

B. TECH.

THEORY EXAMINATION (SEM-VI) 2016-17

DIGITAL SIGNAL PROCESSING

Time : 3 Hours

Max. Marks : 100

Note : Be precise in your answer. In case of numerical problem assume data wherever not provided.

SECTION – A

1. Attempt the following questions:

10 x 2 = 20

- Define digital signal processing.
- Draw the block diagram of digital signal processing.
- Explain the basic elements required for realization of digital system.
- Define linear convolution and its physical significance.
- What is the fundamental time period of the signal $x(t) = \sin 15\pi t$.
- Draw a transformation matrix of size 4x4 and explain the properties of twiddle factor.
- Differentiate between IIR and FIR filters
- Enumerate the Advantages of DSP over ASP.
- Write the expression for computation efficiency of an FFT.
- Calculate the DFT of the sequence $s(n) = \{1, 2, 1, 3\}$.

SECTION – B

2. Attempt any five of the following questions:

5 x 10 = 50

- Obtain the Parallel form realization for the transfer function $H(z)$ given below:

$$H(z) = \frac{2 + z^{-1} + \frac{1}{4}z^{-2}}{(1 + \frac{1}{2}z^{-1})(1 + z^{-1} + \frac{1}{2}z^{-2})}$$

- Calculate the DFT of $x(n) = \cos an$
- Derive and draw the flow graph for DIF FFT algorithm for $N=8$.
- Determine $H(z)$ using the impulse invariant technique for the analog system function

$$H(s) = \frac{1}{(s + 0.5)(s^2 + 0.5s + 2)}$$

- Determine $H(z)$ for a Butterworth filter satisfying the following constraints

$$\sqrt{0.5} \leq |H(e^{j\omega})| \leq 1 \quad 0 \leq \omega \leq \frac{\pi}{2}$$

$$|H(e^{j\omega})| \leq 0.2 \quad \frac{3\pi}{4} \leq \omega \leq \pi$$

with $T=1$ sec. Apply impulse invariant transformation.

- Given $x(n) = 2^n$ and $N=8$ find $X(K)$ using DIT FFT algorithm. Also calculate the computational reduction factor.
- Design a low-pass filter with the following desired frequency response

$$H_d(e^{j\omega}) = \begin{cases} e^{-j2\omega}, & -\frac{\pi}{4} \leq \omega \leq \frac{\pi}{4} \\ 0, & \frac{\pi}{4} < |\omega| < \pi \end{cases} \quad \text{and using window function}$$

$$w(n) = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{otherwise} \end{cases}$$

- (h) Convert the analog filter with system function $H(s) = \frac{s+0.1}{(s+0.1)^2 + 9}$ into digital filter

with a resonant frequency of $\omega_r = \frac{\pi}{4}$ of using bilinear transformation.

SECTION – C

Attempt any two of the following questions:

2 x 15 = 30

- 3 (i) Obtain the ladder structure for the system function $H(z)$ given below.

$$H(z) = \frac{2 + 8z^{-1} + 6z^{-2}}{1 + 8z^{-1} + 12z^{-2}}$$

- (ii) Compute the Circular convolution of two discrete time sequences $x_1(n) = \{1, 2, 1, 2\}$ and $x_2(n) = \{3, 2, 1, 4\}$

- 4 (a) Determine the 4-point discrete time sequence from its DFT $X(k) = \{4, 1-j, -2, 1+j\}$
 (b) Explain the following phenomenon: (i) Gibbs Oscillations, (ii) Frequency wrapping
- 5 (a) Derive the relation between DFT and Z-transform of a discrete time sequence $s(n)$.
 (b) Design a digital Chebyshev filter to satisfy the constraints

$$\begin{aligned} 0.707 \leq |H(e^{j\omega})| \leq 1 & \quad 0 \leq \omega \leq 0.2\pi \\ |H(e^{j\omega})| \leq 0.1, & \quad 0.5\pi \leq \omega \leq \pi \end{aligned}$$

Using bilinear transformation with $T=1s$