

www.FirstRanker.com

DU MPhil Phd in Mathematics

Topic:- DU_J19_MPHIL_MATHS

1) Which of the following journals is published by Indian Mathematical Society

[Question ID = 13918]

- 1. Indian Journal of Pure and Applied Mathematics. [Option ID = 25669]
- Indian Journal of Mathematics. [Option ID = 25671]
- Ramanujan Journal of Mathematics. [Option ID = 25670]
- The Mathematics Students . [Option ID = 25672]

Correct Answer :-

- Indian Journal of Pure and Applied Mathematics. [Option ID = 25669]
- Name a Fellow of Royal Society who expired in 2019 [Question ID = 13917]
- 1. M. S. Ragunathan. [Option ID = 25665]
- Manjul Bhargava. [Option ID = 25666]
- 3. Michael Atiyah. [Option ID = 25667]
- 4. S. R. Srinivasa Varadhan. [Option ID = 25668]

Correct Answer :-

- M. S. Ragunathan. [Option ID = 25665]
- 3) Which of the following statements is true? [Question ID = 13973]

Every topological space having Bolzano-Weiestrass property is a compact space.

[Option ID = 25890]

2.

If $\{x_n\}$ is a convergent sequence in a topological space X with a limit x then $Y = \{x\} \cup \{x_n : n = 1, 2, \cdots\}$ is a compact subset of X.

[Option ID = 25891]

The projection map $p: X \times Y \to Y$ defined by p(x,y) = y is a closed map for all topological spaces X, Y.

[Option ID = 25889]

Every topological space is a first countable space.

[Option ID = 25892]

Correct Answer :-

The projection map $p: X \times Y \to Y$ defined by p(x,y) = y is a closed map for all topological spaces X, Y.

[Option ID = 25889]

4) Which of the following statements is true for topological spaces? [Question ID = 13927]

FirstRanker.com

Firstranker's choice www.FirstRanker.com

- Every first countable space is second cor
- Every first countable space is separable. [Option ID = 25707]

Correct Answer :-

- Every separable space is second countable. [Option ID = 25705]
- Which of the following statements is not true? [Question ID = 13997]
- If H and K are normal subgroups of G, then the subgroup generated by $H \cup K$ is also a normal subgroup of G.

www.FirstRanker.com

[Option ID = 25987]

Let G be a finite group and H a subgroup of order n. If H is the only subgroup of order n, then H is normal in G.

[Option ID = 25986]

The set of all permutations σ of S_n $(n \geq 3)$ such that $\sigma(n) = n$ is a normal subgroup of S_n .

[Option ID = 25985]

For groups G and H and $f: G \to H$ a group homomorphism. If H is abelian and V is a subgroup of G containing ker f then N is a normal subgroup of G.

[Option ID = 25988]

Correct Answer :-

The set of all permutations σ of S_n $(n \geq 3)$ such that $\sigma(n) = n$ is a normal subgroup of S_n .

[Option ID = 25985]

- 6) Which one of the following fellowship is based on merit in M.A/M.Sc. of the University [Question ID = 13920
- NBHM-JRF. [Option ID = 25679]
- 2. INSPIRE-JRF [Option ID = 25677]
- UGC-JRF. [Option ID = 25680]
- CSIR-JRF [Option ID = 25678]

Correct Answer :-

- INSPIRE-JRF [Option ID = 25677]
- The Abel prize 2019 was awarded to [Question ID = 13919]
- 1. Lennert Carleson. [Option ID = 25673]
- Mikhail Gromov. [Option ID = 25676]
- Karen Keskulla Uhlenbeck. [Option ID = 25674]
- 4. Peter Lax. [Option ID = 25675]

Correct Answer :-

Lennert Carleson. [Option ID = 25673]

www.FirstRanker.com Let X be a normed space over \mathbb{C} and f a non-zero linear functional on X. Then

[Question ID = 13981]

- f is surjective and a closed map. [Option ID = 25922]
- f is surjective and open. [Option ID = 25921]
- f is continuous and bijective. [Option ID = 25924]
- f is open and continuous. [Option ID = 25923]

Correct Answer :-

- f is surjective and open. [Option ID = 25921]
- Let $f: \mathbb{R} \to \mathbb{R}$ be defined as $f(x) = \begin{cases} x^2 \sin \frac{1}{x}, & x \neq 0 \\ 0, & x = 0 \end{cases}$. Then which of the following statements is not true?

[Ouestion ID = 13968]

- f is bounded above on (a, ∞) . [Option ID = 25869] f' is not continuous at 0. [Option ID = 25871]
- f is infinitly differentiable at every non zero $x \in \mathbb{R}$. [Option ID = 25870]
- f is neither convex nor concave on $(0, \delta)$.

f is bounded above on (a, ∞) . [Option ID = 25869]

10)

The principal part of the Laurent series of $f(z) = \frac{1}{z(z-1)(z-3)}$ in the annulus $\{z: 0 < |z| < 1\}$ is

[Question ID = 13988]

$$-\frac{1}{3z}$$
 [Option ID = 25951]

- 2. **Z**.[Option ID = 25949]
- 3. 3z [Option ID = 25952]

www.FirstRanker.com

2.[Option ID = 25949]

11) The general solution of the differential equation

$$\frac{dy}{dx} = \frac{y}{x} + \cot\frac{y}{x}$$

where c is a constant, is

[Question ID = 14009]

- cosec(y/x) = c/x. [Option ID = 26036]
- 2. cosec(y/x) = cx. [Option ID = 26035]
- 3. sec(y/x) = cx. [Option ID = 26033]
- sec(y/x) = c/x. [Option ID = 26034]

Correct Answer :-

sec(y/x) = cx. [Option ID = 26033]

Velocity potential for the uniform stream flow with velocity $\overline{q} = -Ui$, where U is constant and i is the unit vector in x-direction, past a stationary sphere of radius a and centre at origin, for $r \geq a$ is

[Question ID = 14008]

$$_{1.}U\cos heta\left(r+rac{1}{2}rac{a^{2}}{r^{3}}
ight) .$$
 [Option ID = 26029]

$$U\cos\theta\left(r^2+\frac{a^*}{r^3}\right)$$
.

$$U\cos heta\left(r^2+rac{a^2}{r^3}
ight)$$
 [Option ID = 26032] $U\cos heta\left(r^2+rac{1}{2}rac{a^2}{r^3}
ight)$ [Option ID = 26031]

$$U \cos \theta \left(r + \frac{a^2}{r^3}\right)$$
. [Option ID = 26030]

$$U\cos heta\left(r+rac{1}{2}rac{a^2}{r^3}
ight)$$
. [Option ID = 26029]

13)

Let X = P[a, b] be the linear space of all polynomials on [a, b]. Then which of the following statements is not true?

[Question ID = 13979]

- X is dense in C[a, b] with $||.||_p$ -norm, $1 \le p \le \infty$. [Option ID = 25916]
- X is a Banach space with $||.||_{p}$ norm, $1 \le p \le \infty$. [Option ID = 25913]
- X has a denumerable basis. [Option ID = 25915]
- X is incomplete with $||.||_{\infty}$ -norm. [Option ID = 25914]



. X is a Banach space with $||.||_{p^-}$ norm, $1 \le p \le \infty$. [Option ID = 25913]

14)

Let $W = \{(x, x, x) : x \in \mathbb{R}\}$ be a subspace of the inner product space \mathbb{R}^3 over \mathbb{R} . The orthogonal complement of W in \mathbb{R}^3 is the plane

[Question ID = 13995]

- 1. 2x + y + z = 0. [Option ID = 25979]
- 2. x + 2y + z = 0. [Option ID = 25978]
- 3. x + y + z = 0. [Option ID = 25980]
- x + y + 2z = 0. [Option ID = 25977]

Correct Answer :-

x + y + 2z = 0. [Option ID = 25977]

15

The integral surface of the partial differential equation $x^2p + y^2q + z^2 = 0$, $p = \frac{\partial z}{\partial x}$, $q = \frac{\partial z}{\partial y}$ which passes through the hyperbola xy = x + y, z = 1 is

[Question ID = 14007]

- 1. $\frac{1}{x} + \frac{2}{y} + \frac{1}{z} = 3$. [Option ID = 26027]
- $\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 3.$ [Option ID = 26028]
- $\frac{2}{x} + \frac{1}{y} + \frac{1}{z} = 3.$ [Option ID = 26026]
- $\frac{1}{x} + \frac{1}{y} + \frac{2}{z} = 3.$ [Option ID = 26025]

Correct Answer :-

$$\frac{1}{x} + \frac{1}{y} + \frac{2}{z} = 3.$$
 [Option ID = 26025]

16)

The value of $\oint_C x^2 dx + (xy + y^2) dy$, where C is the boundary of the region R bounded by y = x and $y = x^2$ and is oriented in positive direction is

[Question ID = 13969]

- 1. 1/15 [Option ID = 25876]
- 2. 2 [Option ID = 25875]
- 1/10 [Option ID = 25874]
- 4. 1/5 [Option ID = 25873]

Correct Answer :-

1/5 [Option ID = 25873]

17

Firstranker's choice

www.FirstRanker.com

- lines parallel to z-axis. [Option ID = 25975]
- lines perpendicular to z-axis. [Option ID = 25976]
- planes perpendicular to xz- plane. [Option ID = 25973]
- planes parallel to yz- plane. [Option ID = 25974]

Correct Answer :-

planes perpendicular to xz- plane. [Option ID = 25973]

18)

Let R be a ring with unity. An element a of R is called nilpotent if $a^n = 0$ for some positive integer n. An element a of R is called unipotent if and only if 1-ais nilpotent. Consider the following statements:

- (I) In a commutative ring with unity, product of two unipotent elements is invertible.
- (II) In a ring with unity, every unipotent element is invertible. Then

[Question ID = 14001]

- Neither (I) nor (II) is correct. [Option ID = 26004]
- 2. Both (I) and (II) are correct. [Option ID = 26003]
- Only (I) is correct. [Option ID = 26001]
- Only (II) is correct. [Option ID = 26002]

Correct Answer :-

- Only (I) is correct. [Option ID = 26001
- Which of the following statements is not true?

[Question ID = 13970]

$$g_n(x) = \frac{1}{n(1+x^2)} \to 0, n \to \infty$$
 uniformly on \mathbb{R} .

 $h_n(x) = \frac{\sin nx}{n}$ converges uniformly on \mathbb{R} .

 $f_n(x) = \frac{x^2 + nx}{x}$ converges uniformly on \mathbb{R} .

[Option ID = 25878]

[Option ID = 25877]

$$u_n(x) = \frac{x^n}{n}$$
 converges uniformly on [0, 1].

[Option ID = 25880]

Correct Answer :-



Firstranker's choice $g_n(x) = \frac{1}{n(1+x^2)} \to 0, n \to \infty$ uniformly on \mathbb{R} .

www.FirstRanker.com

[Option

[Option ID = 25877]

20)

The value of the integral $\int_C \frac{dz}{z^2+4}$ where C is the anticlockwise circle |z-i|=2 is

[Question ID = 13984]

- 1. 2π . [Option ID = 25935]
- 2. 0 [Option ID = 25933]
- 3. $\pi/2$. [Option ID = 25934]
- π. [Option ID = 25936]

Correct Answer :-

0 [Option ID = 25933]

21)

Which of the following statements is true for the product $\prod_{\alpha \in \Lambda} X_{\alpha}$ with product topology of a family $\{X_{\alpha}\}_{\alpha \in \Lambda}$ of topological spaces?

[Question ID = 13974]

- If each X_{α} is metrizable then $\prod_{\alpha \in \Lambda} X_{\alpha}$ is metrizable. [Option ID = 25895]
- If each X_{α} is normal then $\prod_{\alpha \in \Lambda} X_{\alpha}$ is normal. [Option ID = 25893]

If each X_{α} is completely regular then $\prod_{\alpha \in \Lambda} X_{\alpha}$ is completely regular.

If each X_{α} is locally connected then $\prod_{\alpha \in \Lambda} X_{\alpha}$ is locally connected.

[Option ID =

Correct Answer :-

If each X_{α} is normal then $\prod_{\alpha \in \Lambda} X_{\alpha}$ is normal. [Option ID = 25893]

Consider \mathbb{R} with usual metric and a continuous map $f : \mathbb{R} \to \mathbb{R}$ then

[Question ID = 13975]

- f(A) is bounded for every bounded subset A of \mathbb{R} . [Option ID = 25899]
- f is bounded. [Option ID = 25897]
- $_{3.}$ $f^{-1}(A)$ is compact for all compact subset A of \mathbb{R} . [Option ID = 25900]
- Image of f is an open subset of R. [Option ID = 25898]

Correct Answer :-

f is bounded. [Option ID = 25897]

Firstranker's choice Define a sequence of funwww.FifstRanker.com

www.FirstRanker.com

$$f_n(x) = \begin{cases} 1, & \text{if } x \in [-n-2, -n) \\ 0, & \text{otherwise.} \end{cases}$$

Let $\alpha = \int_{-\infty}^{\infty} \lim_{n \to \infty} f_n(x) dx$ and $\beta = \lim_{n \to \infty} \int_{-\infty}^{\infty} f_n(x) dx$. Then

[Question ID = 13986]

1. $0 < \alpha < 1, \beta = 1$ [Option ID = 25942]

2. $\alpha = 0$, $\beta = \infty$. [Option ID = 25943]

3. $\alpha = \beta = \emptyset$. [Option ID = 25941]

4. $\alpha = 0$, $\beta = 2$. [Option ID = 25944]

Correct Answer :-

α = β = 0. [Option ID = 25941]

24)

Suppose f is an entire function with f(0) = 0 and u be the real part of f such that $|u(x, y)| \le 1$ for all $(x, y) \in \mathbb{R}^2$. Then the range of u is

[Question ID = 13985]

1. [-1, 1]. [Option ID = 25938]

2. [0, 1]. [Option ID = 25937]

3. {0}. [Option ID = 25939]

[-1, 0]. [Option ID = 25940]

Correct Answer :-

[0, 1]. [Option ID = 25937]

25)

For the minimal splitting field F of a polynomial f(x) of degree n over a field K. Consider the following statements:

F over K is a normal extension.

(II) n | [F : K].

(III) F over K is a separable extension.

Then

[Question ID = 14002]

- All (I), (II) and (III) are true. [Option ID = 26007]
- 2. None of (I), (II) and (III) is true. [Option ID = 26008]
- Only (I) is true. [Option ID = 26005]
- 4. Only (I) and (II) are true. [Option ID = 26006]

Correct Answer :-

Only (I) is true. [Option ID = 26005]

261

Firstranker's choice Let $V = \{x + \alpha y : \alpha, x, y \in \mathcal{W}$ will its tranker some space www. Firstranker som

[Question ID = 13991]

- 1. 2 [Option ID = 25963]
- 1 [Option ID = 25964]
- 3. 3 [Option ID = 25962]
- 4. infinity. [Option ID = 25961]

Correct Answer :-

infinity. [Option ID = 25961]

27

Let $X = \mathbb{C}^2$ with $||.||_1$ norm and $X_0 = \{(x_1, x_2) \in X : x_2 = 0\}$. Define $g: X_0 \to \mathbb{C}$ by $g(x) = x_1, x = (x_1, 0)$. Consider the following statements:

- (I) Every f ∈ X' (dual space of X) is of the form f(x₁, x₂) = ax₁ + bx₂ for some a, b ∈ C.
- (II) Hahn-Banach extensions of g are precisely of the form $f(x) = x_1 + bx_2$, $x = (x_1, x_2) \in X$, $|b| \le 1$, $b \in \mathbb{C}$.

Then

[Question ID = 13982]

- 1. (I) is true but (II) is false. [Option ID = 25925]
- 2. (I) is false but (II) is true. [Option ID = 25926]
- Neither (I) nor (II) is true. [Option ID = 25927]
- 4. Both (I) and (II) are true. [Option ID = 25928

Correct Answer :-

(I) is true but (II) is false. [Option ID 25925]

28)

Which of the following statements is not true for a subset A of a metric space X, whose closure is \overline{A} ?

[Question ID = 13978]

- 1. If X is totally bounded then \underline{A} is totally bounded. [Option ID = 25911]
- A is connected if and only if \overline{A} is connected. [Option ID = 25912]
- 3. A is bounded if and only if \overline{A} is bounded. [Option ID = 25909]
- 4. A is totally bounded if and only if A is totally bounded. [Option ID = 25910]

Correct Answer :-

- . A is bounded if and only if A is bounded. [Option ID = 25909]
- 29) How many pairs of elements are there that generate

$$D_8 = \langle a, b | a^4 = b^2 = 1, ab = ba^{-1} \rangle$$

www.FirstRanker.com

2. 5 [Option ID = 25991]

- 3. 8 [Option ID = 25992]
- 4. 4 [Option ID = 25990]

Correct Answer :-

2 [Option ID = 25989]

30

For each $n \in \mathbb{N}$, define $x_n \in C[0, 1]$ by

$$x_n(t) = \begin{cases} n^2 t, & 0 \le t \le 1/n \\ 1/t, & 1/n < t \le 1 \end{cases}$$

where C[0, 1] is endowed with sup-norm. Then which of the following is not true:

[Question ID = 13983]

- The sequence $\{x_n\}_{n\in\mathbb{N}}$ is uniformly bounded on [0, 1]. [Option ID = 25931]
- Each x_n is uniformly continuous on [0, 1]. [Option ID = 25932]
- The set $\{x_n(t): n \in \mathbb{N}\}$ is bounded for each $t \in [0, 1]$. [Option ID = 25929]
- $||x_n||_{\infty} \leq n \text{ for all } n.$ [Option ID = 25930]

Correct Answer :-

The set $\{x_n(t): n \in \mathbb{N}\}$ is bounded for each $t \in [0, 1]$.

31)

The eigenvalues of the boundary value problem $y'' + y' + (1 + \lambda)y = 0$, y(0) = 0, y(1) = 0 are

[Question ID = 14005]

- $_{1.}$ $-\frac{3}{4}+n^{2},\ n\in\mathbb{N}.$ [Option ID = 26018]
- $\frac{3}{4} + n^2 \pi^2, n \in \mathbb{N}.$ [Option ID = 26019]
- $-\frac{3}{4} + n^2 \pi^2, n \in \mathbb{N}.$ [Option ID = 26020]
- $\frac{3}{4} + n^2, \, n \in \mathbb{N}.$ [Option ID = 26017]

Correct Answer :-

$$\frac{3}{4}+n^2,\,n\in\mathbb{N}.$$
 [Option ID = 26017]

32)

Let (X, d) be a complete metric space. Then which of the following statements holds true?

[Question ID = 13976]

Firstranker's choice is cowwwtFirstRanker.com

www.FirstRanker.com

2.

If $\{F_n\}$ is a decreasing sequence of non-empty closed subsets of X then $F = \bigcap_{n=1}^{\infty} F_n$ is non-empty.

[Option ID = 25903]

Every open subspace of X is complete. [Option ID = 25904]

If X is union of a sequence of its subsets then the closure of at least one set in the sequence must have non-empty interior.

[Option ID = 25901]

Correct Answer :-

If X is union of a sequence of its subsets then the closure of at least one set in the sequence must have non-empty interior.

[Option ID = 25901]

33)

Let V be the set of all polynomials over \mathbb{R} . A linear transformation $D:V\to V$ is defined by $D(f(x))=\frac{d^3}{dx^3}(f(x))$. Then

[Question ID = 13993]

- dimension of kernel of D is 2. [Option ID = 25969]
- dimension of kernel of D is 4. [Option ID = 25970]
- range of D = V . [Option ID = 25972]
- 4. range of p is a finite dimensional space [Option ID = 25971]

Correct Answer :-

dimension of kernel of D is 2. [Option ID = 25969]

³⁴⁾ If $G = \mathbb{Z}_6 \oplus \mathbb{Z}_{20} \oplus \mathbb{Z}_{72}$, then G is isomorphic to

[Question ID = 14000]

- $\mathbb{Z}_8 \oplus \mathbb{Z}_9 \oplus \mathbb{Z}_{40}$. [Option ID = 25998]
- 2. $\mathbb{Z}_2 \oplus \mathbb{Z}_{12} \oplus \mathbb{Z}_{360}$. [Option ID = 26000]
- $\mathbb{Z}_5 \oplus \mathbb{Z}_{27} \oplus \mathbb{Z}_{64}$. [Option ID = 25997]
- 4. Z₆ ⊕ Z₃₂ ⊕ Z₄₅. [Option ID = 25999]

Correct Answer :-

 $\mathbb{Z}_5 \oplus \mathbb{Z}_{27} \oplus \mathbb{Z}_{64}$. [Option ID = 25997]

35)

FirstRanker.com

Firstranker's choice The general solution of the pwww.FirstRanker.com

$$\frac{\partial^2 z}{\partial x \partial y} + \frac{\partial z}{\partial x} - \frac{\partial z}{\partial y} - z = xy$$

is

[Question ID = 14006]

$$e^x f_1(y) + e^{-y} f_2(x) + xy + y - x - 1$$
. [Option ID = 26023]

$$e^x f_1(y) + e^{-y} f_2(x) - xy - y + x + 1.$$
 [Option ID = 26022]

$$e^{-x}f_1(y) + e^yf_2(x) + xy + y - x - 1.$$
 [Option ID = 26024]

$$e^{-x}f_1(y) + e^yf_2(x) - xy - y + x + 1.$$
 [Option ID = 26021]

Correct Answer :-

$$e^{-x}f_1(y) + e^yf_2(x) - xy - y + x + 1.$$
 [Option ID = 26021]

36

The function $f:[0,2\pi]\to S^1$ defined by $f(t)=e^{it}$, where S^1 is the unit circle, is

[Question ID = 13972]

- 1. continuous, one-one but not onto. [Option ID = 25886]
- 2. not a continuous map. [Option ID = 25885]
- 3. a continuous bijection but not an open map. [Option ID = 25887]
- 4. a homeomorphism. [Option ID = 25888]

Correct Answer :-

- not a continuous map. [Option ID = 25885]
- 37) Define f on C by

$$f(z) = \begin{cases} \frac{(\overline{z})^2}{z}, & \text{if } z \neq 0 \\ 0, & z = 0. \end{cases}$$

Let u and v denote the real and imaginary parts of f. Then at the origin

[Question ID = 13990]

- u, v do not satisfy the Cauchy Riemann equations but f is differentiable.
- u, v satisfy the Cauchy Riemann equations but f is not differentiable [Option ID = 25958]
- $_3$. f is differentiable and u, v satisfy the Cauchy Riemann equations. [Option ID = 25957]
 - f is not differentiable and u, v do not satisfy the Cauchy Riemann equations.

[Option ID = 25960]

Firstranker's choice and u, v www.firstranker.com

Let V be the set of all polynomials over \mathbb{R} . Define $W = \{x^n f(x) : f(x) \in V\}$, $n \in \mathbb{N}$ is fixed. Then which of the following statements is not true?

[Question ID = 13992]

- V is infinite dimensional over \mathbb{R} . [Option ID = 25967]
- The quotient space V/W is finite dimensional. [Option ID = 25966]
- W is not a subspace of V. [Option ID = 25965]
- V has linearly independent set of m vectors for every $m \in \mathbb{N}$. [Option ID = 25968]

Correct Answer :-

W is not a subspace of V. [Option ID = 25965]

Navier Stokes equation of motion for steady viscous incompressible fluid flow in absence of body force is (where \overline{q} , p, ρ , $\overline{\varsigma}$ and ν are velocity, pressure, density, vorticity, and kinematic coefficient of viscosity respectively)

[Question ID = 14004]

$$\nabla \left(\frac{1}{2}\overline{q}^2 - \frac{p}{\rho}\right) + \overline{q} \times \overline{\varsigma} = \nu \nabla^2 \overline{q}.$$
[Option ID = 26015]
$$\nabla \left(\frac{1}{2}\overline{q}^2 + \frac{p}{\rho}\right) - \overline{q} \times \overline{\varsigma} = \nu \nabla^2 \overline{q}.$$
[Option ID = 26014]

$$\nabla \left(\frac{1}{2}\overline{q}^2 + \frac{p}{\rho}\right) - \overline{q} \times \overline{\varsigma} = \nu \nabla^2 \overline{q}.$$
 [Option ID = 26014]

$$\nabla(\frac{1}{2}\overline{q}^2 + \frac{p}{\rho}) + \overline{q} \times \overline{\varsigma} = \nu\nabla^2\overline{q}.$$
[Option ID = 26013]

$$abla (\overline{q}^2 + \frac{p}{
ho}) - \overline{q} imes \overline{\varsigma} = -
u
abla^2 \overline{q}.$$
[Option ID = 26013]

Correct Answer :-

$$\nabla(\frac{1}{2}\overline{q}^2 + \frac{p}{\rho}) + \overline{q} \times \overline{\varsigma} = \nu \nabla^2 \overline{q}.$$
 [Option ID = 26013]

40)

Let $X = C_{00}$ (the space of all real sequences having only finitely many non-zero terms) with $||.||_{\infty}$ -norm. Define $P: X \to X$ by

$$P(x)(2j-1) = x(2j-1) + jx(2j)$$

 $P(x)(2j) = 0$

for $x \in X$, $j \in \mathbb{N}$. Then which of the following statements is not true?

[Question ID = 13980]

Firstranker's choice www.FirstRanker.com

www.FirstRanker.com

- _{2.} P is linear and $P^2 = P$. [Option ID = 25917]
- Range(P) is a closed subspace of X. [Option ID = 25919]
- P is a continuous map. [Option ID = 25920]

Correct Answer :-

. P is linear and $P^2 = P$. [Option ID = 25917]

41)

The value of $\int_C 2x \, ds$, where C consists of the arc C_1 of the parabola $y = x^2$ from (0, 0) to (1, 1) followed by the line segment from (1, 1) to (0, 0) is

[Question ID = 13971]

$$\int_{1}^{6} \frac{5\sqrt{5}-1}{6} + 2\sqrt{2}.$$
 [Option ID = 25882]

$$\frac{5\sqrt{5}-4}{3}+2\sqrt{2}$$
.

[Option ID = 25884]

$$\frac{5\sqrt{5}-1}{6}+\sqrt{2}$$
. [Option ID = 2588]

$$\frac{3\sqrt{5}-1}{5}+\sqrt{2}$$
.

[Option ID = 25883]

Correct Answer :-

$$\frac{5\sqrt{5}-1}{6} + \sqrt{2}$$

42)

For each integer n, define $f_n(x) = x + n$, $x \in \mathbb{R}$ and let $G = \{f_n : n \in \mathbb{Z}\}$. Then

[Question ID = 13999]

- G is a cyclic group under composition. [Option ID = 25994]
- G is a non-cyclic group under composition. [Option ID = 25995]
- G does not form a group under composition. [Option ID = 25993]
- G is a non-abelian group under composition. [Option ID = 25996]

Correct Answer :-

G does not form a group under composition. [Option ID = 25993]

43)

Suppose G is an open connected subset of \mathbb{C} containing 0 and $f: G \to \mathbb{C}$ is analytic such that f(0) = 0 and |f(z) - 1| = 1 for all $z \in G$. Then the range of f

www.FirstRanker.com

$$\begin{array}{l} {}_{1.} \left\{0,\,2\right\}_{\text{:[Option ID = 25954]}} \\ {}_{2.} \left\{1+e^{i\theta}:\,0\leq\theta\leq\pi\right\}_{\text{[Option ID = 25956]}} \\ {}_{3.} \left\{1+e^{i\theta}:\,0\leq\theta\leq2\pi\right\}_{\text{:[Option ID = 25953]}} \\ {}_{4.} \left\{0\right\}_{\text{[Option ID = 25955]}} \end{array}$$

Correct Answer :-

$$\{1 + e^{i\theta}: 0 \le \theta \le 2\pi\}.$$
 [Option ID = 25953]

44) Consider the following statements:

Dimension of kinematic coefficient of viscosity is

- (I) L^2T^{-1} .
- (II) same as dimension of stream function.
- (III) $L^{-2}T^{1}$.
- (IV) same as dimension of stokes stream function.
 Then

[Question ID = 14003]

- 1. Only (III) and (IV) are true. [Option ID = 26012]
- 2. Only (I) and (II) are true. [Option ID = 26009]
- 3. Only (II) and (III) are true. [Option ID = 26011
- Only (I) and (IV) are true. [Option ID = 26010]

Correct Answer :-

Only (I) and (II) are true. [Option ID 26009]

45)

Consider a sequence $\{x_n\}$ defined by $0 < x_1 < 1$ and $x_{n+1} = 1 - \sqrt{1 - x_n}$, $n = 1, 2, \cdots$. Then $\frac{x_{n+1}}{x_n}$ converges to

[Question ID = 13967]

- 1. 0 [Option ID = 25866]
- 2. 1/3 [Option ID = 25867]
- 1/2 [Option ID = 25868]
- 4. 1 [Option ID = 25865]

Correct Answer :-

1 [Option ID = 25865]

46)

Which of the following statements about the outer measure m^* on $\mathbb R$ is true?

[Question ID = 13987]

FirstRanker.com

Firstranker's choice There exists an open subsetware firstRankeh.com

- Every subset of ℝ of zero outer measure is at most countable. [Option ID = 25947]
 If B ⊆ ℝ is unbounded, then m*B > 0.
- [Option ID = 25948]
- Every non empty closed subset E of \mathbb{R} has $m^*E > 0$. [Option ID = 25946]

Correct Answer :-

There exists an open subset $A \subseteq \mathbb{R}$ such that $m^*A = 0$.

47) Which of the following statements is true? [Question ID = 13977]

In a metric space, the image of a Cauchy sequence under a continuous map is a Cauchy sequence .

[Option ID = 25906]

- Every closed and bounded subset of a metric space is compact. [Option ID = 25907]
- Every infinite subset of the closed unit ball B in \mathbb{R}^n has a limit point in B.

 [Option ID = 25905]
- In a metric space, every closed ball of positive radius is connected. [Option ID = 25908]

Correct Answer :-

- Every infinite subset of the closed unit ball B in \mathbb{R}^n has a limit point in B.

 [Option ID = 25905]
- 48) Which one of the following statements is not true? [Question ID = 13966]
 - There is a function f defined on \mathbb{R} which is continuous on \mathbb{Q} (rational numbers) and discontinuous on \mathbb{Q}' (irrational numbers).

[Option ID = 25861]

- Monotone convergence property is equivalent to completeness of R. [Option ID = 25864]
- 3. Bolzano-Weiestrass theorem is equivalent to completeness of \mathbb{R} . [Option ID = 25863]
- Cantor's intersection property of \mathbb{R} is equivalent to completeness of \mathbb{R} [Option ID = 25862]

Correct Answer :-

There is a function f defined on \mathbb{R} which is continuous on \mathbb{Q} (rational numbers) and discontinuous on \mathbb{Q}' (irrational numbers).

[Option ID = 25861]

Present President of the Ramanujan Mathematical Society is [Question ID = 13916]

www.FirstRanker.com

3. S. Ponnusamy [Option ID = 25662] 4. R. Balakrishnan. [Option ID = 25663]

Correct Answer :-

Dinesh Singh [Option ID = 25661]

50) The characteristic and the minimal polynomial are same for the matrix

[Question ID = 13996]

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}_{[Option ID = 25983]}$$

$$\begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix}_{[Option ID = 25982]}$$

$$\begin{pmatrix} 0 & 0 \end{pmatrix}$$

[Option ID = 25981]

4. All of the above matrices [Option ID = 25984]

Correct Answer :-

www.FirstPanker.com

