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## GUJARAT TECHNOLOGICAL UNIVERSITY <br> BE - SEMESTER- IV (New) EXAMINATION - WINTER 2019

Subject Code: 2142505
Date: 13/12/2019
Subject Name: Probability and Introduction to Statistics
Time:10:30 AM TO 01:00 PM
Total Marks: 70 Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
Q. 1 (a) Define/ explain following:
4. Random Experiment
5. Primary data
6. Ogives
(b) Calculate the mean for the following data

| Class | $0-7$ | $7-14$ | $14-21$ | $21-28$ | $28-35$ | $35-42$ | $42-49$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 19 | 25 | 36 | 72 | 51 | 43 | 28 |

(c) Find variance, standard deviation and coefficient of variation for the following data set.

| Gross profit (in \% of Sales | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of Companies | 22 | 38 | 46 | 35 | 20 |

## Q. 2 (a) Define/ explain following:

1. Random Variable
2. Cumulative Distribution Function
3. Compound Events
(b) Compare various measures of Central Tendencies.
(c) Discuss Joint Probability Distribution with suitable example. 07

## OR

(c) Discuss Normal Distribution with suitable example. 07
Q. 3 (a) State Baye's Theorem 03
(b) Discuss Type-I and Type -II error. 04
(c) When a machine is set correctly, it produces $25 \%$ defectives; otherwise it $\mathbf{0 7}$ produces $60 \%$ defectives. From the past knowledge and experience, the manufacturer knows that the chances that the machine is set correctly or wrongly are 50:50. The machine was set and before commencement of production, one piece was inspected and found to be defectives. What is the probability of machine set up being correct?

OR
Q. 3 (a) Briefly explain Binomial Distribution 03
(b) Explain probability sampling method
(c) What is Probability? Discuss Classical approach and Bayesian Approach for assigning probability.
Q. 4 (a) Give properties of Expectation ..... 03
(b) A machine produces 50 articles per day. On average 3 articles produced are ..... 04 found defective in a day. If a sample of 15 articles are drawn at random, what is the probability that one article of this lot is defective?
(c) Explain z-test with suitable example.Q. 4 (a) What is Simple Linear Regression?03
(b) Let X and Y be the random variables such that $\mathrm{E}[\mathrm{X}]=2.8, \mathrm{E}[\mathrm{Y}]=5.3, \mathrm{~V}[\mathrm{X}]$ ..... 04$=18.6, \mathrm{~V}[\mathrm{Y}]=41.3$. Compute the following:

1. $\mathrm{E}(\mathrm{X}+1)$
2. $\mathrm{E}(\mathrm{X}+2 \mathrm{Y}+1)$
3. $\mathrm{V}(2 \mathrm{X}+5)$
4. $\mathrm{V}(6 \mathrm{Y}+9)$
(c) For the probability distribution:

| X | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}(\mathrm{X})$ | 0.25 | 0.35 | 0.25 | 0.10 | 0.05 |07

Find $E[X]$ and $V[X]$
Q. 5 (a) Give properties of Binomial Distribution ..... 03
(b) Explain application of Chi-Square Test ..... 04
(c) Discuss F-test with suitable example. ..... 07
OR
Q. 5 (a) Explain Correlation Coefficient. ..... 03
(b) Discuss Simple Random Sampling. ..... 04
(c) Discuss ANOVA with suitable example. ..... 07

