

Printed Pages: 02

Paper Id: 110257

Sub Code: RCS403

Roll No.

--	--	--	--	--	--	--	--	--	--

B TECH

(SEM-IV) THEORY EXAMINATION 2018-19
THEORY OF AUTOMATA AND FORMAL LANGUAGES

Time: 3 Hours

Total Marks: 70

Note: Attempt all Sections. If require any missing data; then choose suitably.

SECTION A

1. Attempt all questions in brief.

2 x 7 = 14

- For the given language $L_1 = \epsilon$, $L_2 = \{a\}$, $L_3 = \emptyset$. Compute $L_1 L_2^* \cup L_3^*$.
- Design a FA to accept the string that always ends with 101.
- Write regular expression for set of all strings such that number of a's divisible by 3 over $\Sigma = \{a, b\}$
- Construct the CFG for the Language $L = \{a^{2n}b^n \mid n \geq 3\}$.
- What do you mean by ϵ -Closure in FA?
- Explain Universal TM.
- Explain Two Stack PDA.

SECTION B

2. Attempt any three of the following:

7 x 3 = 21

- Construct a minimum state DFA from given FA

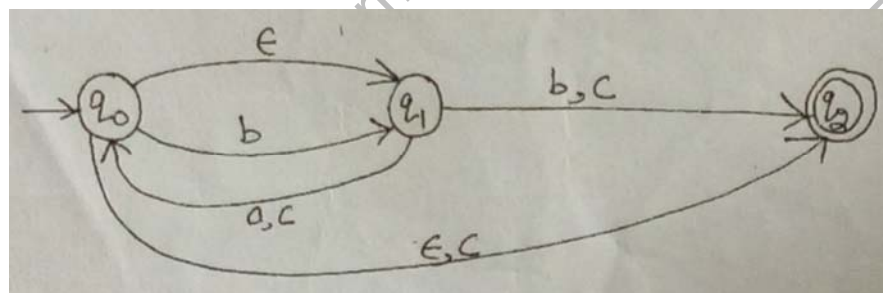


Fig. 1

- Find the regular expression corresponding to the finite automata given below:

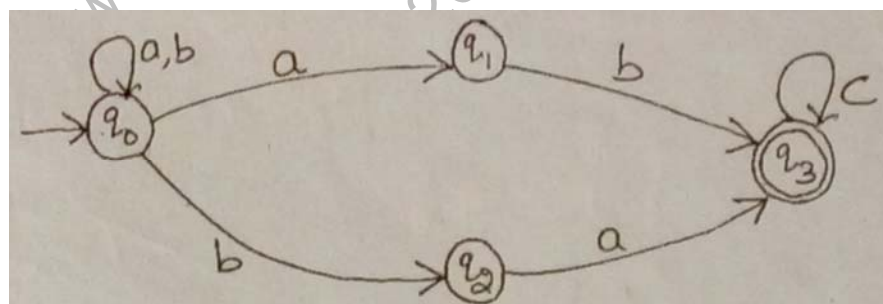


Fig. 2

P.T.O

- c. Convert the following CFG to its equivalent GNF:
 $S \rightarrow AA \mid a, A \rightarrow SS \mid b.$
- d. Design a PDA for the following language:
 $L = \{a^i b^j c^k \mid i = j \text{ or } j = k\}$
- e. Design a TM for the following language:
 $L = \{a^{n+2} b^n \mid n > 0\}$

SECTION C

3. Attempt any *one* part of the following: 7 x 1 = 7

- (a) Design FA for ternary number divisible by 5.
- (b) Explain Myhill-Nerode Theorem using suitable example.

4. Attempt any *one* part of the following: 7 x 1 = 7

- (a) Prove that the following Language $L = \{a^n b^n\}$ is not regular
- (b) Explain the Closure properties of regular expression.

5. Attempt any *one* part of the following: 7 x 1 = 7

- (a) Design the CFG for the following language:
 - i) $L = \{0^m 1^n \mid m \neq n \text{ \& } m, n \geq 1\}$
 - ii) $L = \{a^l b^m c^n \mid l + m = n \text{ \& } l, m \geq 1\}$
- (b) Prove that the following Language $L = \{a^n b^n c^n\}$ is not Context Free.

6. Attempt any *one* part of the following: 7 x 1 = 7

- (a) Design a PDA for the Language $L = \{WW^R \mid W = \{a, b\}^*\}$
- (b) Generate CFG for the given PDA M is defined as
 $M = (\{q_0, q_1\}, \{0, 1\}, \{x, z_0\}, \delta, q_0, z_0, q_1)$ where δ is given as follows:
 $\delta(q_0, 1, z_0) = (q_0, xz_0)$
 $\delta(q_0, 1, x) = (q_0, xx)$
 $\delta(q_0, 0, x) = (q_0, x)$
 $\delta(q_0, \epsilon, x) = (q_1, \epsilon)$
 $\delta(q_1, \epsilon, x) = (q_1, \epsilon)$
 $\delta(q_1, 0, x) = (q_1, xx)$
 $\delta(q_1, 0, z_0) = (q_1, \epsilon)$

7. Attempt any *one* part of the following: 7 x 1 = 7

- (a) Design a TM for the following language:
 $L = \{a^n b^n c^n \mid n \geq 1\}$
- (b) Write short note on:
 - i) Recursive Language and Recursively Enumerable Language.
 - ii) PCP problem and Modified PCP Problem