

[illegible]

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- i) Verify whether the linear combination of e^x and e^{-2x} is a solution of the differential equation

$$y'' + y' - 2y = 0$$

- j) Find the Wronskian of the functions x , x^2 and x^3 .

SECTION-B

2. Solve the following integral

$$\int_0^{\ln 2} \int_0^{\sqrt{(\ln 2)^2 - y^2}} e^{\sqrt{x^2 + y^2}} dx dy$$

by converting it into an equivalent polar integral.

3. For what values of x does the following power series converge ?

$$\sum_{n=1}^{\infty} (-1)^{n-1} \frac{x^n}{n}$$

4. Solve the differential equation $(3x^2y^3e^y + y^3 + y^2) dx + (x^3y^3e^y - xy) dy = 0$.
5. Solve the differential equation $y'' + 4y' + 4y = e^{-2x} \sin x$ by using method of variation of parameters.
6. Check the convergence of the following series

(i) $\sum_{n=1}^{\infty} \frac{(2n)!}{n!n!}$

(ii) $\sum_{n=2}^{\infty} \frac{1}{\sqrt{n \ln n}}$

SECTION-C

7. a) Find the maximum and minimum values of the function $f(x, y) = 3x + 4y$ on the circle $x^2 + y^2 = 1$.
- b) Find the volume in the first octant bounded by the coordinate planes and the surface $z = 4 - x^2 - y$.
8. State and prove Leibniz's test for alternating series.
9. Find the general solution of the equation $x^3y''' - 3xy' + 3y = 16x + 9x^2 \ln x$.

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