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B. TECH. (SEM III) THEORY EXAMINATION 2018-19 DISCRETE STRUCTURES AND THEORY OF LOGIC

Time: 3 Hours

Total Marks: 70

Note: 1. Attempt all Sections: If require any missing data; then choose suitably 2. Any special paper specific instruction.

SECTION A

Attempt all questions in brief.

2 x 7 = 14

- Find the power set of each of these sets, where a and b are distinct elements i) {a} ii) {a, b} iii) { \emptyset , { \emptyset }} iv) {a, {a}} a.
- Define Ring and Field.
- Draw the Hasse diagram for D₁₀
- Draw the Fasse angram for Dis.
 What are the contrapositive, converse, and the inverse of the conditional statement. The home team wins whenever it is raining?
 How many bit strangs of length eight either stagewish a "1" bit or end with the two bits "00"?
 Define Injective, surjective and bijective function.

- Show that \neg (p \lor q) and \neg p \land \neg q are logically equivalent.

SECTION B

Attempt any three of the following: 2.

7x3=21

- A total of 1232 student have taken a course in Spanish, 879 have taken a course in French, and 184 have taken a course in Russian. Further, 103 have taken courses in both Spanish and French, 23 have taken courses in both Spanish and Russian, and 14 have taken courses in both Spanish Russian If 2002 students have taken at least one of Spanish. French, and Russian If 2002 students have taken at least one of Spanish. French, and Russian, how many students have taken a course in all three languages?
- (i) Let H be a subgroup of a finite group G. Prove that order of H is a divisor of order of G.
 (ii) Prove that every group of printe order is cyclic.
- Define a lattice. For any a,b,c,d in a lattice (A,\leq) if $a\leq b$ and $c\leq d$ then show that $a\vee c\leq b\vee d$ and $a\wedge c\leq b\wedge d$.
- Show that $((p\vee q)\wedge^{>}(\sim p\wedge(\sim q\vee \neg r)))\vee(\neg p\wedge \neg q)\vee(\neg p\vee r)$ is a tautology without using truth hable.
- Define a Binary Tree. A binary tree has 11 nodes. It's in order and preorder

traversals node sequences are: Preorder: ABDHIEJKCFG In-order: HDIBJEKAFCG Draw the tree.





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SECTION C

Attempt any one part of the following:

- (a) Prove that if n is a positive integer, then 133 divides $11^{n+1} + 12^{2n-1}$.
- (b) Let n be a positive integer and S a set of strings. Suppose that R_n is the relation on S such that s R_n t if and only if s = t, or both s and t have at least n characters and the first n characters of s and t are the same. That is, a string of fewer than n characters is related only to itself; a string s with at least n characters is related to a string t if and only if t has at least n characters and t begins with the n characters at the string of s. n characters at the start of s.

 What is the equivalence class of the string 0111 with respect to the equivalence relation R.

Attempt any one part of the following:

 $7 \times 1 = 7$

- (a) Let G = {1, -1, i, -i} with the binary operation multiplication be an algebraic structure, where $i = \sqrt{-1}$. Determine whether G is an Abelian or not.
- What is meant by a ring? Give examples of both commutative and noncommutative rings

- Attempt any one part of the following:

 7 x 1 7

 (a) Show that the inclusion relation (is a partial ordering on the power set of a set S. Draw the Hasse diagram for inclusion on the set P (S), where S (a, b, c, d). Also Determine whether (P (S), G) is a lattice.
- (b) Find the sum-of-puddlets and Product of sum expansion of the Boolean function $F\left(x,y,z\right)=(x+y)\,z^{\prime}$

Attempt any one part of the following:

- (a) What is a tautology, contradiction and contingency? Show that $(p \lor q) \land (\neg p \lor r) \rightarrow (q \lor r)$ is a tautology, contradiction or contingency.
- (b) Show that the premises "It is not sungly this afternoon and it is colder than yesterday," "We will go swimming only if it is sunny," "If we do not go swimming, then we will take a carbot trip," and "If we take a canoe trip, then we will be home by sunset" load to the conclusion "We will be home by

Attempt any one part of the following:

- (a) What are different ways to represent a graph. Define Euler circuit and Euler graph. Give necessary and sufficient conditions for Euler circuits and paths.
- Suppose that a valid codeword is an n-digit number in decimal notation containing an even number of 0's. Let a_n denote the number of valid codewords of length n satisfying the recurrence relation $a_n = 8a_{n-1} + 10^{n-1}$ and the initial condition $a_1 = 9$. Use generating functions to find an explicit formula for a_n .

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