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MCA I Semester Regular & Supplementary February 2014 Examinations MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE

(For 2009, 2010, 2011, 2012 & 2013 admitted batches only)

Time: 3 hours

Max. Marks: 60

Answer any FIVE questions All questions carry equal marks

- 1 (a) Obtain PCNF of $(\neg P \rightarrow R) \land (Q \rightleftharpoons P)$.
 - (b) State the laws of algebra of propositions.
- 2 (a) Check whether the following arguments are valid or not.
 No professors are ignored
 All ignorant people are vain
 Hence, no professors are vain.
 - (b) What is predicate logic? Explain free and bound variables with example.
- 3 (a) Prove that "A relation on a set A is reflexive if and only if the inverse relation R^{-1} is reflexive".
 - (b) What is a lattice? Explain the properties of lattice.
- 4 (a) Prove that the intersection of two submonoids of a monoid is a monoid.
 - (b) State and explain the four axioms of a group. With an example, explain about a group.
- 5 (a) How many integers between 10⁵ and 10⁶
 (i) Have no digits other than 2, 5, 8?
 (ii) Have no digits other than 0, 2, 5 or 8?
 - (b) Explain the principle of inclusion-exclusion for n sets.
- 6 (a) Solve the recurrence relation $a_n = na_{n-1}$ for $n \ge 1$, given that $a_0 = 1$.
 - (b) Write the working procedure for solving non-homogeneous finite order relations.
- 7 (a) Prove that the sum of degrees of the regions of a planar graph G is equal to twice the number of edges in G.
 - (b) Define a graph. Explain various types of graphs with example.
- 8 (a) Find the chromatic number of the graph.



(b) Prove the following:

(i) A path with n vertices is of length n-1.

(ii) If a cycle has 'n' vertices, it has 'n' edges.