## FACULTY OF ENGINEERING \& INFORMATICS

B.E. I Year (Common to all Branches) (Suppl.) Examination, December 2013

Subject: Mathematics - I
Time: 3 Hours
Max.Marks: 75

## Note: Answer all questions from Part A. Answer any five questions from Part B.

## PART _ A (25 Marks)

1. Find the Taylor's series expansion of $f(x)=2^{x}$ about $x=0$.
2. Find the radius of curvature of the curve $r=a \operatorname{sine}+b \cos @ a t e . z r / 2$
3. Show that $\lim _{(X, Y) \cdot(),(0)} \frac{x^{2}-}{X^{2} y}$ does not exist.
4. If $z=y+f(u), u=-\frac{x}{-}$, show that $u \frac{a z}{a x}+\frac{a z}{a y}=1$.

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5. Evaluate $e_{02 y} \mathrm{ex}^{2} d x d y$ by changing the order of integration.
6. Find a vector that gives the direction of maximum rate of increase for $f(x, y, z)=6 x y z$ at $(-1,2,1)$.
7. Find the values of $A$ and $p$ such that the system of equations $x+y+z=6$, $x+2 y+3 z=10, x+2 y+A z \neq 0$ has an infinite number of solutions.
B. Show that the vectors $(2,2,0),(3,0,2),(2,-2,2)$ are linearly independent.
9. Discuss the convergence of the series $Z\left(1+\frac{1}{n}\right) n p>0$.
10. Test whether the series
(-1)n nVn converges absolutely or not.

PART - B (50 Marks)
11.(a) State and prove Rolle's theorem.
(b) Find the envelope of the family of curves $x \tan a+y \sec a=5$, $a$ is a parameter.
12.(a) Trace the curve $y=x^{3}-12 x 16$.
(b) Examine $f(x, y)=x^{4}+2 x^{2} y-x^{2}+3 y^{2}$ for maximum and minimum values.
13.(a) Show that $V=12 x i 15 y^{2} j+k$ is irrotational and find a scalar function $f(x, y, z)$ such that $V=\operatorname{grad} \mathrm{f}$.
(b) Use the divergence theorem to evaluate $\int J_{F, n}$ ds, where $F 4-2 y^{2} j+z^{2} k$ and $S$ is the surface bounding the region $x^{2}+y^{2}=4, z=0$ and $z=3$. find the eigen values of
(b) Find the canonical form, nature, index and signature of the quadratic form
$Q=8 x_{i}^{2}+7 x^{2},+3 x_{3}^{2}-12 \times 1 \times 2-8 \times 2 \times 3+4 \times 3 x i$.
15. Test the convergence of the series
a) $\frac{1}{1.3 .5}+2+\frac{3}{3.5 .7}+$
b) $\frac{\left(r^{11}\right)^{2} x^{2 n}}{(2 n) i}$
16.(a) Find the evolute of the curve $y^{2}=4 a x$.
$x 2 y(x-y)$
(b) For the function $\left.f(x, y) \neq \frac{x 2 y(x-y)}{x^{2}+y^{2}} \cdot<x y\right) \#(0,0)$

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0 \quad(x, y)=(0,0)
$$

show that $\frac{a^{2}{ }^{2}}{a x \text { ay } a^{5^{2} \mathrm{~F}} \mathrm{ax}}$ at (0,0).
17.(a) Show that $V x(V \times V)=V(V . V)-V^{2} V$
$\left(23+\mathbf{3} 4^{1}\right.$
(b) Find the rank of the matrix $A=\begin{array}{llll}3 & 2 & -1 & 1 \\ 4 & -1 & 3 & -2\end{array}-2$

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