

Printed Pages : 5

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NCS-302

(Following Paper ID and Roll No. to be filled in your Answer Book)

Paper ID : 110302

Roll No.

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B.Tech.

(SEM. III) THEORY EXAMINATION. 2015-16

DISCRETE STRUCTURES AND GRAPH THEORY

[Time : 3 hours]

[Total Marks : 100]

Section-A

1. Attempt **all** parts. All parts carry **equal** marks. Write answers of each section in short. (10x2=20)
- (a) Define multiset and power set. Determine the power set $A = \{1, 2\}$.
- (b) Show that $(((pq) \Rightarrow r) (\neg p))) \Rightarrow (q=r)$ is tautology or contradiction.
- (c) State and prove pigeon hole principle.
- (d) Show that if set A has 3 elements, then we can have 26 symmetric relation on A.
- (e) Prove that $(P \vee Q) \rightarrow (P \wedge Q)$ is logically equivalent to $P \leftrightarrow Q$.

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(1)

P.T.O.

- (f) How many 4 digit numbers can be formed by using the digits 2, 4, 6, 8 when repetition of digits is allowed.
- (g) The converse of a statements is: **If a steel rod is stretched, then it has been heated.** Write the inverse of the statement.
- (h) If **a** and **b** are any two elements of group **G** then prove $(ab)^{-1} = (b^{-1}a^{-1})$.
- (i) If $f: A \rightarrow B$ is one-one onto mapping, then prove that $f^{-1}: B \rightarrow A$ will be one-one onto mapping.
- (j) Write the following in DNF $(x+y)(x'+y')$.

Section-B

Attempt any five questions.

(10×5=50)

2. If D_n define the set of all positive odd integers, i.e. $D_n = \{1, 3, 5, \dots\}$, then prove with the help of mathematical induction $P(n): 1+3n$ is divisible by 4.
3. Solve the recurrence relation using generating function:
 $an-7an-1+10n-2=0$ with $a_0=3, a_1=3$.

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4. Express the following statements using quantifiers and logical connectives.
- (a) Mathematics book that is published in India has a blue cover.
- (b) All animals are mortal. All human being are animal. Therefore, all human being are mortal.
- (c) There exists a mathematics book with a cover that is not blue.
- (d) He eats crackers only if he drinks milk.
- (e) There are mathematics books that are published outside India.
- (f) Not all books have bibliographies.
5. Draw the Hasse diagram of $\{p(a, b, c), \leq\}$. (Note: ' \leq ' stands for subset). Find greatest element, least element, minimal element and maximal element.
6. Simplify the following boolean expressions using k map:
- a) $Y = ((AB)^x + A^x + AB)^x$
- b) $A^x B^x C^x D^x + A^x B^x C^x D + A^x B^x C D + A^x B^x C D^x = A^x B^x$

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P.T.O

7. Let G be the set of all non-zero real number and let $a * b = ab/2$. Show that $(G, *)$ be an abelian group.
8. The following relation on $A = \{1, 2, 3, 4\}$. Determine whether the following:
- a) $R = \{(1, 3), (3, 1), (1, 1), (1, 2), (3, 3), (4, 4)\}$,
b) $R = AXA$
9. If the permutation of the elements of $\{1, 2, 3, 4, 5\}$ are given by $a = (1\ 2\ 3)(4\ 5)$, $b = (1)(2)(3)(4\ 5)$, $c = (1\ 5\ 2\ 4)(3)$. Find the value of x , if $ax = b$. And also prove that the set $Z_4 = \{0, 1, 2, 3\}$ is a commutative ring with respect to the binary modulo operation $+4$ and $*4$.

Section-C

Attempt any two questions.

(2×15=30)

10. Let L be a bounded distributed lattice, prove if a complement exists, it is unique. Is D_{12} a complemented lattice? Draw the Hasse diagram of $[P(a, b, c), \leq]$. (Note: \leq stands for subset). Find greatest element, least element, minimal element and maximal element.

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11. Determine whether each of these functions is a bijection from R to R .
- (a) $f(x) = x^2 + 1$
(b) $f(x) = x^3$
(c) $f(x) = (x^2 + 1)/(x^2 + 2)$
12. a) Prove that inverse of each element in a group is unique.
b) Show that $G = \{1, 2, 4, 5, 7, 8, X9\}$ is cyclic. How many generators are there? What are they?

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