

DR. BABASAHEB AMBEDKAR TECHNOLOGICAL UNIVERSITY, LONERE

Mid Semester Examination -Oct. 2019

Course: S.Y. B. Tech. ALI

Sem: III

Subject Name: Engineering Mathematics-III

Subject Code: BTMS301

Max. Marks: 20

Date: 03.10.2019

Duration: 1Hr.

Instructions: 1. All questions are compulsory.

2. Use of nonprogrammable calculator is allowed.

3. Figures to right indicate full marks.

Q1. Attempt the following.

(6Marks)

a) Find Laplace transform of $e^{-3t}t^4$

co1

i) $\frac{4}{(s+3)^5}$ ii) $\frac{5}{(s+3)^5}$ iii) $\frac{4!}{(s+3)^5}$ iv) $\frac{4!}{(s+3)^4}$

b) The Laplace transform of $\sin 2t \delta(t-2)$ is

co1

i) $e^{-2s} \sin 2$ ii) $e^{-2s} \sin 4$ iii) $e^{-4s} \sin 4$ iv) $e^{-2s} \sin 4s$

c) Find Inverse Laplace Transform of $\left[\frac{s^2-3s+4}{s^3} \right]$

co2

i) $t-3t+2t^2$ ii) $1-3t+4t^2$ iii) $1-6t+2t^2$ iv) $1-3t+2t^2$

d) $L^{-1} \left[\frac{1}{s} F(s) \right] =$

co2

i) $t \int_0^t f(t) dt$ ii) $e^{-t} \int_0^t f(t) dt$ iii) $\int_0^t f(t) dt$ iv) $\int_0^t f(t) dt$

e) If $F(s)$ is Fourier transform of $f(x)$ then Fourier transform of $f(ax)$ is

co3

i) $\frac{1}{a} F\left(\frac{s}{a}\right)$ ii) $F\left(\frac{s}{a}\right)$ iii) $\frac{1}{a} F(a)$ iv) $\frac{1}{a} F\left(\frac{s}{a}\right)$

co3

f) Fourier cosine transform of $f(t) = e^{-2t}$ is

i) $\sqrt{\frac{2}{\pi}} \frac{2s}{s^2+4}$ ii) $\sqrt{\frac{2}{\pi}} \frac{s}{s^2+4}$ iii) $\sqrt{\frac{2}{\pi}} \frac{1}{s^2+4}$ iv) $\sqrt{\frac{2}{\pi}} \frac{2}{s^2+4}$

Q2. Attempt any Two of the following.

(6Marks)

(A) Find $L\{e^{3t} \int_0^t t \sin t dt\}$

co1

(B) Find Inverse Laplace Transform of $\log \left(\frac{s^2+16}{s^2+9} \right)$

co2

(C) Find Fourier cosine transform of e^{-3x}

co3

Q3. Attempt any ONE.

(6Marks)

(A) Solve $\frac{dy}{dx} + x = \cos t$, $\frac{dx}{dt} + y = \sin t$ such that $y(0) = 2, x(0) = 0$ by Laplace transform

co2

(B) Find $f(x)$ if $F_s(\lambda) = \frac{e^{-a\lambda}}{\lambda}$

co3