## Topic:- ECO MA S2

1) Consider independently and identically distributed random variables $X_{1}, \ldots, X_{n}$ with values in [ 0,2 ]. Each of these random variables is uniformly distributed on $[0,2]$. If $Y=\max \left\{X_{1}, \ldots, X_{n}\right\}$, then the mean of $Y$ is
[Question ID = 5844]
1. $[n /(n+1)]^{2}[$ Option ID $=23370]$
2. $n / 2(n+1)[$ Option ID $=23371]$
3. $2 n /(n+1)[O p t i o n ~ I D=23372]$
4. $n /(n+1)[$ Option ID $=23373]$

## Correct Answer :-

- $2 \mathrm{n} /(\mathrm{n}+1)$ [Option ID $=23372$ ]

2) A coin toss has possible outcomes $H$ and $T$ with probabilities $3 / 4$ and $1 / 4$ respectively. A gambler observes a sequence of tosses of this coin until H occurs. Let the first H occur on the $\mathrm{n}^{\text {th }}$ toss. If n is odd, then the gambler's prize is $-2^{\mathrm{n}}$, and if n is even, then the gambler's prize is $2^{\mathrm{n}}$. What is the expected value of the gambler's prize?
[Question ID = 5845]
1. 1 [Option ID $=23374$ ]
2. -1 [Option ID $=23375$ ]
3. 3 [Option ID $=23376$ ]
4. -3 [Option ID = 23377]

Correct Answer :-

-     - 1 [Option ID = 23375]

3) Suppose two fair dice are tossed simultaneously. What is the probability that the total number of spots on the upper faces of the two dice is not divisible by 2,3 , or 5 ?
[Question ID = 5846]
1. $1 / 3$ [Option ID $=23378$ ]
2. $2 / 9$ [Option ID $=23379$ ]
3. $4 / 9$ [Option ID $=23380$ ]
4. $7 / 16$ [Option ID $=23381$ ]

Correct Answer :-

- $2 / 9$ [Option ID = 23379]

4) A student is answering a multiple-choice examination. Suppose a question has m possible answers. The student knows the correct answer with probability p. If the student knows the correct answer, then she picks that answer; otherwise, she picks randomly from the choices with probability $1 / m$ each. Given that the student picked the correct answer, the probability that she knew the correct answer is
[Question ID = 5847]
1. $m p /[1+(m-1) p][$ Option ID $=23382]$
2. $\mathrm{mp} /[1+(1-\mathrm{p}) \mathrm{m}][$ Option $\mathrm{ID}=23383]$
3. $(1-p) /[1+(m-1) p][$ Option $I D=23384]$
4. $(1-p) /[1+(1-p) m][O p t i o n ~ I D=23385]$

Correct Answer :-

- mp/[1 + $(\mathrm{m}-1) \mathrm{p}]$ [Option ID $=23382$ ]

5) Suppose $Y$ is a random variable with uniform distribution on [0,2]. The value of the cumulative distribution function of the random variable $X=e^{Y}$ at $x \in\left[1, e^{2}\right]$ is
[Question ID = 5848]
1. $2^{-1} \ln \times[$ Option $I D=23386]$
2. $4^{-1} \ln x-2^{-1}$ [Option ID $=23387$ ]
3. $\ln \times[$ Option ID $=23388$ ]
4. $\ln x-1$ [Option ID $=23389$ ]

Correct Answer :-

- $2^{-1} \ln x[$ Option ID $=23386]$

6) Consider an economy where the final commodity is produced by a single firm using labour only. The price-setting firm charges a $25 \%$ mark-up over its per unit nominal wage cost. The workers demand a real wage rate $W / P=(1-u)$, where $u$ is the unemployment rate, P is the price, and W is the nominal wage rate. The natural rate of unemployment in this
7) The aggregate production function of an economy is $Y_{t}=\left(K_{t} L_{t}\right)^{1 / 2}$. Capital grows according to $K_{t+1}=(1-\delta) K_{t}+S_{t}$, where $S_{t}=s Y_{t}, L_{t}=\bar{L}$, $s$ is the saving rate, $\delta$ is the depreciation rate and ${ }_{\mathrm{L}}$ is the total population. Then, the steady-state level of consumption per capita is
[Question ID = 5850]
1. $s / \delta$
[Option ID = 23394]
2. $s^{2} / \delta^{2}$
[Option ID = 23395]
3. $\delta^{1 / 5}$
[Option ID = 23396]
4. $s(1-s) / \delta$
[Option ID = 23397]
Correct Answer :-

- $s(1-s) / \delta$
[Option ID = 23397]

8) Consider a production technology $Y=A L$, where $Y$ is output, $A$ is productivity, and $L$ is labour input. A firm sets its price $P$ at a constant mark-up $\mu$ over the effective wage cost per unit of production W/A. The expected real wage rate of workers is $W / P^{e}=A^{a}(1-u)^{1-a}$, where $0<a<1$ and $P^{e}$ is the expected price. If the price expected by workers matches the actual price level, then the effect of a rise in the level of productivity on unemployment is
[Question ID = 5851]
1. positive
[Option ID = 23398]
2. negative
[Option ID = 23399]
3. zero
[Option ID = 23400]
4. ambiguous
[Option ID = 23401]

## Correct Answer :-

- negative
[Option ID = 23399]

9) A household has an endowment of 1 unit of time. The household maximises its utility $u=\ln c+b \ln (1-\mathrm{l})$, where c denotes consumption and $I \in[0,1]$ denotes time spent working. It finances its consumption from labour income wl, where w is the market wage rate per unit of labour time. If the market wage rate goes up, then equilibrium labour supply of the household

## [Question ID = 5852]

1. increases
[Option ID = 23402]
2. decreases
[Option ID = 23403]
3. remains constant
[Option ID = 23404]
4. changes in an ambiguous manner
[Option ID = 23405]

## Correct Answer :-

- remains constant
[Option ID = 23404]

10) Consider the IS-LM model with a given price levelp Infestment is a decreasing function of the interest rate and savings is an increasing function of aggregate income. Fhe diranaker comoney balances $M / P$ is an increasing function of aggregate income and a decreasing function of the interest rate. The monetary authority chooses nominal money supply $M$

Correct Answer :-

- a fall in equilibrium output [Option ID $=23407$ ]

11) Consider the Solow growth model with a given savings ratio, a constant population growth rate, zero rate of capital depreciation, and no technical progress. Let $k^{*}$ be the steady-state capital-labour ratio in this economy. Suppose the economy is yet to reach the steady-state and has capital-labour ratio $k_{1}$ at time $t_{1}$ and capital-labour ratio $k_{2}$ at time $t_{2}$, such that $t_{1}<t_{2}$ and $k_{1}<k_{2}<k^{*}$. Let the associated growth rates of per capita income at time $t_{1}$ and $t_{2}$ be $g_{1}$ and $g_{2}$ respectively. Then, by the properties of the Solow model,
[Question ID = 5854]
1. $g_{1}<g_{2}$
[Option ID = 23410]
2. $g_{1}>g_{2}$
[Option ID = 23411]
3. $\mathrm{g}_{1}=\mathrm{g}_{2}$
[Option ID = 23412]
4. the relationship between $g_{1}$ and $g_{2}$ is ambiguous
[Option ID = 23413]
Correct Answer :-

- $\mathrm{g}_{1}>\mathrm{g}_{2}$
[Option ID = 23411]

12) A consumer lives for periods 1 and 2 . Given consumptions $c_{1}$ and $c_{2}$ in these periods, her utility is $U=\ln c_{1}+(1+$
p) $)^{-1}$ In $c_{2}$. She earns incomes $w_{1}$ and $w_{2}$ in the two periods and her lifetime budget constraint is $c_{1}+(1+r)^{-1} c_{2}=w_{1}+(1+$ $r)^{-1} w_{2}$, where $r$ is the interest rate on savings. If $r>\rho$, then
[Question ID = 5855]
1. $c_{1}>c_{2}$
[Option ID = 23414]
2. $c_{1}<c_{2}$
[Option ID = 23415]
3. $c_{1}=c_{2}$
[Option ID = 23416]
4. The relationship between $\mathrm{c}_{1}$ and $\mathrm{c}_{2}$ is ambiguous
[Option ID = 23417]
Correct Answer :-

- $\mathrm{c}_{1}<\mathrm{c}_{2}$
[Option ID = 23415]

13) A consumer lives for periods 1 and 2. Her lifetime utility function is $U\left(c_{1}, c_{2}\right)=\left(c_{1}^{\gamma}+c_{2}^{\gamma}\right) / \gamma$ where $0<\gamma<1$ and $c_{i}$ is consumption in period i . The elasticity of substitution between consumption in period 1 and consumption in period 2 is
[Question ID = 5856]
1. $1+\gamma$
[Option ID = 23418]
2. $1-\gamma$
[Option ID = 23419]
3. $1 /(1+\gamma)$
[Option ID = 23420]
4. $1 /(1-\gamma)$
[Option ID = 23421]
[Question ID = 5857]
5. less than the probability that it will end in 7 games
[Option ID = 23422]
6. equal to the probability that it will end in 7 games
[Option ID = 23423]
7. greater than the probability that it will end in 7 games
[Option ID = 23424]
8. None of these
[Option ID = 23425]
Correct Answer :-

- equal to the probability that it will end in 7 games
[Option ID = 23423]

15) Let $X$ and $Y$ be jointly normally distributed, i.e., $(X, Y) \sim N\left(\mu_{X}, \mu_{Y}, \sigma_{X}^{2}, \sigma_{Y}^{2}, \rho\right)$

If $\sigma_{X}^{2}=\sigma_{Y}^{2}$ and $0<\rho<1$, then

## [Question ID = 5858]

1. the OLS regression of $Y$ on $X$ will yield a slope that is less than unity, and that of $X$ on $Y$ will yield a slope greater than unity
[Option ID = 23426]
2. the OLS regression of $Y$ on $X$ will yield a slope that is less than unity, and that of $X$ on $Y$ will yield a slope less than unity
[Option ID = 23427]
3. the OLS regression of $Y$ on $X$ will yield a slope that is greater than unity, and that of $X$ on $Y$ will yield a slope less than unity
[Option ID = 23428]
4. it is not possible to draw conclusions about the magnitude of the slope with the given information
[Option ID = 23429]
Correct Answer :-

- the OLS regression of $Y$ on $X$ will yield a slope that is less than unity, and that of $X$ on $Y$ will yield a slope less than unity
[Option ID = 23427]

16) Let $\neg$ denote the negation of a statement. Consider a set $X$ and a binary relation $>$ on $X$. Relation $>$ is said to be irreflexive if $\neg x>x$ for every $x \in X$. Relation $>$ is said to be transitive if, for all $x, y, z \in X, x>y$ and $y>z$ implies $x>z$.

If $>$ is asymmetric (i.e., for all $x, y \in X, x>y$ implies $\neg y>x$ ) and negatively transitive (i.e., for all $x, y, z \in X, x>y$ implies $x>z$, or $z>y$, or both), then $>$ is
[Question ID = 5859]

1. irreflexive, but not transitive
[Option ID = 23430]
2. transitive, but not irreflexive
[Option ID = 23431]
3. irreflexive and transitive
[Option ID = 23432]
4. neither transitive, nor irreflexive
[Option ID = 23433]

## Correct Answer :-

- irreflexive and transitive
[Option ID = 23432]

17) Let $\neg$ denote the negation of a statement. Consider a set $X$ and a binary relation $>$ on $X$. For all $x, y \in X$, we say $x \geqslant y$ if and only if $\neg y>x$. Relation $\geqslant$ is said to be total if, for all $x, y \in X, \neg x \geqslant y$ implies $y \geqslant x$.

If $>$ is asymmetric (i.e., for all $x, y \in X, x>y$ implies $\neg y>x$ ) and negatively transitive (i.e., for all $x, y, z \in X, x>y$ implies $x>z$, or $z>y$, or both), then $\geqslant$
[Option ID = 23437]
Correct Answer :-

- is total
[Option ID = 23435]

18) Let $\neg$ denote the negation of a statement. Consider a set $X$ and a binary relation $>$ on $X$. For all $x, y \in X$, we say $x \geqslant y$ if and only if $\neg y>x$. Relation $\geqslant$ is said to be transitive if, for all $x, y, z \in X, x \geqslant y$ and $y \geqslant z$ implies $x \geqslant z$.

If $>$ is asymmetric (i.e., for all $x, y \in X, x>y$ implies $\neg y>x$ ) and negatively transitive (i.e., for all $x, y, z \in X, x>y$ implies $x>z$, or $z>y$, or both), then $\geqslant$
[Question ID = 5861]

1. is not transitive over a nonempty subset of $X$
[Option ID = 23438]
2. is not transitive
[Option ID = 23439]
3. may not be transitive
[Option ID = 23440]
4. is transitive
[Option ID = 23441]
Correct Answer :-

- is transitive
[Option ID = 23441]

19) Let $\neg$ denote the negation of a statement. Consider a set $X$ and a binary relation $>$ on $X$. For all $x, y \in X$, we say $x \sim y$ if and only if $\neg x>y$ and $\neg y>x$. Relation $\sim$ is said to be transitive if, for all $x, y, z \in X, x \sim y$ and $y \sim z$ implies $x \sim z$.

If $>$ is asymmetric (i.e., for all $x, y \in X, x>y$ implies $\neg y>x$ ) and negatively transitive (i.e., for all $x, y, z \in X, x>y$ implies $x>z$, or $z>y$, or both), then ~
[Question ID = 5862]

1. is transitive
[Option ID = 23442]
2. is not transitive
[Option ID = 23443]
3. may not be transitive
[Option ID = 23444]
4. is not transitive over a nonempty subset of $X$
[Option ID = 23445]

## Correct Answer :-

- is transitive
[Option ID = 23442]

20) Let $\neg$ denote the negation of a statement. Consider a set $X$ and a binary relation $>$ on $X$. For all $x, y \in X$, we say $x \sim y$ if and only if $\neg x>y$ and $\neg y>x$. Relation $\sim$ is said to be symmetric if, for all $x, y \in X, x \sim y$ implies $y \sim x$.

If $>$ is asymmetric (i.e., for all $x, y \in X, x>y$ implies $\neg y>x$ ) and negatively transitive (i.e., for all $x, y, z \in X, x>y$ implies $x>z$, or $z>y$, or both), then ~
[Question ID = 5863]

1. is symmetric
[Option ID = 23446]
2. is not symmetric
[Option ID = 23447]
3. may not be symmetric
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21) Consider the following game for players 1 and 2 . Player 1 moves first and chooses $L$ or $R$. If she chooses $L$, then the game ends and the payoffs are ( 1,0 ), where the first entry is 1 's payoff and the second entry is 2 's payoff. If she chooses $R$, then 2 chooses $U$ or $D$. If she chooses $U$, then the game ends and the payoffs are $(0,2)$. If she chooses $D$, then 1 chooses $L$ or $R$. If she chooses $L$, then the game ends and the payoffs are ( 4,0 ). If she chooses $R$, then the game ends and the payoffs are $(3,3)$. This game has
[Question ID = 5864]
1. one Nash equilibrium in pure strategies [Option ID $=23450$ ]
2. two Nash equilibria in pure strategies [Option ID = 23451]
3. three Nash equilibria in pure strategies [Option ID $=23452$ ]
4. no Nash equilibria in pure strategies [Option ID $=23453$ ]

## Correct Answer :-

- two Nash equilibria in pure strategies [Option ID = 23451]

22) Consider the following game for players 1 and 2 . Player 1 moves first and chooses $L$ or $R$. If she chooses $L$, then the game ends and the payoffs are ( 1,0 ), where the first entry is 1 's payoff and the second entry is 2 's payoff. If she chooses $R$, then 2 chooses $U$ or $D$. If she chooses $U$, then the game ends and the payoffs are $(0,2)$. If she chooses $D$, then 1 chooses $L$ or $R$. If she chooses $L$, then the game ends and the payoffs are ( 4,0 ). If she chooses $R$, then the game ends and the payoffs are $(3,3)$. This game has
[Question ID = 5865]
1. one subgame perfect Nash equilibrium [Option ID $=23454$ ]
2. two subgame perfect Nash equilibria [Option ID $=23455$ ]
3. three subgame perfect Nash equilibria [Option ID $=23456$ ]
4. no subgame perfect Nash equilibria [Option ID $=23457$ ]

Correct Answer :-

- one subgame perfect Nash equilibrium [Option ID = 23454]


## 23) In a non-cooperative game, if a profile of strategies

[Question ID = 5866]

1. is a Nash equilibrium, then it is an equilibrium in dominant strategies [Option ID = 23458]
2. is a Nash equilibrium, then it is a subgame perfect equilibrium [Option ID = 23459]
3. is a Nash equilibrium, then it is a sequential equilibrium [Option ID = 23460]
4. is an equilibrium in dominant strategies, then it is a Nash equilibrium [Option ID = 23461]

## Correct Answer :-

- is an equilibrium in dominant strategies, then it is a Nash equilibrium [Option ID = 23461]

24) If player 1 is the row player and player 2 is the column player in games
[Question ID = 5867]
1. 2's payoff in a Nash equilibrium of G' cannot be less than 2's payoff in a Nash equilibrium of $G$
[Option ID = 23462]
2. 2's payoff in a Nash equilibrium of G cannot be less than 2's payoff in a Nash equilibrium of G'
[Option ID = 23463]
3. 2's payoff in a Nash equilibrium of $G$ must be equal to 2 's payoff in a Nash equilibrium of $\mathrm{G}^{\prime}$
[Option ID = 23464]
4. 2's payoff in a Nash equilibrium of G may be higher than 2's payoff in a Nash equilibrium of G'
[Option ID = 23465]
Correct Answer :-

- 2's payoff in a Nash equilibrium of G may be higher than 2's payoff in a Nash equilibrium of G'
[Option ID = 23465]

25) Consider an exchange economy with agents 1 and 2 and goods $x$ and $y$. Agent 1 lexicographically prefers $x$ to $y$, i.e., between two non-identical bundles of $x$ and $y$, she strictly prefers the bundle with more of $x$, but if the bundles have the same amount of $x$, then she strictly prefers the bundle with more of $y$.

Agent 2's utility function is $u_{2}(x, y)=x+y$
Agent 1's endowment is $\left(\omega_{x}^{1}, \omega_{y}^{1}\right)=(0,10)$ and Agent 2's endowment is $\left(\omega_{x}^{2}, \omega_{y}^{2}\right)=(10,0)$
2. $[0,1]$
[Option ID = 23467]
3. $(0,1]$
[Option ID = 23468]
4. $\varnothing$
[Option ID = 23469]

## Correct Answer :-

- \{1\}
[Option ID = 23466]

26) Consider an exchange economy with agents 1 and 2 and goods $x$ and $y$.

Agent 1 lexicographically prefers $y$ to $x$, i.e., between two non-identical bundles of $x$ and $y$, she strictly prefers the bundle with more of $y$, but if the bundles have the same amount of $y$, then she strictly prefers the bundle with more of $x$.

Agent 2's utility function is $u_{2}(x, y)=x+y$
Agent 1's endowment is $\left(\omega_{x}^{1}, \omega_{y}^{1}\right)=(0,10)$ and Agent 2's endowment is $\left(\omega_{x}^{2}, \omega_{y}^{2}\right)=(10,0)$
The set of competitive equilibrium price ratios $p_{x} / p_{y}$ for this economy is
[Question ID = 5869]

1. $\{1\}$
[Option ID = 23470]
2. $[0,1]$
[Option ID = 23471]
3. $(0,1]$
[Option ID = 23472]
4. $\varnothing$
[Option ID = 23473]
Correct Answer :-

- $(0,1]$
[Option ID = 23472]

27) Consider an exchange economy with goods $x$ and $y$, and agents 1 and 2 , whose endowments are $\left(\omega_{x}^{1}, \omega_{y}^{1}\right)=(0,9)$ and $\left(\omega_{x}^{2}, \omega_{y}^{2}\right)=(10,0)$ respectively.

The utility functions of 1 and 2 are $u_{1}(x, y)=\min \{x, y\}$ and $u_{2}(x, y)=\min \{x, y\}$ respectively.
The competitive equilibrium price ratio $p_{x} / p_{y}$ is
[Question ID = 5870]

1. $9 / 10$
[Option ID = 23474]
2. $10 / 9$
[Option ID = 23475]
3. 1
[Option ID = 23476]
4. 0
[Option ID = 23477]

## Correct Answer :-

- 0
[Option ID = 23477]

28) Consider an exchange economy with goods $x$ and $y$, and agents 1 and 2 , whose endowments are $\left(\omega_{x}^{1}, \omega_{y}^{1}\right)=(0,9)$ and $\left(\omega_{x}^{2}, \omega_{y}^{2}\right)=(10,0)$ respectively.

The utility functions of 1 and 2 are $u_{1}(x, y)=\min \{x, y\}$ and $u_{2}(x, y)=\min \{x, y\}$ respectively.
The competitive equilibrium allocations are
[Option ID = 23479]
3. 1 gets $(x, y)$ and 2 gets $(9-x, 10-y)$, where $x \in[8,9]$ and $y=10$
[Option ID = 23480]
4. 1 gets $(x, y)$ and 2 gets $(9-x, 10-y)$, where $x=9$ and $y \in[9,10]$
[Option ID = 23481]

## Correct Answer :-

- 1 gets $(x, y)$ and 2 gets ( $10-x, 9-y$ ), where $x \in[9,10]$ and $y=9$
[Option ID = 23479]

29) Consider an exchange economy with goods $x$ and $y$, and agents 1 and 2 , whose endowments are $\left(\omega_{x}^{1}, \omega_{y}^{1}\right)=(0,9)$ and $\left(\omega_{x}^{2}, \omega_{y}^{2}\right)=(10,0)$ respectively.

The utility functions of 1 and 2 are $u_{1}(x, y)=\min \{x, y\}$ and $u_{2}(x, y)=\min \{x, y\}$ respectively.
The allocation that gives $(10,9)$ to 1 and $(0,0)$ to 2 is
[Question ID = 5872]

1. Pareto efficient but not a competitive equilibrium allocation
[Option ID = 23482]
2. neither Pareto efficient nor a competitive equilibrium allocation
[Option ID = 23483]
3. a competitive equilibrium allocation that is Pareto efficient
[Option ID = 23484]
4. a competitive equilibrium allocation that is not Pareto efficient
[Option ID = 23485]

## Correct Answer :-

- a competitive equilibrium allocation that is Pareto efficient
[Option ID = 23484]

30) Given a non-empty set $\mathrm{C}_{\subset \mathbb{R}^{n}}$, for every $\mathrm{p} \in \mathbb{R}_{+}^{n}$, let $\mathrm{c}(\mathrm{p}) \in \mathrm{C}$ be such that $p . c(p) \leq p . c$ for every $\mathrm{c} \in \mathrm{C}$. Then, the function $e: \mathbb{R}_{+}^{n} \rightarrow \mathbb{R}$ given by $e(p)=p . c(p)$ is
[Question ID = 5873]
1. linear
[Option ID = 23486]
2. convex
[Option ID = 23487]
3. concave
[Option ID = 23488]
4. quasi-convex
[Option ID = 23489]

## Correct Answer :-

- concave
[Option ID = 23488]

31) Given a non-empty set $\mathrm{C}_{\subset \mathbb{R}^{n}}$, for every $\mathrm{p} \in \mathbb{R}_{+}^{n}$, let $\mathrm{c}(\mathrm{p}) \in \mathrm{C}$ be such that $p . c(p) \leq p . c$ for every $\mathrm{c} \in \mathrm{C}$. Then, the function $e: \mathbb{R}_{+}^{n} \rightarrow \mathbb{R}$ given by $e(p)=p . c(p)$ is
[Question ID = 5874]
1. homogenous of degree 0
[Option ID = 23490]
2. homogenous of degree 1
[Option ID = 23491]
3. homogenous of degree $\infty$
[Option ID = 23492]
4. non-homogenous
[Option ID = 23493]
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32) Suppose $u: \mathbb{R} \rightarrow \mathbb{R}_{+}$is strictly increasing and has the supremum (i.e.; ceast upper bound) a $a \in \mathbb{E}$. Then, the function $x \mapsto u(x) /[\alpha-u(x)]$ is
[Question ID = 5875]
1. not well defined for some $x \in \mathbb{R}$
[Option ID = 23494]
2. bounded above
[Option ID = 23495]
3. unbounded above
[Option ID = 23496]
4. not strictly increasing
[Option ID = 23497]

## Correct Answer :-

- unbounded above
[Option ID = 23496]

33) The interval $[0, \infty)$ can be expressed as
[Question ID = 5876]
1. $\cap_{n=1}^{\infty}\left(a_{n}, \infty\right)$, where each $a_{n}$ is a rational number
[Option ID = 23498]
2. $\cup_{n=1}^{\infty}\left(a_{n}, b_{n}\right]$, where each $a_{n}$ and $b_{n}$ is a real number
[Option ID = 23499]
3. $n_{n=1}^{\infty}\left[a_{n}, b_{n}\right]$, where each $a_{n}$ and $b_{n}$ is an irrational number
[Option ID = 23500]
4. All of these
[Option ID = 23501]

## Correct Answer :-

- $\cap_{n=1}^{\infty}\left(a_{n}, \infty\right)$, where each $a_{n}$ is a rational number
[Option ID = 23498]

34) If $f: \mathbb{R}^{2} \rightarrow \mathbb{R}$ is given by

$$
f(x, y)= \begin{cases}x y /\left(x^{2}+y^{2}\right), & \text { if }(x, y) \neq(0,0) \\ 0, & \text { if }(x, y)=(0,0)\end{cases}
$$

then

## [Question ID = 5877]

1. $f$ is differentiable at $(0,0)$ and both partial derivatives at $(0,0)$ are 0
[Option ID = 23502]
2. $f$ is non-differentiable at $(0,0)$ and both partial derivatives at $(0,0)$ are 0
[Option ID = 23503]
3. $f$ is differentiable at $(0,0)$ and neither partial derivative at $(0,0)$ is 0
[Option ID = 23504]
4. $f$ is non-differentiable at $(0,0)$ and neither partial derivative at $(0,0)$ exists
[Option ID = 23505]

## Correct Answer :-

- $f$ is non-differentiable at $(0,0)$ and both partial derivatives at $(0,0)$ are 0
[Option ID = 23503]

35) Suppose $f: \mathbb{R} \rightarrow \mathbb{R}$ is a twice-differentiable function that solves the differential equation $D^{2} f-D f-f-1=0$ over $_{\mathbb{R}}$ and satisfies the condition $f(0)=0=f(k)$ for some $k>0$. Then,

## [Question-1D = 5878]

1. $f$ has positive and negative values over $(0, k)$

Correct Answer :-

- f has only negative values over $(0, k)$
[Option ID = 23508]

36) Let ${ }_{B}$ be the collection of sets $E \subset R$ satisfying: for every $x \in E$, there are real numbers $a$ and $b$ such that $a<b$ and $x \in(a, b) \subset E$

Let ${ }_{C}$ be the collection of sets $E \subset R$ satisfying: for every ${ }_{x \in E}$, there are rational numbers $a$ and ${ }_{b}$ such that $a<b$ and $x \in(a, b) \subset E$
then,
[Question ID = 5879]

1. $\mathcal{B} \subset C$ and $\mathcal{B} \neq C$
[Option ID = 23510]
2. $\mathcal{C} \mathcal{B}$ and $\mathcal{B} \neq \mathcal{C}$
[Option ID = 23511]
3. $\mathcal{B}=\mathrm{C}$
[Option ID = 23512]
4. Neither $\mathcal{B} \subset \mathcal{C}$ nor $\mathcal{C} \subset \mathcal{B}$
[Option ID = 23513]

## Correct Answer :-

- $\mathcal{B}=\mathrm{C}$
[Option ID = 23512]

37) The set $\left\{(x, y) \in \mathbb{R}^{2} \mid x>0\right.$ and $\left.y \leq \ln x-e^{x}\right\}$ is
[Question ID = 5880]
1. a linear subspace of $\mathbb{R}^{2}$
[Option ID = 23514]
2. convex
[Option ID = 23515]
3. non-convex
[Option ID = 23516]
4. a convex polytope
[Option ID = 23517]

## Correct Answer :-

- convex
[Option ID = 23515]

38) Suppose the distance between $x, y \in \mathbb{R}$ is given by $|x-y|$ and $f: \mathbb{R} \rightarrow \mathbb{R}$ is a continuous function. If $E$ is an open subset of $\mathbb{R}$ , then $\{x \in \mathbb{R} \mid f(x) \in E\}$ is
[Question ID = 5881]
1. An open subset of $\mathbb{R}$
[Option ID = 23518]
2. A closed subset of $\mathbb{R}$
[Option ID = 23519]
3. Neither an open, nor a closed, subset of $\mathbb{R}$
[Option ID = 23520]
4. An open and closed subset of $\mathbb{R}$

## [OptionTIV = 23521]

[Question ID = 5882]

1. $e^{k \pi}$
[Option ID = 23522]
2. $\pi^{k e}$
[Option ID = 23523]
3. They are equal
[Option ID = 23524]
4. It depends on the value of $k$
[Option ID = 23525]

## Correct Answer :-

- It depends on the value of $k$
[Option ID = 23525]

40) Consider the matrix $A=\left(\begin{array}{cc}\cos \theta & -\sin \theta \\ \sin \theta & \cos \theta\end{array}\right)$
where $\theta \in[0,2 \pi)$. The inner product of vectors $v=\left(v_{1}, v_{2}\right)$ and $w=\left(w_{1}, w_{2}\right)$ in $\mathbb{R}^{2}$ is defined by $\langle v, w\rangle=v_{1} w_{1}+v_{2} w_{2}$. So, for the vectors $v$ and $w$ in $\mathbb{R}^{2}$
[Question ID = 5883]
1. $\langle A v, A w\rangle=\langle v, w\rangle$
[Option ID = 23526]
2. $\langle A v, A w\rangle\rangle\langle v, w\rangle$
[Option ID = 23527]
3. $\langle A v, A w\rangle<\langle v, w\rangle$
[Option ID = 23528]
4. The comparison of $\langle A v, A w\rangle$ and $\langle v, w\rangle$ depends on the value of $\theta$
[Option ID $=23529]$
Correct Answer :-

- $\langle A v, A w\rangle=\langle v, w\rangle$
[Option ID = 23526]

41) Let $\lfloor x\rfloor$ be the greatest integer that is less than or equal to $x \in \mathbb{R}$. The function $f: \mathbb{R} \rightarrow \mathbb{R}$, defined by $f(x)=x-\lfloor x\rfloor$ for $x \in \mathbb{R}$, is

## [Question ID = 5884]

1. Left-discontinuous at an integer
[Option ID = 23530]
2. Right-discontinuous at an integer
[Option ID = 23531]
3. Left discontinuous and right-discontinuous at an integer
[Option ID = 23532]
4. Discontinuous everywhere
[Option ID = 23533]
Correct Answer :-

- Left-discontinuous at an integer
[Option ID $=23530$ ]

42) Let $[x]$ be the smallest integer that is greater than or equal to $x \in \mathbb{R}$. The function $f: \mathbb{R} \rightarrow \mathbb{R}$, defined by $f(x)=\lceil x\rceil-x$ for $x \in \mathbb{R}$ is
[Question ID = 5885]
1. Left-discontinuous at an integer

## Correct Answer :-

- Right-discontinuous at an integer
[Option ID = 23535]

43) Let $\lfloor x\rfloor$ be the greatest integer that is less than or equal to $x \in \mathbb{R}$. Let $\lceil x\rceil$ be the smallest integer that is greater than or equal to $x \in \mathbb{R}$. The function $f: \mathbb{R} \rightarrow \mathbb{R}$, defined by $f(x)=\lceil x\rceil-\lfloor x\rfloor$ for $x \in \mathbb{R}$, is

## [Question ID = 5886]

1. Left-discontinuous at an integer
[Option ID = 23538]
2. Right-discontinuous at an integer
[Option ID = 23539]
3. Left discontinuous and right-discontinuous at an integer
[Option ID = 23540]
4. Discontinuous everywhere
[Option ID = 23541]

## Correct Answer :-

- Left discontinuous and right-discontinuous at an integer
[Option ID = 23540]

44) If
$A=\left\{(x, y) \in \mathbb{R}^{2} \mid x \geq 0, y \geq 0, x y \geq 1\right\}$
$B=\left\{(x, y) \in \mathbb{R}^{2} \mid x \leq 0, y \geq 0, x y \leq-1\right\}$
and
$C=\{a+b \mid a \in A, b \in B\}$
Then,
[Question ID = 5887]
1. $\left\{(x, y) \in \mathbb{R}^{2} \mid x=0, y \geq 0\right\}$ is a subset of C
[Option ID = 23542]
2. $\left\{(x, y) \in \mathbb{R}^{2} \mid x=0, y>0\right\}$ is a subset of C
[Option ID $=23543$ ]
3. $\left\{(x, y) \in \mathbb{R}^{2} \mid x \geq 0, y=0\right\}$ is a subset of $C$
[Option ID $=23544]$
4. $\left\{(x, y) \in \mathbb{R}^{2} \mid x>0, y=0\right\}$ is a subset of C
[Option ID $=23545$ ]
Correct Answer :-

- $\left\{(x, y) \in \mathbb{R}^{2} \mid x=0, y>0\right\}$ is a subset of $C$
[Option ID = 23543]

45) Consider a $4 \times 4$-matrix A. Obtain matrix $B$ from matrix $A$ by performing the following operations in sequence:
(1) Interchange the first and fourth columns, and then
(2) Interchange the second and fourth rows. Then,
[Question ID = 5888]
1. $\operatorname{det} A=\operatorname{det} B$
[Option ID = 23546]
2. $\operatorname{det} A \neq \operatorname{det} B$
[Option ID = 23547]
3. $\operatorname{det} \mathrm{B} \leq 0$
46) The maximum value of $f(x, y)=x y$, subject to $|x| \geq|y|$ and $|x|+|y| \leq 1$, is

## [Question ID = 5889]

1. $1 / 4$
[Option ID = 23550]
2. $1 / 2$
[Option ID = 23551]
3. 4
[Option ID = 23552]
4. 2
[Option ID = 23553]

## Correct Answer :-

- $1 / 4$
[Option ID = 23550]

47) Consider a decreasing differentiable function $g: \mathbb{R}_{+} \rightarrow \mathbb{R}_{+}$and an increasing continuous function $f: \mathbb{R}_{+} \rightarrow \mathbb{R}_{+}$. If $F: \mathbb{R}_{+} \rightarrow \mathbb{R}_{+}$ satisfies $F(x)=\int_{0}^{g(x)} f(t) d t$ for every $x \in \mathbb{R}_{+}$, then F is
[Question ID = 5890]
1. Increasing over [0, a] and decreasing over $[\mathrm{a}, \infty)$, for some a > 0
[Option ID = 23554]
2. Decreasing over [0, a] and increasing over [a, $\infty$ ), for some a > 0
[Option ID = 23555]
3. Increasing
[Option ID = 23556]
4. Decreasing
[Option ID = 23557]
Correct Answer :-

- Decreasing
[Option ID = 23557]

48) If $f: \mathbb{R} \rightarrow \mathbb{R}$ and $g: \mathbb{R} \rightarrow \mathbb{R}$ are defined by
$f(x)=\left\{\begin{array}{ll}0, & \text { if } x \text { is rational } \\ x, & \text { if } x \text { is irrational }\end{array}\right.$ and $g(x)=\left\{\begin{array}{c}0, \text { if } x \text { is irrational } \\ x, \text { if } x \text { is rational }\end{array}\right.$
Then $h: \mathbb{R} \rightarrow \mathbb{R}$, given by $h(x)=f(x)-g(x)$, is
[Question ID = 5891]
1. Injective but not surjective
[Option ID = 23558]
2. Surjective but not injective
[Option ID = 23559]
3. Neither injective nor surjective
[Option ID = 23560]
4. Bijective
[Option ID = 23561]
Correct Answer :-

- Bijective
[Option ID = 23561]

49) Given nonempty subsets of $\mathbb{R}^{2}$, say $Y_{1}, \ldots, Y_{n}$, let


Fix $\mathbf{p} \in \mathbb{R}^{2}$. For a nonempty set $X_{\subset} \mathbb{R}^{2}$, let $v(p, X)$ www. FirstRanker.com
[Question ID = 5892]

1. $v\left(p, Y^{*}\right)<\sum_{j=1}^{n} v\left(p, Y_{j}\right)$ or $v\left(p, Y^{*}\right)>\sum_{j=1}^{n} v\left(p, Y_{j}\right)$
[Option ID $=23562$ ]
2. $v\left(p, Y^{*}\right)=\sum_{j=1}^{n} v\left(p, Y_{j}\right)$
[Option ID = 23563]
3. $v\left(p, Y^{*}\right)<\sum_{j=1}^{n} v\left(p, Y_{j}\right)$
[Option ID = 23564]
4. $v\left(p, Y^{*}\right)>\sum_{j=1}^{n} v\left(p, Y_{j}\right)$
[Option ID = 23565]
Correct Answer :-

- $v\left(p, Y^{*}\right)=\sum_{j=1}^{n} v\left(p, Y_{j}\right)$
[Option ID = 23563]

50) If $A=\left[\begin{array}{cccc}1 & 0 & 0 & 0 \\ 2 & 2 & 0 & 0 \\ 3 & 2 & -2 & 0 \\ 4 & 3 & 2 & -1\end{array}\right]$
and $A^{T}$ is the transpose of ${ }_{A}$, then $\operatorname{det}\left(A^{T} A\right)$ is
[Question ID = 5893]
1. 16
[Option ID = 23566]
2. -16
[Option ID = 23567]
3. 4
[Option ID = 23568]
4. -4
[Option ID = 23569]
Correct Answer :-

- 16
[Option ID = 23566]

