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## GUJARAT TECHNOLOGICAL UNIVERSITY

**BE - SEMESTER- III(OLD) EXAMINATION - SUMMER 2019** Subject Code: 130002 Date: 30/05/2019 **Subject Name: Advanced Engineering Mathematics** Time: 02:30 PM TO 05:30 PM **Total Marks: 70 Instructions:** 1. Attempt all questions. 2. Make suitable assumptions wherever necessary. 3. Figures to the right indicate full marks. (a) (i) Solve  $3e^x \tan y \, dx + (1 - e^x) \sec^2 y \, dy = 0$ 0.1 03 (ii) Solve y'-  $(1 + 3x^{-1})y = x+2$ ;  $y(1) = e^{-1}$ 04 (b) Find the Power series solution of the differential equation y'' = y'. 07 (a) Using the method of separation of variables solve  $u_{xx} = 16 u_{y}$ . Q.2 07 (b) Find the series solution of the differential equation by Frobenius method 07  $x\frac{d^2y}{dx^2} + \frac{dy}{dx} - y = 0$ (b) (i) Solve  $y'' + 4y = 8 \cos 2x$ , y(0) = 0, y'(0) = 2(ii) Solve  $y'' - 4y' - 12y = 7 e^{-7x}$  by method of undetermined coefficients. 03 04 (a) Find the Fourier series for the function  $f(x) = x^2 + x$ ,  $-\pi \le x \le \pi$ . 07 Q.3 (b) Find the Fourier series of the function 07  $f(x) = \begin{cases} -\pi, & 0 < x < \pi \\ x - \pi, & \pi < x < 2\pi \end{cases}$ OR (a) Find the Fourier series with period 3 to represent  $f(x) = 2x - x^2$  in the range 07 **Q.3** (0, 3).(b) Find the half range Fourier cosine series of the function f(x) = c - x in interval 07 (0, c) with period 2c. (a) (i) Find the Laplace transform of  $e^{-t} (4t^3 + 3\cos 2t + 2e^{-2t})$ **Q.4** 03 (ii) Prove that 04  $L(sinat) = \frac{a}{s^2 + a^2}$  and  $L(cosat) = \frac{s}{s^2 + a^2}$ s > 0, where *a* is a constant. Find the Inverse Laplace transform of (1)  $\frac{s+3}{(s^2+1)(s^2+9)}$  (2) **(b)** 07 (2)  $\frac{2s+3}{s^2-2s+5}$ OR Q.4 (a) (i) Find the Laplace transform of 03  $e^{-2t} \int_0^t t \cos t \, dt$ (ii) Find the Inverse Laplace transform of  $\frac{1+e^{-\frac{\pi}{2}s}}{s^2+4}$ 04

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Q.5 (a) (i) Form Partial differential equation by eliminating the arbitrary function from 03 the equation

$$z = y^2 + 2f\left(\frac{1}{x} + \log y\right)$$

(ii) Define the following: (1) Beta function (2) Dirac's Delta Function 04

(b) Express the function as a Fourier Integral  $f(x) = \begin{cases} 1, \\ 0, \end{cases}$  $|x| \leq 1$ 

OR

- (a) (i) Solve: p + q = pq(ii) Solve:  $x (y^2 z^2) p + y (z^2 x^2) q = z(x^2 y^2)$ . Q.5 03 04 07
  - Solve the following: **(b)** 
    - (i)  $\frac{\partial^3 z}{\partial x^3} 4 \frac{\partial^3 z}{\partial x^2 \partial y} + 4 \frac{\partial^3 z}{\partial x \partial y^2} = 2\sin(3x + 2y)$ (ii)  $(D - D' - 1) (D - D' - 2) z = e^{2x - y}$

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