

Roll No. Total No. of Pages : 02

Total No. of Questions: 09

B.Tech.(IT) (2018 Batch) (Sem.-3) MATHEMATICS-III

Subject Code : BTAM-301-18 M.Code : 76393

Time: 3 Hrs. Max. Marks: 60

INSTRUCTIONS TO CANDIDATES:

- SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
- 3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

SECTION-A

1. Write briefly:

- a) Show that the function $f(x, y) = \frac{2x^2y}{x^4 + y^2}$ has no limit as (x, y) approaches (0, 0).
- b) Find the local extreme values of the function $f(x, y) = x^3 y^3 2xy + 6$.
- c) Sketch the region of integration for the integral

$$\int_0^{\sin x} \int_0^{\pi} y \, dy dx$$

and write an integral with the order of integration reversed.

- d) Define convergence of a series and give an example of a convergent series.
- e) Explain the limit comparison test.
- f) By inspection obtain the integrating factor and solve the differential equation :

$$xdx = vdv + 2(x^2 + v^2) dx = 0$$

g) Check whether the following differential equation exact.

$$(2x + e^{y}) dx + xe^{y} dy = 0$$

h) Find the general solution of the differential equation y'' + 2y' + y = 0

i) Verify whether the linear combination of e^x and e^{-2x} is a solution of the differential equation

$$y^{\prime\prime} + y^{\prime} - 2y = 0$$

j) Find the Wronskian of the functions x, x^2 and x^3 .

SECTION-B

2. Solve the following integral

$$\int_{0}^{\ln 2} \int_{0}^{\sqrt{(\ln 2)^{2}-y^{2}}} e^{\sqrt{x^{2}+y^{2}}} dxdy$$

by converting it into an equivalent polar integral.

3. For what values of x does the following power series converge?

$$\sum_{n=1}^{\infty} (-1)^{n-1} \frac{x^n}{n}$$

- 4. Solve the differential equation $(3x^2y^3e^y + y^3 + y^2) dx + (x^3y^3e^y xy) dy = 0$.
- 5. Solve the differential equation $y'' + 4y' + 4y = e^{-2x} \sin x$ by using method of variation of parameters.
- 6. Check the convergence of the following series
 - $(i) \sum_{n=1}^{\infty} \frac{(2n)!}{n!n!}$
- (ii) $\sum_{n=2}^{\infty} \frac{1}{\sqrt{n} \ln n}$

SECTION-C

- 7. a) Find the maximum and minimum values of the function f(x, y) = 3x + 4y on the circle $x^2 + y^2 = 1$.
 - b) Find the volume in the first octant bounded by the coordinate planes and the surface $z = 4 x^2 y$.
- 8. State and prove Leibniz's test for alternating series.
- 9. Find the general solution of the equation $x^3y''' 3xy' + 3y = 16x + 9x^2 \ln x$.

NOTE: Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.

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