

Seat No.: _ Enrolment No._

GUJARAT TECHNOLOGICAL UNIVERSITY

BE - SEMESTER-IV(NEW) - EXAMINATION - SUMMER 2019

Subject Code:2141005 Date:28/05/2019

Subject Name: Signals and Systems

Time:02:30 PM TO 05:00 PM **Total Marks: 70**

Instructions:

- 1. Attempt all questions.
- 2. Make suitable assumptions wherever necessary.
- 3. Figures to the right indicate full marks.
- Find whether given signal is periodic or not? If yes, give its fundamental 03 Q.1 period.

(i)
$$x(t) = 3\cos(10\pi t) + 5\sin(6\pi t)$$

(ii) $x[n] = e^{j10n}$

(b) Decompose following signals into their even and odd parts.

04

(i)
$$x(t) = 3t^2 + 2t + 1$$

(ii)
$$x[n] = \{1, 1, 1\}$$

- 07 (c) Explain following property for the system y(t) = x(t) + 2. (i) Linearity (ii) Time-invariance (iii) Causality (iv) Dynamicity
 - (v) Stability.
- (a) Let x[n] be a signal with x[n] = 0 for n < -2 and n > 4. For each of the 03 Q.2 following signal, determine the values of n for which it is guaranteed to be zero.

(i)
$$x[n-3]$$

(ii)
$$x[-n-2]$$

04 Prove associativity property of convolution sum. 07

(c) For, $x[n] = \delta[n] + 2\delta[n-1] - \delta[n-3]$ and

$$x[n] = \delta[n] + 2\delta[n-1] - \delta[n]$$

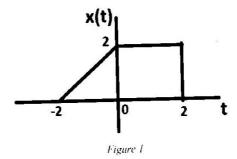
 $h[n] = 2\delta[n+1] + 2\delta[n-1],$

Compute (i)
$$y_1[n] = x[n] * h[n]$$
 and (ii) $y_2[n] = x[n] * h[n+2]$.

(c) Sketch each of the following signals for a signal shown in Figure 1. 07

- (i) x(2-t)
- (ii) x(2t+1)

(iii)[
$$x(t) + x(-t)$$
] $u(t)$ [2+2+3 Marks]



where $x[n] = \{1,2,3\}$ and 03 x[n]*h[n],convolution the Q.3 Find $h[n] = \{1,0,1\}.$



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- (b) Given that y[n] = x[n] * h[n], $x[n] = \{1,0,1\}$, y[n] = 0 for n < -1 and y[n] = 2 for n = -1,0,3. Find h[n]. Given y[n] is of finite duration signal with length of 5.
- Consider periodic signal x(t) with fundamental frequency $\omega_0 = \pi$, determine 07 its complex exponential Fourier series representation. Where,

$$x(t) = \begin{cases} 1.5, & 0 \le t < 1 \\ -1.5, & 1 \le t < 2 \end{cases}$$

- 03 Find the convolution x(t) * h(t), where $x(t) = h(t) = e^{-at}u(t)$. Q.3 (a)
 - Given that x[n] has Fourier transform $X(e^{j\omega})$, express the Fourier transform of **(b)** the $w[n] = (n-1)^2 x[n]$ in terms of $X(e^{j\omega})$. [hint: Use Fourier transform property.]
 - Let x(t) be a periodic signal with fundamental frequency ω_1 and Fourier 07 (c) coefficients a_k . Given that y(t) = x(1-t) + x(t-1), how is the fundamental frequency ω_2 of y(t) related to ω_1 ? Also, find a relationship between the Fourier series coefficients b_k of y(t) and the coefficients a_k .
- 03 State and prove Time scaling property of Fourier transform. **Q.4** (a)
 - Given the relationships y(t) = x(t) * h(t) and g(t) = x(3t) * h(3t). Also given that x(t) and h(t) have Fourier transform $X(j\omega)$ and $H(j\omega)$ respectively. Using Fourier transform property show that g(t) = Ay(Bt) and determine the values of A and B.
 - Find the response of an LTI system with impulse response $h(t) = e^{-at}u(t)$, a > 0 to the input signal $x(t) = e^{-bt}u(t)$, b > 0, $a \neq b$, using Fourier transform.

OR

- 03 State and prove Duality property of Fourier transform. 0.4
 - A stable LTI system characterized by the differential equation 04

Find the impulse response of the system.
$$\frac{dy(t)}{dt} + ay(t) = x(t), \qquad a > 0.$$

- Find the Fourier transform of $x(t) = e^{-|t|}$. Using property find Fourier (c) transform of $\frac{2}{1+t^2}$
- Find the inverse z-transform of $X(z) = z^{-2} + 1 + z^3$, $0 < z < \infty$. 03 Q.5 (a)
 - Discuss causality and stability of LTI system using z-transforms. 04 **(b)**
 - Using partial fraction expansion find the inverse z-transform of 07 (c)

$$X(z) = \frac{1 - \frac{1}{3}z^{-1}}{(1 - z^{-1})(1 + 2z^{-1})}, \qquad |z| > 2$$

- 03 Find DTFT of $x[n] = \{1,0,4,2\}.$ (a) 04
- State and prove differentiation property of z-transform.
- Consider the following algebraic expression for the z-transform X(z) of 07 signal x[n]:

$$X(z) = \frac{1+z^{-1}}{1+\frac{1}{3}z^{-1}}$$

0.5

- (i) Assuming the ROC to be |z| > 1/3, use long division to determine the values of x[0], x[1], and x[2].
- (ii) Assuming the ROC to be |z| < 1/3, use long division to determine the values of x[0], x[-1], and x[-2].
