

Q.1 Attempt the following Questions

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1. The polar form the complex number $z=1$ is

- a) $(\cos 0 + i \sin 0)$ b) $(\cos \pi + i \sin \pi)$
c) $\sqrt{2}(\cos 0 + i \sin 0)$ d) $(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2})$

CO1

(Level:CO)

Marks

1*6=6

2. The complex number $z = -1 + 3i$ lies in --

- a) First quadrant b) Second quadrant
c) Third quadrant d) Fourth quadrant

CO1

3. The circular function $\sin x$ is equal to --

- a) $\frac{e^{ix} + e^{-ix}}{2i}$ b) $\frac{e^{ix} - e^{-ix}}{2i}$ c) $\frac{e^{ix} + e^{-ix}}{2}$ d) $\frac{e^{ix} - e^{-ix}}{2}$

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4. The necessary condition for the differential equation $M(x,y) dx + N(x,y) dy = 0$ to be exact is

- a) $\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$ b) $\frac{\partial M}{\partial y} = \frac{\partial M}{\partial x}$ c) $\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$ d) $\frac{\partial M}{\partial x} = \frac{\partial N}{\partial y}$

CO2

5. The differential equation of an electric circuit containing an inductance L , r Voltage E , the current i is given by _____

CO2

- a) $L \frac{di}{dt} + Ri = E$ b) $L \frac{di}{dt} - Ri = E$
c) $L \frac{di}{dt} + Ri = -E$ d) $\frac{di}{dt} + \frac{R}{L} i = E$
6. The differential equation of family of curves $xy = k^2$ is -----
a) $x \frac{dy}{dx} + y = 0$ b) $y \frac{dx}{dy} + x = 0$ c) $-x \frac{dy}{dx} + y = 0$ d) $-y \frac{dx}{dy} + x = 0$

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Q.2 Attempt any TWO of the following:

(A) Prove that $(x + iy)^{\frac{m}{n}} + (x - iy)^{\frac{m}{n}} = 2\sqrt{x^2 + y^2}^{\frac{m}{n}} \cos\left(\frac{m}{n} \tan^{-1} \frac{y}{x}\right)$

(B) Solve $\frac{dy}{dx} = -\frac{(y \cos x + \sin y + y)}{(\sin x + x \cos y + x)}$

(C) Prove that $\cos \left[i \log \frac{a-ib}{a+ib} \right] = \frac{a^2-b^2}{a^2+b^2}$

Q.3 Attempt the following

(A) If z_1 and z_2 are two complex numbers such that $|z_1 + z_2| = |z_1 - z_2|$. Prove the difference of their amplitudes is $\frac{\pi}{2}$.

Moderate
/CO1

(B) A resistance of 100 ohms and inductance of 0.1 henries are connected in series with a battery of 20 volts. Find the current in the circuit at any time t , if the relation between

Difficult
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L, R and E is $L \frac{di}{dt} + Ri = E$

OR

Q.3 Attempt the following

(A) Solve $x^{10} + 11x^5 + 10 = 0$

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(B) Solve $\frac{dy}{dx} - y \tan x = y^4 \sec x$

*** End ***

Moderate
/CO2