Roll No. $\square$ Total No. of Pages: 02
Total No. of Questions: 18
B.Tech. (CSE/IT) (2012 to 2017) (Sem.4)

DISCRETE STRUCTURES
Subject Code : BTCS-402
M.Code: 71106

Time : 3 Hrs.
Max. Marks : 60

## INSTRUCTIONS TO CANDIDATES :

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

## SECTION-A

Answer briefly :

1) Define Poset.
2) Define Anti-symmetric relation.
3) Write General Inclusion-Exclusion principle.
4) State Involution Law in Boolean algebra.
5) Find the number of distinct permutations that can be formed from all the letters of word 'PROGRAMMMING'.
6) Give an example of graph that has Euler's circuit but Hamiltonian circuit.
7) Define Cyclic Subgroup.
8) Write generating function of $S(n)=2.7^{n}, n \geq 0$.
9) Define Directed Graph.
10) What is the difference between a graph and a tree?

## SECTION-B

11) If $R$ is equivalence relation on a set $A$, then show that $R^{-1}$ is also equivalence relation on $A$.
12) Reduce the following Boolean expressions to complete sum of products form:
a. $f(x, y, z)=x\left(y^{\prime} z\right)^{\prime}$
b. $f(x, y, z)=z\left(x^{\prime}+y\right)+y^{\prime}$
13) Show that in group $G,(x y)^{-1}=y^{-1} x^{-1} \forall x, y \in G$.
14) Prove that in any graph :
a. There are even number of vertices of odd degree.
b. Sum of degree of all the vertices is even.
15) Define and give example of:
a. Isomorphism
b. Integral domain.

## SECTION-C

16) Solve the recurrence relation by using generating function :
$S(n-2)=S(n-1)+S(n)$, where $S(0)=1, \mathrm{~S}(1)=1$.
17) State and prove Euler's theorem in graph theory.
18) If $\{B,+, \cdot$,$\} is Boolean Algebra, then :$
a. If $x+y=x+z$ and $x^{\prime}+y=x^{\prime}+z$ then $y=\mathrm{z}$.
b. If $x . y=x . z$ and $x^{\prime} . y=x^{\prime} . z$ then $y=z$.
