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www.FirstRanker.com www.FirstRanker.com **O.2** (a) Which of the following are linear combination of u = (0, -2, 2) and v = (1, 3, -1)? Justify! (i) (2,2,2), (ii) (0, 4, 5)(b) Using Gram-Schmidt orthogonalization process find the corresponding orthonormal

(c) Using Gauss- Jordan elimination find the inverse of $\begin{pmatrix} -1 & 3 & -4 \\ 2 & 4 & 1 \\ -4 & 2 & 0 \end{pmatrix}$. 07

			/1	-1	3 \		
Q.3	(a)	Find the rank of the matrix and basis of the null space of	5	-4	-4		03
			7\	-6	2 /		
	(b)	Solve the system of linear equations using Gauss eliminat	the system of linear equations using Gauss elimination method:				04

x + y + 2z = 8, -x - 2y + 3z = 1, 3x - 7y + 4z = 10. (c) Show that the set of all real numbers of the form (x, 1) with operations 07 (x, 1) + (x', 1) = (x + x', 1) and k(x, 1) = (kx, 1) forms a vector space.

Q.4 (a) Determine whether the following are linear transformation or not?
(i) T:
$$P_2 \rightarrow P_2$$
, $T(p(x)) = p(x + 1)$, 03

(ii) T: P₂
$$\rightarrow$$
 P₂, T(a + bx + cx²) = (a + 1) + (b + 1)x + (c + 1) x².

$$\mathbf{A} = \begin{pmatrix} \mathbf{1} & \mathbf{2} & \mathbf{1} \\ \mathbf{1} & \mathbf{2} & \mathbf{1} \\ -\mathbf{1} & -\mathbf{1} & \mathbf{0} \end{pmatrix}$$

Q.5 (a) Find basis of kernel and range of T: $\mathbb{R}^2 \rightarrow \mathbb{R}^2$, defined by T(x, y) = (2x - y, -8x + 4y) 03

- (b) Which of the following are basis of $\mathbb{R}^{3?}$ Justify! 04 (i) { (1, 0, 0), (2, 2, 0), (3, 3, 3) }, (ii) { (3, 1, -4), (2, 5, 6), (1, 4, 8) }
- (c) Let T: $P_2 \rightarrow P_2$, defined by T(p(x)) = p(3x 5)(i) Find the matrix of T with respect to the basis $\{1, x, x^2\}$.
 - (ii) Use the indirect procedure using matrix to compute $T(1 + 2x + 3x^2)$.
 - (iii) Check the result in (b) by computing $T(1 + 2x + 3x^2)$ directly.

Show that $\overline{F} = \frac{(yi - xj)}{x^2 + y^2}$ is irrotational. (a) **Q.6** 03

- (b) Find the directional derivative of $f(x, y, z) = x^2z + y^3z^2 xyz$ at (1,1,1) in the direction 04 of the vector (-1,0,3).
- 07 (c) Using Green's theorem evaluate \oint_C (3x² - 8y²) dx + (4y - 6xy) dy, where C is the boundary of the region bounded by $y^2 = x$ and $y = x^2$.
- **Q.7** (a) Find the work done by $\overline{F} = (y x^2) i + (z y^2) j + (x z^2) k$ over the curve 03 $\mathbf{r}(t) = t \mathbf{i} + t^2 \mathbf{j} + t^3 \mathbf{k}; \mathbf{0} \le t \le \mathbf{1}$, from (0,0,0) to (1,1,1).
 - (b) Use Cramer's rule to solve: x + 2z = 6, -x + 4y + 6z = 30, -x 2y + 3z = 8. 04
 - (c) Verify divergence theorem for $\overline{F} = x i + yj + zk$ over the sphere $x^2 + y^2 + z^2 = a^2$. 07

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(b) Which of the following sets of vectors of \mathbb{R}^3 are linearly independent? Justify. 04 (i) { (4, -1, 2), (-4, 10, 2) } (ii) { (-3, 0, 4), (5, -1, 2), (1, 1, 3) } (c) Find the eigenvalues and bases for the eigenspaces for A^{11} , 07 *(*−1 −2 −2)

set to {
$$(1, 1, 1), (0, 1, 1), (0, 0, 1)$$
 }.
 $(-1 \ 3 \ -4$

03

04

07

