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В.Tech.

(SEM. I) THEORY EXAMINATION, 2015-16

ENGINEERING MATHEMATICS-I

[Time:3 hours]

[Total Marks:100]

Section-A

Q.1 Attempt all parts. All parts carry equal marks. Write answer of each part in shorts. ($10 \times 2=20$)

(a) If $Y = e^{\sin^{-1}x}$, find the value of $(1-x^2)y_2 - xy_1 - a^2y$.

(b) If
$$V = (x^2 + y^2 + z^2)^{-1/2}$$
, then find $x \frac{\partial v}{\partial x} + y \frac{\partial v}{\partial y} + z \frac{\partial z}{\partial x}$.

(c) If f(x,y,z,w)=0, then find $\frac{\partial x}{\partial y} \times \frac{\partial y}{\partial z} \times \frac{\partial z}{\partial w} \times \frac{\partial w}{\partial x}$.

(d) If $pv^2 = k$ and the relative errors in p and v are respectively 0.05 and 0.025, show that the error in k is 10%.

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- (e) Examine whether the vectors $x_1 = [3,1,1], x_2 = [2,0,-1]$ 1], $x_3 = [4,2,1]$ are linearly independent.
- (f) If $A = \begin{bmatrix} -1 & 0 & 0 \\ 2 & -3 & 0 \\ 1 & 4 & -2 \end{bmatrix}$, find the eigen values of A².
- (g) Evaluate $\iint \frac{dxdy}{\sqrt{1-x^2}\sqrt{1-y^2}}$
- (h) Find the value of integral $\int_0^\infty e^{-ax} x^{n-1} dx$.
- (i) Find the curl of $\vec{F} = xy\hat{i} + y^2\hat{j} + xz\hat{k}$ at (-2,4,1)
- (j) State Stoke's theorem.

Section-B

Attempt any five Questions from this section:

(5x10=50)

Q.2. If $\cos^{-1} x = \log(y)^{1/m}$, then show $(1-x^2)y_{n+2}$ Y_n when x=0. $(2n+1)xy_{m-1}-(n^2+m^2)y_n=0$ and hence Calculate

the expression is real.

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- Q.3 If u,v,w are the roots of the equation $(\lambda-x)^3+(\lambda-y)^3+(\lambda-z)^3=0$ in λ find $\frac{\partial(u,v,w)}{\partial(x,y,z)}$
- Q.4 Using the Lagrange's method find the dimension of is given when (a) box is open at the top (b) box is closed. rectangular box of maximum capacity whose surface area
- Q.5 Find the characteristic equation of the matrix

 $A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$ and verify Cayley Hamilton theorem.

Also evaluate $A^6 - 6A^5 + 9A^4 - 2A^3 - 12A^2 + 23A - 9I$.

Q.6 Prove that $\iiint \frac{dx \, dy \, dz}{\sqrt{(1-x^2-y^2-z^2)}} = \frac{n^2}{8}$, the integral being Q.7 Verify the Green's theorem to evaluate the line integral extended to all positive values of the variables for which region bounded by y = x and $y = x^2$. $\int_{C} (2y^2 dx + 3x dy)$, where C is the boundary of the closed

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$$x+y+z=6$$

 $x+2y+3z=10$,

x + 2y + az = b

- (ii) A unique solution
- (iii) Infinite no of solutions.

Q.9 Find the mass of a solid
$$\left(\frac{x}{ab}\right)^p + \left(\frac{y}{b}\right)^q + \left(\frac{z}{c}\right)^r = 1$$
, the

density at any point being
$$p = kx^{l-1}y^{m-1}z^{n-1}$$
 where x, y, z are all positive.

It being
$$p = kx^{l-1}y^{m-1}z^{n-1}$$
 where x, y, z b)

Section-C

- <u>င</u> Prove that, for every field \overline{V} ; div curl $\overline{V} = 0$.
- Q.12 a) Evaluate $\iiint_R (x+y+z)dx dy dz$ where

Q10. a) If u = f(r) where $r^2 = x^2 + y^2$, show that

 $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f''(r) + \frac{1}{r} f'(r).$

Attempt any two questions from this section: $(2 \times 15 = 30)$

 $R: 0 \le x \le 1; 1 \le y \le 2; 2 \le z \le 3$

b) Trace the curve
$$y^2(2a-x)=x^3$$
.

b) Change the order of Integration in
$$l = \int_0^1 \int_{x^2}^{2-x} xy \, dxdy \text{ and hence evalute.}$$

- Find the rank of the matrix by reducing to normal
- form. $\begin{pmatrix} 3 & 2 & -1 \\ 4 & 2 & 6 \\ 7 & 4 & 5 \end{pmatrix}$
- Q.11 a) A fluid motion is potential. $\overline{v} = (y+z) \hat{i} + (z+x)\hat{j} + (x+y) \hat{k}$. Show that the motion is irrotational and hence find the velocity given by
- If x+y+z=u, y+z=uv, z=uvw then find $\frac{\partial(x,y,z)}{\partial(u,v,w)}.$
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 $Z = \frac{x^{\frac{1}{3}} + y^{\frac{1}{3}}}{x^{\frac{1}{2}} + y^{\frac{1}{2}}}.$

c) Verify Euler's theorem for the function

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