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BE - SEMESTER- I & II (NEW) EXAMINATION - WINTER 2019

Subject Code: 3110014 Date: 17/01/2020

Subject Name: Mathematics – I

Time: 10:30 AM TO 01:30 PM **Total Marks: 70**

Instructions:

- 1. Attempt all questions.
- 2. Make suitable assumptions wherever necessary.
- 3. Figures to the right indicate full marks.

			MARKS
Q.1	(a)	Find the equations of the tenagent plane and normal line to the surface $x^2 + y^2 + z^2 = 3$ at the point $(1,1,1)$	03
	4		0.4

- 04 **(b)** Evaluate $\lim_{x\to 0} \frac{xe^x - log(1+x)}{x^2}$
- Using Gauss Elimination method solve the following system **07** (c) -x+3y+4z = 303x + 2y - z = 92x-y+2z = 10

Q.2 (a) Test the convergence of the series
$$\frac{1}{3} + \left(\frac{2}{5}\right)^2 + \left(\frac{3}{7}\right)^3 + \dots + \left(\frac{n}{2n+1}\right)^n + \dots$$

- Discuss the Maxima and Minima of the function $3x^2 y^2 + x^3$ **(b)** 04
- Find the fourier series of $f(x) = \frac{(\pi x)}{2}$ in the interval $(0,2\pi)$ OR

 Change the order of integration and evaluate $\int_0^1 \int_x^1 \sin y^2 \ dy \ dx$ **07 (c)**
- 07 (c)

Q.3 (a) Find the value of
$$\beta\left(\frac{7}{2}, \frac{5}{2}\right)$$
 03
(b) Obtain the fourier cosine series of the function $f(x) = e^x$ in the range $(0,l)$ 04

- Obtain the fourier cosine series of the function $f(x) = e^x$ in the range (0,l)04 **(b)**
- Find the maximum and minimum distance fom the point (1,2,2) to the (c) 07 sphere $x^2 + y^2 + z^2 = 36$

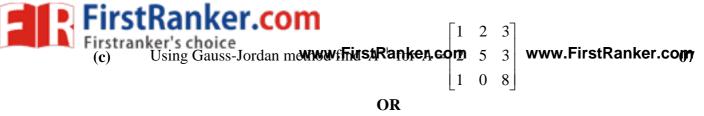
sphere
$$x^2 + y^2 + z^2 = 36$$

Q.3 (a) Test the convergence of the series
$$\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots$$
 03

- Evaluate $\iint (x^2 y^2) dx dy$ over the triangle with the vertices (0,1), **(b)** 04 (1,1), (1,2)
- Find the volume of the solid generated by rotating the plane region 07 **(c)** bounded by $y = \frac{1}{x}$, x=1 and x=3 about the X axis.

Q.4 (a) Evaluate
$$\int_0^{\pi} \int_0^{\sin \theta} r \, dr \, d\theta$$
 03

(b) Express
$$f(x) = 2x^3 + 3x^2 - 8x + 7$$
 in terms of (x-2)



Q.4 03 (a) Using Cayley-Hamilton Theorem find A^{-1} for $A = \begin{bmatrix} 1 & -1 \\ 2 & 3 \end{bmatrix}$

Evaluate $\int_0^\infty \frac{dx}{x^2+1}$ 04 **(b)**

Test the convergence of the series **07** (c) $\frac{x}{1:2} + \frac{x^2}{3:4} + \frac{x^3}{5:6} + \frac{x^4}{7:8} + \cdots$

Evaluate $\int_0^1 \int_1^2 xy \, dy \, dx$ **Q.5** (a) 03

Find the eigen values and eigenvectors of the matrix $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & -3 & 3 \end{bmatrix}$ If u = f (x-y, y-z, z-x) then show that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$ **(b)** 04

07 (c)

Find the directional derivatives of $f = xy^2 + yz^2$ at the point (2,-1,1), in **Q.5** (a) 03 the direction of i+2j+2k.

Test the convergence of the series $\sum_{n=1}^{\infty} \frac{\sqrt{n}}{n^2+1}$ Evaluate $\iiint xyz \ dx \ dy \ dz$ over the positive octant of the sphere x^2 + 04 **(b)**

(c) 07 $v^2 + z^2 = 4$

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