D) Maximum likelihood estimator of Neither μ nor α exists

Q.23 Suppose *X* and *Y* are two random variables such that aX + bY is a normal random variable for all $a, b \in \mathbb{R}$. Consider the following statements P, Q, R and S:

- (P) : *X* is a standard normal random variable.
- (Q) : The conditional distribution of *X* given *Y* is normal.
- (R) : The conditional distribution of X given X + Y is normal.
- (S) : X Y has mean 0.

Which of the above statements ALWAYS hold TRUE?

(A) both P and Q(C) both Q and S

(B) both Q and R(D) both P and S

Q.24 Consider the following statements P and Q:

(P) : If *H* is a normal subgroup of order 4 of the symmetric group S_4 , then $S_4/_H$ is

abelian.

(Q) : If $Q = \{\pm 1, \pm i, \pm j, \pm k\}$ is the quaternion group, then $\frac{Q}{(-1,1)}$ is abelian.

Which of the above statements hold TRUE?

- (A) both P and Q (B) only P
- (C) only Q (D) Neither P nor Q
- Q.25 Let *F* be a field of order 32. Then the number of non-zero solutions $(a, b) \in F \times F$ of the equation $x^2 + x y + y^2 = 0$ is equal to ______



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Q. 26 – Q. 55 carry two marks each.

Q.26 Let $\gamma = \{z \in \mathbb{C} : |z| = 2\}$ be oriented in the counter-clockwise direction. Let

$$I = \frac{1}{2\pi i} \oint_{\gamma} z^7 \cos\left(\frac{1}{z^2}\right) dz.$$

Then, the value of *I* is equal to _____

- Q.27 Let $u(x,y) = x^3 + a x^2 y + b x y^2 + 2 y^3$ be a harmonic function and v(x,y) its harmonic conjugate. If v(0,0) = 1, then |a + b + v(1,1)| is equal to ______
- Q.28 Let γ be the triangular path connecting the points (0,0), (2,2) and (0,2) in the counterclockwise direction in \mathbb{R}^2 . Then

$$I = \oint_{\gamma} \sin(x^{3})dx + 6xy dy$$

is equal to ______
Q.29 Let y be the solution of
Then y(1) is equal to
$$(A) \frac{2}{e} - \frac{2}{e^{2}}$$
$$(B) \frac{2}{e} - 2e^{2}$$
$$(D) 2 - 2e$$

Q.30 Let *X* be a random variable with the following cumulative distribution function:

$$F(x) = \begin{cases} 0 & x < 0\\ x^2 & 0 \le x < \frac{1}{2}\\ \frac{3}{4} & \frac{1}{2} \le x < 1\\ 1 & x \ge 1. \end{cases}$$

Then $P\left(\frac{1}{4} < X < 1\right)$ is equal to _____



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Q.31 Let γ be the curve which passes through (0,1) and intersects each curve of the family $y = c x^2$ orthogonally. Then γ also passes through the point

(A) $(\sqrt{2}, 0)$	(B) $(0, \sqrt{2})$
(C) (1,1)	(D) (-1,1)

Q.32 Let $S(x) = a_0 + \sum_{n=1}^{\infty} (a_n \cos(nx) + b_n \sin(nx))$ be the Fourier series of the 2π periodic function defined by $f(x) = x^2 + 4\sin(x)\cos(x), -\pi \le x \le \pi$. Then

$$\left|\sum_{n=0}^{\infty}a_n-\sum_{n=1}^{\infty}b_n\right|$$

is equal to _____

Q.33 Let y(t) be a continuous function on $[0, \infty)$. If

$$y(t) = t (1 - 4 \int_{0}^{t} y(x) dx) + 4 \int_{0}^{t} x y(x) dx,$$

then $\int_0^{\pi/2} y(t) dt$ is equal to _____

Q.34 Let $S_n = \sum_{k=1}^n \frac{1}{k}$ and $I_n = \int_1^n \frac{x - [x]}{x^2} dx$. Then, $S_{10} + I_{10}$ is equal to (A) $\ln 10 + 1$ (B) $\ln 10 - 1$

(A) In 10 + 1
(B) In 10 - 1
(C)
$$\ln 10 - \frac{1}{10}$$
(D) $\ln 10 + \frac{1}{10}$

Q.35 For any $(x, y) \in \mathbb{R}^2 \setminus \overline{B(0, 1)}$, let $f(x, y) = \text{distance}((x, y), \overline{B(0, 1)})$ $= \inf \{\sqrt{(x - x_1)^2 + (y - y_1)^2} : (x_1, y_1) \in \overline{B(0, 1)} \}.$

Then, $|| \nabla f (3,4) ||$ is equal to _____

Q.36 Let $f(x) = (\int_0^x e^{-t^2} dt)^2$ and $g(x) = \int_0^1 \frac{e^{-x^2(1+t^2)}}{1+t^2} dt$. Then $f'(\sqrt{\pi}) + g'(\sqrt{\pi})$ is equal to ______



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Q.41 The number of roots of the equation $x^2 - \cos(x) = 0$ in the interval $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$ is equal to _____



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GATE 201	6	Mathematics - M	1A
Q.42	For the fixed point iteration x_k .	$g_{k+1} = g(x_k), \ k = 0, 1, 2, \dots$, consider the following	lowing
	statements P and Q:		
	(P) : If $g(x) = 1 + \frac{2}{x}$ then the f	fixed point iteration converges to 2 for all x_0	∈ [1, 100].
	(Q): If $g(x) = \sqrt{2 + x}$ then the	e fixed point iteration converges to 2 for	
	all $x_0 \in [0, 100]$.		
	Which of the above statements	hold TRUE?	
	(A) both P and Q	(B) only P	
	(C) only Q	(D) Neither P nor Q	
Q.43	Let $T : \ell_2 \to \ell_2$ be defined by		
	$T((x_1, x_2, \cdots, x_n, \cdots))$)) = $(x_2 - x_1, x_3 - x_2, \dots, x_{n+1} - x_n, \dots)$.	
	Then		
	(A) $ T = 1$		
	(B) $ T > 2$ but bounded		
	(C) $1 < T \le 2$	all	
	(D) $ T $ is unbounded	, CO	
		XO	
Q.44	Minimize $w = x + 2y$ subject t	.0	
	Ċ	$2x + y \ge 3$ $x + y \ge 2$	
		$x \ge 0, y \ge 0.$	
	Then, the minimum value of w	is equal to	
	NN		
Q.45	Maximize $w = 11 x - z$ subjection	t to	
		$10 x + y - z \le 1$	
		$\begin{aligned} 2x - 2y + 2 &\leq 2\\ x, y, z \geq 0. \end{aligned}$	
	Then, the maximum value of <i>w</i>	is equal to	



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GATE 2016 Mathematics - MA Q.46 Let $X_1, X_2, X_3, ...$ be a sequence of i.i.d. random variables with mean 1. If N is a geometric random variable with the probability mass function $P(N = k) = \frac{1}{2^k}$; k = 1,2,3, ... and it is independent of the X_i 's, then $E(X_1 + X_2 + \dots + X_N)$ is equal to

- Q.47 Let X_1 be an exponential random variable with mean 1 and X_2 a gamma random variable with mean 2 and variance 2. If X_1 and X_2 are independently distributed, then $P(X_1 < X_2)$ is equal to ______
- Q.48 Let $X_1, X_2, X_3, ...$ be a sequence of i.i.d. uniform (0,1) random variables. Then, the value of

 $\lim_{n\to\infty} P(-\ln(1-X_1)-\cdots-\ln(1-X_n) \ge n)$

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is equal to _____
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Q.49 Let *X* be a standard normal random variable. Then, P(X < 0 ||[X]| = 1) is equal to



Q.50 Let $X_1, X_2, X_3, ..., X_n$ be a random sample from the probability density function $f(x) = \begin{cases} \theta \ \alpha \ e^{-\alpha x} + (1-\theta)2 \ \alpha \ e^{-2 \ \alpha x}; & x \ge 0 \\ 0 & \text{otherwise,} \end{cases}$ where $\alpha > 0, \ 0 \le \theta \le 1$ are parameters. Consider the following testing problem: $H_0: \theta = 1, \alpha = 1$ versus $H_1: \theta = 0, \alpha = 2$.

Which of the following statements is TRUE?

- (A) Uniformly Most Powerful test does NOT exist
- (B) Uniformly Most Powerful test is of the form $\sum_{i=1}^{n} X_i > c$, for some $0 < c < \infty$
- (C) Uniformly Most Powerful test is of the form $\sum_{i=1}^{n} X_i < c$, for some $0 < c < \infty$
- (D) Uniformly Most Powerful test is of the form $c_1 < \sum_{i=1}^n X_i < c_2$, for

some $0 < c_1 < c_2 < \infty$



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Q.51 Let X_1, X_2, X_3, \dots be a sequence of i.i.d. $N(\mu, 1)$ random variables. Then,

$$\lim_{n\to\infty}\frac{\sqrt{\pi}}{2n}\sum_{i=1}^n E(|X_i-\mu|)$$

is equal to _____

Q.52 Let $X_1, X_2, X_3, ..., X_n$ be a random sample from uniform $[1, \theta]$, for some $\theta > 1$. If $X_{(n)} = Maximum (X_1, X_2, X_3, ..., X_n)$, then the UMVUE of θ is

(A)
$$\frac{n+1}{n} X_{(n)} + \frac{1}{n}$$

(B) $\frac{n+1}{n} X_{(n)} - \frac{1}{n}$
(C) $\frac{n}{n+1} X_{(n)} + \frac{1}{n}$
(D) $\frac{n}{n+1} X_{(n)} + \frac{n+1}{n}$

- Q.53 Let $x_1 = x_2 = x_3 = 1$, $x_4 = x_5 = x_6 = 2$ be a random sample from a Poisson random variable with mean θ , where $\theta \in \{1, 2\}$. Then, the maximum likelihood estimator of θ is equal to ______
- Q.54 The remainder when 98! is divided by 101 is equal to ______ Q.55 Let *G* be a group whose presentation is $G = \{x, y \mid x^5 = y^2 = e, x^2y = yx\}.$ Then *G* is isomorphic to (A) \mathbb{Z}_5 (B) \mathbb{Z}_{10} (C) \mathbb{Z}_2 (D) \mathbb{Z}_{30}



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