

Printed Pages: 7

NAS-401/EAS-401

(Following Paper ID and Roll No. to be filled in your Answer Books)

Paper ID : 199419

Roll No.

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B. TECH.**Theory Examination (Semester-IV) 2015-16****ENGG MATHEMATICS-III****Time : 3 Hours****Max. Marks : 100****Section-A**

1. Attempt all questions of this section. Each question carry equal marks. (2×10 = 20)

- (a) Write the cauchy's Reimaun conditions in polar coordinates system.
- (b) Write the statement of generalized cauchy's integral formula for n^{th} derivative of an analytic function at the point $Z = Z_0$.
- (c) Find the Z – transform of $U_n = \{a^n\}$
- (d) Write the normal equations to fit a curve $y = ax^2 + b$ by least square method.

(1)

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- (e) If covariance between x and y variable is 10 and the variance of x and y are respectively 16 and 9, find the coefficient of correlation.

(f) The regression equations calculated from a given set of observations for two random variable are
 $x = -0.4y + 6.4$ and $y = -0.6x + 4.6$ calculate mean values of x and y .

(g) Write the Newton's Raphson iterative formula to find the value of \sqrt{N} .

(h) Find the missing data in the given table :

(i) If $f(n)$ is given in following table :
- | | | | | |
|--------|-----|-----|---|-----|
| x | 0 | 1 | 2 | 3 |
| $f(x)$ | 580 | 556 | – | 465 |
- | | | | |
|--------|---|-----|-----|
| x | 0 | 0.5 | 1 |
| $f(x)$ | 1 | 0.8 | 0.5 |
- then using trapezoidal rule, evaluate
 $\int_0^1 f(x)dx$
- (j) Find the third forward difference with the arguments 2, 4, 6, 8 of the function $f(x)=x^3-2x$
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(2)
- Section-B
2. Attempt any five questions from this section.

(10×5 = 50)
- (a) Find the Laurent series for the function
 $f(z)=\frac{7z^2+9z-18}{Z^3-9z}$, Z is complex variable
valid for the regions
(i) $0<|z|<3$ (ii) $|z|>3$

(b) Using calculus of residue, evaluate the following integral
 $\int_0^{\infty} \frac{dx}{(a^2+x^2)^2}$

(c) Find the inverse Fourier sine transform of $\frac{1}{x}e^{-ax}$

(d) Using least square method, fit a second degree polynomial from the following data :

x	0	1	2	3	4	5	6	7	8
y	12.0	10.5	10.0	8.0	7.0	8.0	7.5	8.5	9.0

Also estimate y at $x = 6.5$

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- (e) For the following data, calculate the finite differences and obtain the forward and backward difference polynomials. Also interpolate at $x = 0.25$ and $x = 0.35$

x	0.1	0.2	0.3	0.4	0.5
$f(x)$	1.40	1.56	1.76	2.00	2.28

- (f) Construct the divided difference table for the data.

x	0.5	1.5	3.0	5.0	6.5	8.0
$f(x)$	1.62	5.87	31.0	131.0	282.12	521.0

Hence find the interpolating polynomial and an approximation to the value of $f(z)$.

- (g) Solve the system of equations $AX=B$, where

$$A = \begin{bmatrix} 2 & 1 & 1 & -2 \\ 4 & 0 & 2 & 1 \\ 3 & 2 & 2 & 0 \\ 1 & 3 & 2 & -1 \end{bmatrix}, \quad B = \begin{bmatrix} -10 \\ 8 \\ 7 \\ -5 \end{bmatrix}$$

using the LU decomposition method. Take all the diagonal elements of L as 1.

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(4)

- (In) Solve the initial value problem

$$\frac{dy}{dx} = -2xy^2, \quad y(0) = 1$$

with $h = 0.1$ on the interval $[0, 0.3]$. Use the fourth order Runge-Kutta method.

Section-C

Note: Attempt any two questions from this section. Each question carry equal marks. (15×2=30)

3. (a) Show that for the function give as -

$$f(z) = \begin{cases} \frac{2xy(x+iy)}{x^2+y^2} & \text{if } z \neq 0 \\ 0 & \text{if } z = 0 \end{cases}$$

The C-R conditions are satisfied at origin but derivative of $f(z)$ at origin does not exist.

- (b) Verify that the function on $4(xy) = xy$ is harmonic and find its conjugate harmonic function. Express $u+iv$ as an analytic function $f(z)$.

$$u = x^2 - y^2 - y$$

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(5)

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(c) Find the Fourier transform of Block function $f(t)$ of height 1 and duration a defined by

$$f(t)=\begin{cases} 1 & \text{for } |t|\leq \frac{a}{2} \\ 0 & \text{otherwise} \end{cases}$$

4. (a) Using Z - tranform, solve the difference equation

$$u_{n+2}-4u_{n+1}+3u_n=5^n$$

with $u_0=u_1=1$

(b) The first four moments of a distribution about x = 4 are 1, 4, 10, 45. Comment on the skewness and Kurtosis of the distribution.

(c) For 10 observations on price (x) and supply (y) the following data were obtained

$$\Sigma x=130, \Sigma y=220, \Sigma x^2=2288$$

$$\Sigma x^2=5506 \text{ and } \Sigma_{xy}=3467$$

Obtain the two lines of regression.

5. (a) Find the root of the euqation $xe^x=3$ by regula talsi method correct up to two decimal places in the interval (1, 1.5).

(b) Prove the following identities :

(i) $\left(\frac{\Delta^2}{E}\right)\mu_x\neq \frac{\Delta^2\mu_x}{E\mu_x}$

(ii) $\left(\frac{\Delta^2}{E}\right)e^x\cdot \frac{E(e^x)}{\Delta^2e^x}=e^x$

(c) The velocity v of a particle at distance s from a point on its path is given by the following table :

s (m.)	0	10	20	30	40	50	60
v (m./s.)	47	58	64	65	61	52	38

Estimate the time taken to travel 60m. Using Simpson's one-third rule.