

OR

- 4 a. Compute the first two harmonics of the Fourier Series of $f(x)$ given the following table :

x°	0	60°	120°	180°	240°	300°
y	7.9	7.2	3.6	0.5	0.9	6.8

(08 Marks)

- b. Find the half range size series of e^x in the interval $0 < x$

(06 Marks)

- c. Obtain the Fourier series of $f(x) = \frac{\pi c}{12} - \frac{x}{4}$ valid in the interval $(-t, n)$

(06 Marks)

Module-3

- 5 a. Find the Infinite Fourier transform of e^{-x}

(07 Marks)

- b. Find the Fourier cosine transform of $f(x) = e^{-2x} + 4e^{-3x}$.

(06 Marks)

- c. Solve $u_{xx} - 3u_{x_1 x_2} + 2u_{x_2} = 3$, given $u_{x_1} = u_{x_2} = 0$.

(07 Marks)

OR

11 for Ix a

- 6 a. If $f(x) = \begin{cases} 1 & \text{for } |x| \leq a \\ 0 & \text{for } |x| > a \end{cases}$, find the infinite transform of $f(x)$ and hence evaluate $\int_0^\infty dx$.

(07 Marks, _)

- b. Obtain the Z-transform of $\cosh nx$ and $\sinh nx$.

(06 Marks)

- c. Find the inverse Z-transform of $\frac{4z^2 - 2z}{z^2 - 5z + 8z - 4}$

(07 Marks)

Module-4

- 7 a. Solve $\frac{dy}{dx} = e^x - y$, $y(0) = 2$ using Taylor's Series method upto 4th degree terms and find the value of $y(1.1)$.

(07 Marks)

- b. Use Runge-Kutta method of fourth order to solve $\frac{dy}{dx} + y = 2x$ at $x = 1.1$ given $y(1) = 3$ (Take h 0.1)

(06 Marks)

- c. Apply Milne's predictor-corrector formulae to compute $y(0.4)$ given $\frac{dy}{dx} = 2ex - y$, with $y(0) = 1$.

(07 Marks)

x	0	0.1	0.2	0.3
y	2.4	2.473	3.129	4.059

OR

- 8 a. Given $\frac{dy}{dx} = x + \sin y$ $y(0) = 1$. Compute $y(0.4)$ with $h = 0.2$ using Euler's modified method.

(07 Marks)

- b. Apply Runge-Kutta fourth order method, to find $y(0.1)$ with $h = 0.1$ given $\frac{dy}{dx} + y + xy^2 = 0$; $y(0) = 1$.

(06 Marks)

- c. Using Adams-Basforth method, find $y(4.4)$ given $5x \frac{dy}{dx} = 2$ with

x	4	4.1	4.2	4.3
y	1	1.0049	1.0097	1.0143

Module-5

- 9 a. Solve by Runge Kutta method $\frac{d^2y}{dx^2} = x \frac{dy}{dx} - y$, for $x = 0.2$ correct 4 decimal places, using initial conditions $y(0) = 1$, $y'(0) = 0$, $h = 0.2$. (07 Marks)
- b. Derive Euler's equation in the standard $\frac{d}{dy} \frac{df}{dx} = 0$. (06 Marks)
- c. Find the extremal of the functional, $+ (y')^2 + 2ye^{dx}$ (07 Marks)

OR

- 10 a. Apply Milne's predictor corrector method to compute $\frac{d}{dx} y$ and $\frac{dy}{dx}$ and the following table of initial values:
- | x | 0 | 0.1 | 0.2 | 0.3 |
|----|---|--------|--------|--------|
| y | 1 | 1.1103 | 1.2427 | 1.3990 |
| y' | 1 | 1.2103 | 1.4427 | 1.6990 |
- (07 Marks)
- b. Find the extremal for the functional. $- \int_0^2 2y \sin x dx ; y(0) = 1, y(2) = 1$. (06 Marks)
- c. Prove that geodesics of a plane surface are straight lines. (07 Marks)