



Topic: - MATHS MA S2

1) Let $\{x_n\}$ and $\{y_n\}$ be sequences of real numbers such that $x_n \leq y_n$ for all $n \geq N$, where N is some positive integer. Consider the following statements:

(a) $\liminf_{n \rightarrow \infty} x_n \leq \liminf_{n \rightarrow \infty} y_n$

(b) $\limsup_{n \rightarrow \infty} x_n \leq \limsup_{n \rightarrow \infty} y_n$

Which of the above statements is(are) correct?

[Question ID = 5742]

1. Neither (a) nor (b)

[Option ID = 22962]

2. Only (a)

[Option ID = 22963]

3. Only (b)

[Option ID = 22964]

4. Both (a) and (b)

[Option ID = 22965]

Correct Answer :-

• Both (a) and (b)

[Option ID = 22965]

2) Which of the sequences $\{a_n\}$ and $\{b_n\}$ of real numbers with $n - \text{th}$ terms

$$a_n = \frac{(n^2 + 20n + 35) \sin n^3}{n^2 + n + 1}$$

$$b_n = 2 \cos n - \sin n$$

has(have) convergent subsequences?

[Question ID = 5743]

1. Neither $\{a_n\}$ nor $\{b_n\}$

[Option ID = 22966]

2. Only $\{a_n\}$

[Option ID = 22967]

3. Only $\{b_n\}$

[Option ID = 22968]

4. Both $\{a_n\}$ and $\{b_n\}$

[Option ID = 22969]

Correct Answer :-

• Both $\{a_n\}$ and $\{b_n\}$

[Option ID = 22969]

3) Consider the following series:

(a) $\sum_{n=1}^{\infty} \frac{x^n}{n!}, x \in \mathbb{R}$

(b) $\sum_{n=1}^{\infty} \frac{1}{n + \sin n}$

(c) $\sum_{n=1}^{\infty} \frac{1}{2^n \sqrt{n}}$

(d) $\sum_{n=1}^{\infty} \sin n$

Which of the above series is (are) convergent?



[Option ID = 22970]

2. Only (a), (c) and (d)

[Option ID = 22971]

3. Only (a) and (c)

[Option ID = 22972]

4. Only (c)

[Option ID = 22973]

Correct Answer :-

• Only (a) and (c)

[Option ID = 22972]

4) The union of infinitely many closed subsets of the real line is

[Question ID = 5745]

1. uncountable [Option ID = 22974]

2. finite [Option ID = 22975]

3. always closed [Option ID = 22976]

4. need not be closed [Option ID = 22977]

Correct Answer :-

• need not be closed [Option ID = 22977]

5) Consider the series $\sum_{n=1}^{\infty} a_n$ where $a_n = \left(2 + \sin \frac{n\pi}{2}\right) r^n, r > 0$. What are the values of $\liminf_{n \rightarrow \infty} \frac{a_{n+1}}{a_n}$ and $\limsup_{n \rightarrow \infty} \frac{a_{n+1}}{a_n}$?

[Question ID = 5746]

1. $r/2$ and $2r$ [Option ID = 22978]

2. $r/3$ and r [Option ID = 22979]

3. $2r/3$ and $3r/2$ [Option ID = 22980]

4. 0 and 1 [Option ID = 22981]

Correct Answer :-

• $r/2$ and $2r$ [Option ID = 22978]

6) Consider the following series:

(a) $\sum_{n=1}^{\infty} 3^{-n} \sin 3^n x$ on \mathbb{R}

(b) $\sum_{n=1}^{\infty} 2^{-n} x^n$ on $(-2, 2)$

(c) $\sum_{n=1}^{\infty} \frac{1}{n^2} \cos nx$ on \mathbb{R}

Which of the above series converge uniformly on the indicated domain?

[Question ID = 5747]

1. Only (a) and (b)

[Option ID = 22982]

2. Only (b) and (c)

[Option ID = 22983]

3. Only (a) and (c)

[Option ID = 22984]

4. All of (a), (b) and (c)

[Option ID = 22985]

Correct Answer :-

• Only (a) and (c)

[Option ID = 22984]

7) Let $\{f_n\}$ be a sequence of continuous functions on $[a, b]$ converging uniformly to the function f . Consider the following statements:

(a) f is bounded on $[a, b]$



Which of the following statements is(are) correct?

[Question ID = 5748]

1. Only (a) and (b)

[Option ID = 22986]

2. Only (a) and (c)

[Option ID = 22987]

3. Only (c)

[Option ID = 22988]

4. Only (b)

[Option ID = 22989]

Correct Answer :-

• Only (a) and (b)

[Option ID = 22986]

8) Let $G(x)$ be a real-valued function defined by $G(x) = \int_{x^3}^{4x^2} \cos \sqrt{t} dt$. If G' is the derivative of G , then

[Question ID = 5749]

1. $G'(\pi/2) = -4\pi$

[Option ID = 22990]

2. $G'(\pi/2) = -4\pi - 1$

[Option ID = 22991]

3. $G'(\pi/2) = -\pi$

[Option ID = 22992]

4. $G'(\pi/2) = 0$

[Option ID = 22993]

Correct Answer :-

• $G'(\pi/2) = -4\pi$

[Option ID = 22990]

9) Let $f(x) = \begin{cases} (4-x^2)^{5/2}, & |x| < 2 \\ 0, & |x| \geq 2 \end{cases}$

Consider the following statements:

- f is not continuous on \mathbb{R}
- f is continuous on \mathbb{R} but not differentiable at $x = 2, -2$
- f is differentiable on \mathbb{R} but f' is not continuous on \mathbb{R}
- f is differentiable on \mathbb{R} and f' is continuous on \mathbb{R}

Which of the above statements is(are) correct?

[Question ID = 5750]

1. Only (a) and (d)

[Option ID = 22994]

2. Only (b) and (c)

[Option ID = 22995]

3. Only (c)

[Option ID = 22996]

4. Only (d)

[Option ID = 22997]

Correct Answer :-

• Only (d)

[Option ID = 22997]



[Question ID = 5751]

1. $(-1, 1)$

[Option ID = 22998]

2. $[3, 4]$

[Option ID = 22999]

3. $[-2, -1]$

[Option ID = 23000]

4. $[-5, -3]$

[Option ID = 23001]

Correct Answer :-

• $[-2, -1]$

[Option ID = 23000]

11) The Wronskian of $\cos x, \sin x$ and e^{-x} at $x = 0$ is

[Question ID = 5752]

1. 1

[Option ID = 23002]

2. 2

[Option ID = 23003]

3. -1

[Option ID = 23004]

4. -2

[Option ID = 23005]

Correct Answer :-

• 2

[Option ID = 23003]

12) The solution of the initial value problem $y' = 1 + y^2, y(0) = 1$, is:-

[Question ID = 5753]

1. $y = \operatorname{cosec}(x + \pi/4)$

[Option ID = 23006]

2. $y = \tan(x + \pi/4)$

[Option ID = 23007]

3. $y = \sec(x + \pi/4)$

[Option ID = 23008]

4. $y = \cot(x + \pi/4)$

[Option ID = 23009]

Correct Answer :-

• $y = \tan(x + \pi/4)$

[Option ID = 23007]

13) How many solution(s) does the initial value problem $y' - \frac{2}{x}y = 0, y(0) = 0$ have?

[Question ID = 5754]

1. No solution

[Option ID = 23010]

2. Unique solution

[Option ID = 23011]

3. Two solutions

[Option ID = 23012]

4. Infinitely many solutions

[Option ID = 23013]

Correct Answer :-

• Infinitely many solutions



14) The general solution of the equation $y'' + y = \cos x$ ($0 < x < \pi$) is (c_1, c_2 are arbitrary constants)

www.FirstRanker.com

www.FirstRanker.com

[Question ID = 5755]

1. $c_1 \cos x + c_2 \sin x - x \cos x + \sin x \ln(\sin x)$

[Option ID = 23014]

2. $c_1 \cos x + c_2 \sin x + x \cos x + \sin x \ln(\sin x)$

[Option ID = 23015]

3. $c_1 \cos x + c_2 \sin x - x \sin x + \cos x \ln(\sin x)$

[Option ID = 23016]

4. $c_1 \cos x + c_2 \sin x + x \sin x + \cos x \ln(\sin x)$

[Option ID = 23017]

Correct Answer :-

• $c_1 \cos x + c_2 \sin x - x \cos x + \sin x \ln(\sin x)$

[Option ID = 23014]

15) The particular integral of the differential equation is $y'' + y = x^3$ is

[Question ID = 5756]

1. $x^2 + 6x$

[Option ID = 23018]

2. $x^2 - 6x$

[Option ID = 23019]

3. $x^3 + 6x$

[Option ID = 23020]

4. $x^3 - 6x$

[Option ID = 23021]

Correct Answer :-

• $x^3 - 6x$

[Option ID = 23021]

16) The complete integral of the partial differential equation $p^2 z^2 + q^2 = 1$, where $p = \frac{\partial z}{\partial x}$, $q = \frac{\partial z}{\partial y}$ is

(a, b are arbitrary constants)

[Question ID = 5757]

1. $z + a^2 \ln\left(\frac{z + \sqrt{z^2 + a^2}}{a}\right) = 0$

[Option ID = 23022]

2. $a^2 z + by + x^2 = 0$

[Option ID = 23023]

3. $z\sqrt{z^2 + a^2} + a^2 \ln\left(\frac{z + \sqrt{z^2 + a^2}}{a}\right) = 2x + 2ay + 2b$

[Option ID = 23024]

4. $z^2 + y^2 = x^2 + 2x + 2ay + 2b$

[Option ID = 23025]

Correct Answer :-

• $z\sqrt{z^2 + a^2} + a^2 \ln\left(\frac{z + \sqrt{z^2 + a^2}}{a}\right) = 2x + 2ay + 2b$

[Option ID = 23024]

17) The complete integral of the partial differential equation $z = px + qy - \sin(pq)$ where

$p = \frac{\partial z}{\partial x}$, $q = \frac{\partial z}{\partial y}$ is

www.FirstRanker.com

[Question ID = 5758]

2. $z = ax + by - \sin(ab)$
[Option ID = 23026]

[Option ID = 23027]

3. $z = ax + y + \sin b$

[Option ID = 23028]

4. $z = x + by - \sin a$

[Option ID = 23029]

Correct Answer :-

• $z = ax + by - \sin(ab)$

[Option ID = 23027]

18) The partial differential equation $y u_{xx} + 2xy u_{xy} + x u_{yy} = u_x + u_y$ is

[Question ID = 5759]

1. Hyperbolic in $\{(x, y) | 0 < xy < 1\}$

[Option ID = 23030]

2. Hyperbolic in $\{(x, y) | xy > 1\}$

[Option ID = 23031]

3. Elliptic in $\{(x, y) | xy > 1\}$

[Option ID = 23032]

4. Elliptic in $\{(x, y) | xy < 0\}$

[Option ID = 23033]

Correct Answer :-

• Hyperbolic in $\{(x, y) | xy > 1\}$

[Option ID = 23031]

19) The general solution of the equation $\frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial y^2} = x - y$ is

[Question ID = 5760]

1. $\frac{1}{4}x(x-y)^2 + \phi_1(x^2+y) + \phi_2(x-y)$

[Option ID = 23034]

2. $\frac{1}{4}x(x-y)^2 + \phi_1(x+y) + \phi_2(x-y)$

[Option ID = 23035]

3. $\phi_1(x+y) + \phi_2(x^2-y)$

[Option ID = 23036]

4. $\phi_1(x^2+y) + \phi_2(x^2-y) - \frac{1}{4}x(x+y)$

[Option ID = 23037]

Correct Answer :-

• $\frac{1}{4}x(x-y)^2 + \phi_1(x+y) + \phi_2(x-y)$

[Option ID = 23035]

20) The general solution of $\frac{\partial^2 u}{\partial \tau^2} = c^2 \frac{\partial^2 u}{\partial x^2}$ with $u(0, t) = u(2, t) = 0$, $u(x, 0) = \sin^3 \frac{\pi x}{2}$ and $u_\tau(x, 0) = 0$ is

[Question ID = 5761]

1. $\frac{3}{4} \sin \frac{\pi x}{2} \sin \frac{\pi c t}{2}$

[Option ID = 23038]

2. $\frac{3}{4} \sin \frac{\pi x}{2} \cos \frac{\pi c t}{2} - \frac{1}{4} \sin \frac{3\pi x}{2} \cos \frac{3\pi c t}{2}$

[Option ID = 23039]

3. $\frac{3}{4} \cos \frac{\pi x}{2} \sin \frac{\pi c t}{2} - \frac{1}{4} \sin \frac{3\pi x}{2} \sin \frac{3\pi c t}{2}$

[Option ID = 23040]

4. $\frac{3}{4} \sin \frac{\pi x}{2} \cos \frac{\pi c t}{2} - \frac{1}{4} \cos \frac{3\pi x}{2}$

$$\bullet \frac{3}{4} \sin \frac{\pi x}{2} \cos \frac{\pi ct}{2} - \frac{1}{4} \sin \frac{3\pi x}{2} \cos \frac{3\pi ct}{2}$$

[Option ID = 23039]

21) Let $f: \mathbb{R}^2 \rightarrow \mathbb{R}$ be given by

$$f(x, y) = \begin{cases} (x^2 + y^2) \ln(x^2 + y^2), & \text{if } (x, y) \neq (0, 0) \\ 0, & \text{if } (x, y) = (0, 0) \end{cases}$$

Then,

[Question ID = 5762]

1. f_{xy} and f_{yx} are continuous at $(0, 0)$, and $f_{xy}(0, 0) = f_{yx}(0, 0)$

[Option ID = 23042]

2. f_{xy} and f_{yx} are discontinuous at $(0, 0)$, but $f_{xy}(0, 0) = f_{yx}(0, 0)$

[Option ID = 23043]

3. f_{xy} and f_{yx} are continuous at $(0, 0)$, but $f_{xy}(0, 0) \neq f_{yx}(0, 0)$

[Option ID = 23044]

4. f_{xy} and f_{yx} are discontinuous at $(0, 0)$ and $f_{xy}(0, 0) \neq f_{yx}(0, 0)$

[Option ID = 23045]

Correct Answer :-

• f_{xy} and f_{yx} are discontinuous at $(0, 0)$, but $f_{xy}(0, 0) = f_{yx}(0, 0)$

[Option ID = 23043]

22) The directional derivative of $f(x, y, z) = xy^2 + yz^2 + zx^2$ defined on \mathbb{R}^3 along the tangent to the curve $x = t, y = t^2, z = t^3$ at the point $(1, 1, 1)$ is

[Question ID = 5763]

1. $-\frac{18}{\sqrt{14}}$

[Option ID = 23046]

2. $\frac{13}{\sqrt{14}}$

[Option ID = 23047]

3. $-\frac{13}{\sqrt{14}}$

[Option ID = 23048]

4. $\frac{18}{\sqrt{14}}$

[Option ID = 23049]

Correct Answer :-

• $\frac{18}{\sqrt{14}}$

[Option ID = 23049]

23) The unique polynomial of degree 2 passing through $(1, 1)$, $(3, 27)$ and $(4, 64)$ obtained by Lagrange interpolation is

[Question ID = 5764]

1. $8x^2 - 17x + 12$

[Option ID = 23050]

2. $8x^2 - 19x - 12$

[Option ID = 23051]

3. $8x^2 + 14x - 12$

[Option ID = 23052]

4. $8x^2 - 19x + 12$

[Option ID = 23053]

Correct Answer :-

• $8x^2 - 19x + 12$



[Question ID = 5765]

1. 0.8512

[Option ID = 23054]

2. 0.8125

[Option ID = 23055]

3. 0.7625

[Option ID = 23056]

4. 0.6702

[Option ID = 23057]

Correct Answer :-

• 0.8512

[Option ID = 23054]

25) Consider the differential equation, $\frac{dy}{dx} = y - x$, $y(0) = 2$. The absolute value of the difference in the solutions obtained by Euler method and Runge-Kutta second order method at $y(0.1)$ using step size 0.1 is

[Question ID = 5766]

1. 2.205 [Option ID = 23058]

2. 2.252 [Option ID = 23059]

3. 0.005 [Option ID = 23060]

4. 0.055 [Option ID = 23061]

Correct Answer :-

• 0.005 [Option ID = 23060]

26) The approximate value of $(17)^{1/3}$ obtained after two iterations of Newton-Raphson method starting with initial approximation $x_0 = 2$ is

[Question ID = 5767]

1. 2.7566

[Option ID = 23062]

2. 2.5826

[Option ID = 23063]

3. 2.6713

[Option ID = 23064]

4. 2.4566

[Option ID = 23065]

Correct Answer :-

• 2.5826

[Option ID = 23063]

27) For an infinite discrete metric space (X, d) , which of the following statements is correct?

[Question ID = 5768]

1. X is compact

[Option ID = 23066]

2. For every $A \subseteq X$, $A^\circ \cup \bar{A} = X$, where \bar{A} and A° denote respectively the closure and interior of A in X

[Option ID = 23067]

3. X is connected

[Option ID = 23068]

4. X is not totally bounded

[Option ID = 23069]

Correct Answer :-

• X is not totally bounded



28) Consider the metric space (l_2, d) of square summable sequences with the Euclidean metric $d(x, y) = \sqrt{\sum_{i=1}^{\infty} (x_i - y_i)^2}$. Let $Y = \{e_1, e_2, \dots\} \subseteq l_2$ where e_i is the sequence of 1 at the i -th place and 0 elsewhere. Then,

[Question ID = 5769]

1. Y is not compact and has no limit point

[Option ID = 23070]

2. Y is compact and each e_i is a limit point of Y

[Option ID = 23071]

3. Y is not compact and has a limit point

[Option ID = 23072]

4. Y is compact and has no limit point

[Option ID = 23073]

Correct Answer :-

• Y is not compact and has no limit point

[Option ID = 23070]

29) Let $C[0, 1]$ be the set of real valued continuous functions on $[0, 1]$ with sup-metric. Let $A = \{f \in C[0, 1] \mid f(0) = 0\}$ and $B = \{f \in C[0, 1] \mid f(0) > 0\}$ be the subspaces of $C[0, 1]$. Then,

[Question ID = 5770]

1. Both A and B are complete

[Option ID = 23074]

2. A is complete but B is incomplete

[Option ID = 23075]

3. A is incomplete but B is complete

[Option ID = 23076]

4. Neither A nor B is complete

[Option ID = 23077]

Correct Answer :-

• A is complete but B is incomplete

[Option ID = 23075]

30) Let (\mathbb{R}, d) and (\mathbb{R}, u) be the metric spaces with the discrete metric space d and usual metric u respectively.

Let $f: (\mathbb{R}, d) \rightarrow (\mathbb{R}, u)$ and $g: (\mathbb{R}, u) \rightarrow (\mathbb{R}, d)$ be the functions given by

$$f(x) = g(x) = \begin{cases} 0, & x \leq 0 \\ x + 1, & x > 0 \end{cases}$$

Then,

[Question ID = 5771]

1. Both f and g are continuous

[Option ID = 23078]

2. Neither f nor g is continuous

[Option ID = 23079]

3. f is continuous but g is not

[Option ID = 23080]

4. g is continuous but f is not

[Option ID = 23081]

Correct Answer :-

• f is continuous but g is not

[Option ID = 23080]

31) Let $Y_1 = \{(x, y) \in \mathbb{R}^2 \mid y = \sin \frac{1}{x}, 0 < x \leq \pi\}$ and $Y_2 = \{(0, y) \in \mathbb{R}^2 \mid y \in [-2, 2]\}$ be subspaces of the



[Question ID = 5772]

- $\bar{Y}_1 \cup Y_2$ is connected
[Option ID = 23082]
- $Y_1 \cup \bar{Y}_2$ is connected
[Option ID = 23083]
- $\bar{Y}_1 \cap Y_2$ is disconnected
[Option ID = 23084]
- $\overline{Y_1 \cap Y_2}$ is a non-empty bounded subset of \mathbb{R}^2
[Option ID = 23085]

Correct Answer :-

- $\bar{Y}_1 \cup Y_2$ is connected
[Option ID = 23082]

32) Let \mathcal{F} be the set of all real-valued Riemann integrable functions on $[0, 1]$ and let f be the function given by

$$f(x) = \begin{cases} 0, & \text{if } x = 0 \\ \frac{1}{n}, & \text{if } \frac{1}{n+1} < x \leq \frac{1}{n} \text{ for } n \in \mathbb{N} \end{cases}$$

Which of the following statements is correct?

[Question ID = 5773]

- f is monotonically decreasing on $[0, 1]$ but $f \notin R[0, 1]$
[Option ID = 23086]
- f is monotonically decreasing on $[0, 1]$ and $f \in R[0, 1]$
[Option ID = 23087]
- f is discontinuous at infinitely many points in $[0, 1]$ but $f \in R[0, 1]$
[Option ID = 23088]
- f is discontinuous at infinitely many points in $[0, 1]$ and $f \notin R[0, 1]$
[Option ID = 23089]

Correct Answer :-

- f is discontinuous at infinitely many points in $[0, 1]$ and $f \in R[0, 1]$
[Option ID = 23089]

33) The improper integral

$$\int_{-\infty}^{\infty} \frac{dx}{x^2 + 1}$$

[Question ID = 5774]

- Converges to π
[Option ID = 23090]
- Converges to $\pi/2$
[Option ID = 23091]
- Converges to 0
[Option ID = 23092]
- Diverges
[Option ID = 23093]

Correct Answer :-

- Converges to π
[Option ID = 23090]

34) Consider the functions $f(x) = \frac{x^2-1}{x-1}$ and $g(x) = \frac{|x^2-1|}{x-1}$, $x \neq 1$. Then

[Question ID = 5775]

- Both f and g have removable discontinuity at $x = 1$



3. f has a removable discontinuity at $x = 1$, while g has a jump discontinuity at $x = 1$

[Option ID = 23096]

4. f has a jump discontinuity at $x = 1$ while g has a removable discontinuity at $x = 1$

[Option ID = 23097]

Correct Answer :-

- f has a removable discontinuity at $x = 1$, while g has a jump discontinuity at $x = 1$

[Option ID = 23096]

- 35) What is the length of the interval on which the function $f(x) = x^3 - 6x^2 - 15x + 8$ is decreasing?

[Question ID = 5776]

1. 8

[Option ID = 23098]

2. 6

[Option ID = 23099]

3. 4

[Option ID = 23100]

4. 2

[Option ID = 23101]

Correct Answer :-

- 6

[Option ID = 23099]

- 36) Let $f: [a, b] \rightarrow \mathbb{R}$ be a monotonic function. Consider the following statements:

- a. The function f obeys the maximum principle
b. The function f is Riemann integrable on $[a, b]$

Which of the above statement(s) is(are) true?

[Question ID = 5777]

1. Only (a)

[Option ID = 23102]

2. Only (b)

[Option ID = 23103]

3. Both (a) and (b)

[Option ID = 23104]

4. Neither (a) nor (b)

[Option ID = 23105]

Correct Answer :-

- Both (a) and (b)

[Option ID = 23104]

- 37) Consider the following:

- a. $\langle (a, b), (c, d) \rangle = ac - bd, (a, b), (c, d) \in \mathbb{R}^2$
b. $\langle f(x), g(x) \rangle = \int_0^1 f'(x)g(x) dx$, where $f(x), g(x)$ are polynomials over \mathbb{R}

Which of the above is(are) an inner product?

[Question ID = 5778]

1. Neither (a) nor (b)

[Option ID = 23106]

2. Both (a) and (b)

[Option ID = 23107]

3. Only (a)

[Option ID = 23108]

4. Only (b)



[Option ID = 23106]

38) Let $T = \begin{pmatrix} 1 & 0 & 2 \\ 0 & 1 & 1 \\ 0 & 0 & 2 \end{pmatrix}$. Then $T^3 + 4T^2 + 5T - 2I$ is equal to

[Question ID = 5779]

1. $10T + 4I$

[Option ID = 23110]

2. $10T - 4I$

[Option ID = 23111]

3. $-10T + 4I$

[Option ID = 23112]

4. $-10T - 4I$

[Option ID = 23113]

Correct Answer :-

• $10T - 4I$

[Option ID = 23111]

39) Let V be an infinite dimensional vector space over a field F .

Consider the following statements:

- Any one-one linear transformation from V to itself is onto
- Any onto linear transformation from V to itself must be one-one

Which of the above statements is (are) correct?

[Question ID = 5780]

1. Both (a) and (b)

[Option ID = 23114]

2. Only (a)

[Option ID = 23115]

3. Only (b)

[Option ID = 23116]

4. Neither (a) nor (b)

[Option ID = 23117]

Correct Answer :-

• Neither (a) nor (b)

[Option ID = 23117]

40) Let $P_n(\mathbb{R})$ be the set of all polynomials over \mathbb{R} of degree at most n . Let $T: P_n(\mathbb{R}) \rightarrow P_{n+1}(\mathbb{R})$ be given by $T(f(x)) = xf(x)$. Then

[Question ID = 5781]

1. T is one-one and onto linear transformation

[Option ID = 23118]

2. T is an onto function but neither a linear transformation nor one-one

[Option ID = 23119]

3. T is not onto but a one-one linear transformation

[Option ID = 23120]

4. T is one-one but neither a linear transformation nor onto

[Option ID = 23121]

Correct Answer :-

• T is not onto but a one-one linear transformation

[Option ID = 23120]



[Question ID = 5782]

1. $a - 6$

[Option ID = 23122]

2. $a - 4$

[Option ID = 23123]

3. $4 - a$

[Option ID = 23124]

4. $6 - a$

[Option ID = 23125]

Correct Answer :-

• $4 - a$

[Option ID = 23124]

42) Let G be a group of even order. Suppose that exactly half of G consists of elements of order 2 and the rest forms a subgroup H of G . Which of the following statements is incorrect?

[Question ID = 5783]

1. H is a normal subgroup of G

[Option ID = 23126]

2. Order of H is even

[Option ID = 23127]

3. H is abelian

[Option ID = 23128]

4. $|G:H| = 2$

[Option ID = 23129]

Correct Answer :-

• Order of H is even

[Option ID = 23127]

43) Let G and K be finite groups such that $|G| = 21$ and $|K| = 49$. Suppose G does not have a normal subgroup of order 3. Let L be the set of all group homomorphism from G to K . Then the number of elements in L is

[Question ID = 5784]

1. 1

[Option ID = 23130]

2. 3

[Option ID = 23131]

3. 5

[Option ID = 23132]

4. 7

[Option ID = 23133]

Correct Answer :-

• 1

[Option ID = 23130]

44) Let G be a finite group of $a \in G$ has exactly two conjugates. Suppose that $C(a) = \{x^{-1}ax | x \in G\}$ and $N(a) = \{x \in G | ax = xa\}$.

Which of the following statements is incorrect?

[Question ID = 5785]

1. The number of elements in $C(a)$ is a prime number

[Option ID = 23134]

2. G is a simple group

[Option ID = 23135]



$N(a)$ is a normal subgroup of G

[Option ID = 23137]

Correct Answer :-

- G is a simple group

[Option ID = 23135]

45) Let G be a finite group of order 385. Let H, K and L be p -Sylow subgroups of G for $p = 5, 7$ and 11 , respectively. Which of the following statements is incorrect?

[Question ID = 5786]

- K is a normal subgroup of G

[Option ID = 23138]

- L is normal subgroup of G

[Option ID = 23139]

- HK is a non-abelian subgroup of G

[Option ID = 23140]

- $G = HKL$

[Option ID = 23141]

Correct Answer :-

- HK is a non-abelian subgroup of G

[Option ID = 23140]

46) The remainder when 2020^{2020} is divided by 12 is

[Question ID = 5787]

- 0 [Option ID = 23142]

- 2 [Option ID = 23143]

- 4 [Option ID = 23144]

- 8 [Option ID = 23145]

Correct Answer :-

- 4 [Option ID = 23144]

47) The smallest integer $a > 2$ such that $2|a, 3|(a+1), 4|(a+2), 5|(a+3)$ and $6|(a+4)$ is

[Question ID = 5788]

- 14

[Option ID = 23146]

- 56

[Option ID = 23147]

- 122

[Option ID = 23148]

- 62

[Option ID = 23149]

Correct Answer :-

- 62

[Option ID = 23149]

48) Let $R = \left\{ \begin{pmatrix} a & b \\ b & a \end{pmatrix} \mid a, b \in \mathbb{Z} \right\}$ be a ring and $f: R \rightarrow \mathbb{Z}$ be given by $\phi \left(\begin{pmatrix} a & b \\ b & a \end{pmatrix} \right) = a - b$. Which of the following statements is incorrect?

[Question ID = 5789]

- ϕ is a ring homomorphism

[Option ID = 23150]

- $\ker \phi$ is a prime ideal but not maximal

[Option ID = 23151]

- $\ker \phi$ is maximal ideal



Correct Answer :-

- $\ker \phi$ is maximal ideal

[Option ID = 23152]

49) Consider the following statements

- A polynomial is irreducible over a field F if it has no zeros in F
- Let $f(x) \in \mathbb{Z}[x]$. If $f(x)$ is reducible over \mathbb{Q} , then it is reducible over \mathbb{Z}
- For any prime p , the polynomial $x^{p-1} + x^{p-2} + \dots + x + 1$ is irreducible over \mathbb{Q}

Which of the above statements is (are) correct?

[Question ID = 5790]

- Only (a) and (b)

[Option ID = 23154]

- Only (a) and (c)

[Option ID = 23155]

- Only (b) and (c)

[Option ID = 23156]

- All of (a), (b) and (c)

[Option ID = 23157]

Correct Answer :-

- Only (b) and (c)

[Option ID = 23156]

50) Which of the following is a Euclidean domain?

[Question ID = 5791]

- $\mathbb{Q}[x]/\langle x^3 - 2 \rangle$

[Option ID = 23158]

- $\mathbb{Z}[x]$

[Option ID = 23159]

- $\mathbb{Q}[x, y]$

[Option ID = 23160]

- None of these

[Option ID = 23161]

Correct Answer :-

- $\mathbb{Q}[x]/\langle x^3 - 2 \rangle$

[Option ID = 23158]