



USN

**17MAT41** 

# Fourth Semester B.E. Degree Examination, Dec.2019/Jan.2020 Engineering Mathematics \_ IV

Time: 3 hrs. Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

### Module-1

- a. From Taylor's series method, find y(0.1), considering upto fourth degree term if y(x) satisfying the equation  $dy = x y^2$ , y(0) = 1. (06 Marks)
  - b. Using Runge-Kutta method of fourth order  $\frac{dY}{dx} + y = 2x$  at x = 1.1 given that y = 3 at x = 1 initially. (07 Marks)
  - c. If dx = 2ex y, y(0) = 2, y(0.1) = 2.010, y(0.2) = 2.040 and y(0.3) = 2.090, find y(0.4) correct upto four decimal places by using Milne's predictor-corrector formula. (07 Marks)

# OR

- 2 a. Using modified Euler's method find y at x = 0.2 given  $\frac{d}{dx} = 3x + \frac{1}{2}y$  with y(0) = 1 taking h = 0.1.
  - h = 0.1. b. Given  $\frac{dy}{dx}$  + y + zy<sup>2</sup> =0 and y(0) = 1, y(0.1) = 0.9008, y(0.2) = 0.8066, y(0.3) = 0.722. Evaluate y(0.4) by Adams-Bashforth method. (07 Marks)
  - c. Using Runge-Kutta method of fourth order, find y(0.2) for the equation dx y-x y+x, y(0) = 1 taking h = 0.2. (07 Marks)

### Module-2

**3 a.** Apply Milne's method to compute y(0.8) given that  $\frac{d^2y}{dx^2} = 1 - 2y \frac{1}{dx}$  and the following table of initial values.

X	0	0.2	0.4	0.6
у	0	0.02	0.0795	0.1762
у'	0	0.1996	0.3937	0.5689

(06 Marks)

- b. Express  $f(x) = x^4 + 3x^3 x^2 + 5x 2$  in terms of Legendre polynomials.
- c. Obtain the series solution of Bessel's differential equation  $x^2y'' + xy' + (x + n)y = 0$  leading to .1,,(x). (07 Marks)



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OR

4 a. Given y'' - xy' - y = 0 with the initial conditions y(0) = 1, y'(0) = 0, compute y(0.2) y'(0.2) using fourth order Runge-Kutta method. (06 Marks)

b. Prove 
$$J_{-Iii}(k) = \frac{2}{1 - 2} \cos x$$
.

(07 Marks)

c. Prove the Rodfigues formula  $P(x) = \frac{1}{2" \text{ n! dx"}} (x^2 - 1)^{"}$  (07 Marks)

# Module\_3

5 a. Derive Cauchy-Riemann equations in Cartesian form.

(06 Marks)

b. Discuss the transformation  $w = z^{-1}$ .

(07 Marks)

c. By using Cauchy's residue theorem, evaluate

(z+1)(z+2) dz if C is the circle Izi = 3.

(07 Marks)

OR

6 a. Prove that 
$$\begin{cases} a \cdot - x \\ + x \cdot ay^e \end{cases}$$
 If  $(z)|^2 = 41f^2(z)1^2$ 

(06 Marks)

b. State and prove Cauchy's integral formula.

(07 Marks)

c. Find the bilinear transformation which maps z = 00, i, 0 into w = -1, -i, 1.

(07 Marks)

## Module\_4

7 a. Find the mean and standard of Poisson distribution.

(06 Marks)

- b. In an examination 7% of students score less than 35 marks and 89% of the students score less than 60 marks. Find the mean and standard deviation if the marks are normally distributed given A(I.2263) = 0.39 and A(1.4757) = 0.43 (07 Marks)
- c. The joint probability distributio

$\mathbf{V}\setminus$	-2	-1	4			
1	0.1	0.2	0	0.3		
2	0.2	0.1	0.1	0		

Determine:

- i) Marginal distribution of X and Y
- ii) Covariance of X and Y
- iii) Correlation of X and Y

(07 Marks)

## OR

**8 a.** A random variable X has the following robability function:

X	0	1	2	3	4	5	6	7	
P(x)	0	K	2k	2k	3k	$K^2$	$2k^2$	$7k^2+k$	

Find K and evaluate P(x 6) P(3 < x 6).

(06 Marks)

- b. The probability that a pen manufactured by a factory be defective is 1/10. If 12 such pens are manufactured, what is the probability that
  - i) Exactly 2 are defective
  - ii) Atleast two are defective
  - iii) None of them are defective.

(07 Marks)

- c. The length of telephone conversation in a booth has been exponential distribution and found on an average to be 5 minutes. Find the probability that a random call made
  - i) Ends in less than 5 minutes
  - ii) Between 5 and 10 minutes irstRanker.com



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### Module-5

- a. A die is thrown 9000 times and a throw of 3 or 4 was observed 3240 times. Show that the dia cannot be regarded as an unbiased die. (06 Marks)
  - b. A group of 10 boys fed on diet A and another group of 8 boys fed on a different disk B for a period of 6 months recorded the following increase in weight (lbs):

Diet A:	5	6	8	1	12	4	3	9	6	10
Diet B:	2	3	6	8	10	1	2	8		

Test whether diets A aid B differ significantly t.05 = 2.12 at 16d1

(07 Marks)

c. Find the unique fixed probability vector for the regular stochastic matrix 0 1 0

OR

$$0 \quad 1 \quad 0$$

$$A = \frac{1}{6} \frac{1}{2} \frac{1}{3}$$

$$0 \quad \frac{2}{3} \quad \frac{1}{3}$$
(07 Marks)

a. Define the terms:

Null hypothesis
Type-I and Type-II error

iii) Confidence limits

**10** 

i)

(06 Marks)

h. The t.p.m. of a Markov chain is given by  $P = \begin{bmatrix} 1/2 & 0 & 1/2 \\ 1 & 0 & 0 \\ 1/4 & 1/2 & 1/4 \end{bmatrix}$ .

. Find the fined probabilities

1/4 1/2 1/4 vector.

(07 Marks)

c. Two boys B1 and B2 and two girls G1 and G2 are throwing ball from one to another. Each boy throws the ball to the Other boy with probability 1/2 and to each girl with probability 1/4. On the other hand each girl throws the ball to each boy with probability 1/2 and never to the other girl. In the long run how often does each receive the ball? (07 Marks)