

rinted Pages: 5	175	EAS-103
(Following Paper I	D and Roll No. Answer Boo	n your
aper 1D :199123	Roll No.	
	B.Tech.	

(SEM. I) THEORY EXAMINATION, 2015-16 MATHEMATICS-I

[Time:3 hours]

[Total Marks:100]

Section-A

- Attempt all parts. All parts carry equal marks. Write answer of each part in shorts. (10×2=20)
 - (a) If $u = \log(x^2/y)$ then value of $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = ?$.
 - (b) If $z = xyf\left(\frac{x}{y}\right)$ show that $x\frac{\partial z}{\partial x} + y\frac{\partial z}{\partial y} = 2z$.
 - (c) Apply Taylor's series find expansion of $f(x, y) = x^3 + xy^2$ about point (2,1), upto first degree term.
 - (d) If x = u v, $y = u^2 v^2$, find the value of $\frac{\partial(u, v)}{\partial(x, y)}$.

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- (j) Evaluate $\frac{\Gamma(8/3)}{\Gamma(2/3)}$ (i) If $\phi(x, y, z) = x^2y + y^2x + z^2$ find $\nabla \phi$ at the point (h) Evaluate $\int_0^1 \int_1^2 xyz \, dx \, dy \, dz$ Э (e) Find all the asymptotes of the curve Find the inverse of the matrix by using elementary row operations. A = $xy^2 = 4a^2(2a - x).$, find the eigen values of A2.
- 2. If $x = \sin \left\{ \frac{1}{m} \sin^{-1} y \right\}$ find the value of y_n at x = 0. 2

EAS-103

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Note: Attempt any five Questions from this section:

(5x10=50)

7.

any point is kxyz.

The plane $\frac{x}{-} + \frac{y}{-} + \frac{z}{-} = 1$ meets the axes in A, B, and C. Find the Eigen values and corresponding Eigen vectors If r is the distance of a point on Conic If u, v, w are the roots of the equation that the stationary values of r are given by the equation $(\lambda - x)^3 + (\lambda - y)^3 + (\lambda - z)^3 = 0$ in λ find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$ $ax^2 + by^2 + cz^2 = 1$, bx + my + nz = 0 from origin, then

Change the order of Integration in tetrahedron OABC. Also find its mass if the density at Apply Dirichlet's integral to find the volume of the $I = \int_0^1 \int_{x^2}^{2-x} xy \, dx dy \text{ and hence evaluate the same.}$ www.FirstRanke.

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Verify gauss's divergence theorem for the function

Ξ a)

Define Beta and Gamma function and Evalaute

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 $x^2 = 4ay$.

Find the area between the parabola $y^2 = 4ax$ and

c

is zero.

Examine the following vectors for linearly

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possible, $X_1 = (1,1-1,1)$, $X_2 = (1,-1,2-1)$ dependent and find the relation between them, if

 $X_3 = (3,1,0,1).$

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EAS-103

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EAS-103/8600

10. a) Attempt any two questions from this section: $(2\times15=30)$ ভ Show that the Vector field $\vec{F} = \frac{r}{|r|^3}$ is irrotational as well as solenoidal. Find the scalar potential. x = 0, x = 1, y = 0, y = 1 and z = 1, z = 1. $\vec{F} = x^2 \hat{i} + z \hat{j} + yz \hat{k}$, taken over the cube bounded by Expand $e^{ax} \cos by$ in powers of the powers of Determine the constant a and b such that the curl of vector. x and y as terms of third degree. $\overline{A} = (2xy + 3xz) \hat{i} + (x^2 + axz - 4z^2)\hat{j} - (3xy + byz)\hat{k}$ Section-C

c) If $y_1 = \frac{x_2 x_3}{x_1}$, $y_2 = \frac{x_3 x_1}{x_2}$, $y_3 = \frac{x_1 x_2}{x_3}$ find $\frac{\partial (y_1, y_2, y_3)}{\partial (x_1, x_2, x_3)}$

12. a) ೦ ভ Evaluate $\int_0^{\infty} (a^n - x^n)^{1/n}$ Reduce the matrix in to normal form and hence find its rank -2 4 y-x z-x1 2 1 0 1 0 2 -8 3 0 show

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