

Roll No. Total No. of Pages: 02

Total No. of Questions: 18

B.Tech.(CE) (2018 Batch) (Sem.-3)

MATHEMATICS-III (TRANSFORM & DISCRETE MATHEMATICS)

Subject Code : BTAM-301-18 M.Code : 76373

Time: 3 Hrs. Max. Marks: 60

INSTRUCTIONS TO CANDIDATES:

- 1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
- 3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

SECTION-A

Write briefly:

- 1. Define gradient of a scalar point function.
- 2. If F = (x + y + 1) i + j (x + y) k. Show that F. eurl F = 0
- 3. Define Laplace transform.
- 4. Write the relation between Laplace and Fourier transform.
- 5. Represent $f(t) = \sin 2t$, $2\pi < t < 4\pi$ and 0 otherwise, in terms of unit step function.
- 6. Define Solenoidal and irrotational fields.
- 7. State convolution theorem of Fourier transform.
- 8. State Stokes theorem.
- 9. Write Euler's formula of Fourier series.
- 10. Write Gibbs phenomenon.

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SECTION-B

- 11. Find the values of a and b such that the surfaces $ax^2 byz = (a + 2)x$ and $4x^2y + z^3 = 4$ cut orthogonally at (1, -1, 2).
- 12. Apply Convolution theorem to evaluate the inverse Laplace transform of:

$$\frac{s^2}{(s^2+a^2)(s^2+b^2)}$$

13. Find the Fourier sine transform of $e^{-|x|}$. Hence show that

$$\int_0^\infty \frac{x \sin mx}{1 + x^2} dx = \frac{\pi e^{-m}}{2}, \ m > 0$$

- Apply Green's theorem to evaluate $\int_C [(2x^2 y^2)dx + (x^2 + y^2)dy]$, where C is the boundary of the area enclosed by the x-axis and the upper-half of the circle $x^2 + y^2 = a^2$.
- 15. If A and B are irrotational, prove that $A \times B$ is solenoidal.

SECTION-C

- 16. Verify Gauss divergence theorem for $F = (x^2 yz)i + (y^2 zx)j + (z^2 xy)k$ taken over the parallelepiped $0 \le x \le a$, $0 \le y \le b$, $0 \le x \le c$.
- Find the Fourier cosine series of the function $f(x) = \pi x$ in $0 < x < \pi$. Hence show that $\sum_{r=0}^{\infty} \frac{1}{(2r+1)^2} = \frac{\pi^2}{8}$

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18. a) Use Laplace transform method to solve:

$$\frac{d^2x}{dt^2} - \frac{2dx}{dt} + x = e^t$$

With
$$x = 2$$
, $\frac{dx}{dt} = -1$ at $t = 0$.

b) Find the directional derivative of $f = x^2 - y^2 + 2z^2$ at the point P (1, 2, 3) in the direction of the line PQ where Q is the point (5, 0, 4). Also calculate the magnitude of the maximum directional derivatives.

NOTE: Disclosure of Identity by writing Mobile No. or Making of passing request on any page of Answer Sheet will lead to UMC against the Student.

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