

Linear Algebra**Unit-1**

1. Definition of:

- a. Vector Space
- b. Subspace
- c. Linear Span
- d. Linear Combination
- e. Linear Integral
- f. Linear Dependence
- g. Null Space
- h. Column Space
- i. Linear Transformation

2. Theorems on necessary and sufficient condition of subspace and problems.

3. Algebra of subspace

4. If S is subset of vector space $V(F)$ then P.T.

- i. S is Subspace of $V \Rightarrow L(S) = S$
- ii. $L(L(S)) = L(S)$

5. If S, T are subset of Vector space $V(F)$ then

- i. $S \subset T \Rightarrow L(S) \subset L(T)$
- ii. $L(S \cup T) = L(S) + L(T)$

6. Basis Extension theorem and problems.

7. Problems on Linear Transformation.

8. Let u, v be two vVector Space and $T: u \rightarrow v$ is $L > T$ then range set $R(T)$ and Null space $N(T)$ is a Subspace of $U(F)$

9. Rank Nullity theorem and dimensions theorems.

10. Practical problems.

- 1.All theorems in Rank
- 2.Problems in Change of basis,Eigen value and Eigen vector and Characteristic equation.

Unit-3

- 1.Theorems and problems in Diagonalization.
2. An $n \times n$ matrix with n -distinct eigen values is diagonalizable.
- 3.Problems in Complex Eigen value and application of Differential equation problems.
- 4.Definition of:
 - a.Orthogonal vector
 - b.Orthonormal vector
 - c.Inner product space
 - d.Length of a vector
 - e.Unit vector
- 5.Problems in Inner product space and Orthogonality.
- 6.All Inequality theorems.
- 7.Practical problems.
- 8.If $S = \{u_1, \dots, u_p\}$ is an orthogonal set of non-zero vectors in R^n then S is linear independent and hence, is a basis for the subspace spanned by S .