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DU MA MSc Mathematics

Topic:- DU\_J18\_MA\_MATHS\_Topic01

The complete integral of the partial differential equation  $xpq + yq^2 - 1 = 0$  where  $p = \frac{\partial z}{\partial x}$  and

$$q = \frac{\partial z}{\partial y}$$
 is

[Question ID = 2159]

$$(z+b)^2 = 4(ax+y).$$
 [Option ID = 8635]

$$z + b = 2(ax + y)$$
. [Option ID = 8633]

$$z + b = 4(ax + y)^2$$
. [Option ID = 8636]

$$z + b = 2(ax + y)^2$$
. [Option ID = 8634]

$$(z+b)^2 = 4(ax+y)$$
. [Option ID = 8635

Let P be the set of all the polynomials with rational coefficients and S be the set of all sequences of natural numbers. Then which one of the following statements is true?

[Question ID = 2139]

S is countable but P is not. O(D) = S(S(S))

Both the sets P and S are uncountable.

Both the sets P and S are countable.

[Option ID = 8553]

P is countable but S is not. [Option ID = 8554]

P is countable but S is not.  $_{\text{[Ootion ID} = 8554]}$ 

For the differential equation

$$x\frac{dy}{dx} + 6y = 3xy^{4/3}$$

consider the following statements:

- (i) The given differential equation is a linear equation.
- (ii) The differential equation can be reduced to linear equation by the transformation  $V = y^{-1/3}$ .
- (iii) The differential equation can be reduced to linear equation by the transformation  $V = x^{-1/3}$ .

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are [Question ID = 2156]

1. Only (i). [Option ID = 8622]
2. Only (ii). [Option ID = 8624]
3. Only (ii). [Option ID = 8623]
4. Both (i) and (ii). [Option ID = 8621]

Correct Answer:

Only (ii). [Option ID = 8623]

Which one of the following statements is not true for Simpson's 1/3 rule to find approximate value of the definite integral  $I = \int_0^1 f(x) dx$ ?

[Question ID = 2151]

If 
$$y_0 = f(0)$$
,  $y_1 = f(0.5)$ ,  $y_2 = f(1)$ , the approximate value of  $I$  is  $\frac{1}{6}[y_0 + 3y_1 + y_2]$ .

The approximating function has odd number of points common with the function f(x).

[Option ID =

Simpson's 1/3 rule improves trapezoidal rule.

The function f(x) is approximated by a parabola.

Correct Answer :-

If 
$$y_0 = f(0)$$
,  $y_1 = f(0.5)$ ,  $y_2 = f(1)$ , the approximate value of  $I$  is  $\frac{1}{6}[y_0 + 3y_1 + y_2]$ .

[Option ID]

The equation of the tangent plane to the surface  $z = 2x^2 - y^2$  at the point (1, 1, 1) is

[Question ID = 2133]

$$x - y - 2z = 2.$$
[Option ID = 8531]
 $4x - y - 3z = 1.$ 
[Option ID = 8532]

$$2x - y - 2z = 1$$
. [Option ID = 8529]

$$4x - 2y - z = 1.$$
 [Option ID = 8530]

Correct Answer :-

$$4x - 2y - z = 1$$
. [Option ID = 8530]

If  $\{x, y\}$  is an orthonormal set in an inner product space then the value of ||x - y|| + ||x + y|| is

[Question ID = 2128]

1. 
$$2\sqrt{2}$$
. [Option ID = 8510]

$$2 + \sqrt{2}$$
. [Option ID = 8512]

√2.



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 Coption 1D = 85091  $2\sqrt{2}$ . Fortion ID = 85101 Which one of the following spaces, with the usual metric, is not separable? [Question ID = 2147] The space C[a, b] of the set of all real valued continuous functions defined on [a, b]. The space  $l^{\infty}$  of all bounded real sequences with supremum metric. The Euclidean space  $\mathbb{R}^n$ . [Option ID = 8585] The space  $l^1$  of all absolutely convergent real sequences. The space  $l^{\infty}$  of all bounded real sequences with supremum metric. [Cotion ID = 8588] 8) Let G be an abelian group of order 2018 and f: G → G be defined as f(x) = x<sup>5</sup>. Then [Question ID = 2118] f is not injective. [Option ID = 8470] f is not surjective. [Option ID = 8471] there exists  $e \neq x \in G$  such that  $f(x) = x^{-1}$ f is an automorphism of G. f is an automorphism of G.  $_{1000000 \text{ ID}} = 84691$ 9) If f: R→R is a continuous function such that f(x + y) = f(x) + f(y), for all  $x, y \in \mathbb{R}$ , then [Question ID = 2138] f is increasing if  $f(1) \ge 0$  and decreasing if  $f(1) \le 0$ . f is increasing if  $f(1) \le 0$  and decreasing if  $f(1) \ge 0$ . f is a not an increasing function. f is neither an increasing nor a decreasing function. [Option ID = 8550] f is increasing if  $f(1) \ge 0$  and decreasing if  $f(1) \le 0$ .

The central difference operator  $\delta$  and backward difference operator V are related as

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[Question ID = 2154]

$$\delta = \nabla (1 - \nabla)^{\frac{1}{2}},$$
[Option ID = 8615]
$$\delta = \nabla (1 + \nabla)^{-\frac{1}{2}}.$$
[Option ID = 8614]

$$\delta = \nabla(1 + \nabla)^{-\frac{1}{2}}.$$

$$\delta = \nabla (1 - \nabla)^{-\frac{1}{2}}.$$
[Option ID = 8616

$$\delta = \nabla (1 + \nabla)^{\frac{1}{2}}.$$
[Option ID = 8613]

Correct Answer :-

$$\delta = \nabla (1 - \nabla)^{-\frac{1}{2}}.$$
[Option ID = 8616]

How many continuous real functions f can be defined on  $\mathbb{R}$  such that  $(f(x))^2 = x^2$  for every  $x \in \mathbb{R}$ ?

[Question ID = 2144]

- Infinitely many. [Option ID = 8576]
- None. [Option ID = 8575]
- 4. [Option ID = 8574]
- 4. 2. [Option ID = 8573]

Correct Answer :-

- . 4. [Option ID = 8574]
- 12) The greatest common divisor of 11 + 7i and 18 i in the ring of Gaussian integers Z[i] is

[Question ID = 2122]

- 31. [Option ID = 8485]
- 2. [Option ID = 8488]
- 3. 1 + i. [Option ID = 8487]
- 2 + i. [Option ID = 8486]

Correct Answer :-

- . 1. [Option ID = 8488]
- 13) The complete integral of the partial differential equation

$$\frac{\partial^2 z}{\partial x^2} - 2 \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial^2 z}{\partial y^2} = e^{x+2y}$$

is

[Question ID = 2161]

$$\phi_1(y-x) + x\phi_2(y+x) + e^{x+2y}$$
.

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\phi_{1}(y+x) + x\phi_{2}(y+x) + xe^{x+2y}.
[Option ID = 8644]
\phi_{1}(y-x) + \phi_{2}(y+x) + e^{x+2y}.
\phi_{1}(y+x) + x\phi_{2}(y+x) + e^{x+2y}.
[Option ID = 8641]
\phi_{1}(y+x) + x\phi_{2}(y+x) + e^{x+2y}.
[Option ID = 8642]
\phi_1(y+x) + x\phi_2(y+x) + e^{x+2y}. [Option ID = 8642]
14) If S = \{(1, 0, i), (1, 2, 1)\} \subset \mathbb{C}^3 then S^{\perp} is
[Question ID = 2127]
  span \{(i, -\frac{1}{2}(i+1), -1)\}.
   span \{(-i, \frac{1}{2}(i+1), 1)\}.
   span \{(i, -\frac{1}{2}(i+1), 1)\}.
   span \{(i, \frac{1}{2}(i+1), -1)\}.
   span \{(i, -\frac{1}{2}(i+1), 1)\}.
    The improper integral \int_{-\infty}^{0} 2^{x} dx is
[Question ID = 2135]
convergent and converges to 2. [Option ID = 8540]
  divergent. [Option ID = 8539]
   convergent and converges to \frac{1}{\ln 2}.
  convergent and converges to -ln2. [Option ID = 8537]
Correct Answer :-
   convergent and converges to \frac{1}{\ln 2}.
Let f: \mathbb{R} \to \mathbb{R} be a continuous function which takes irrational values at rational points and rational
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[Question ID = 2145]

f is uniformly continuous on  $\mathbb{Q}$ .

f is uniformly continuous on R.

values at irrational points. Then which one of the following statements is true?

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f is uniformly continuous on  $\mathbb{Q}^{c}$ .

[Option ID = 8579]

No such function exists. [Option ID = 8580]

No such function exists. [Option ID = 8580]

17) If f: [0, 10] → ℝ is defined as

$$f(x) = \begin{cases} 0, & 0 \le x < 2, \\ 1, & 2 \le x \le 5, \\ 0, & 5 < x \le 10, \end{cases}$$

and 
$$F(x) = \int_0^x f(t)dt$$
 then

[Question ID = 2134]

$$F(x) = 3 \text{ for } x \le 5.$$
 [Option 1D = 8536]

$$F'(x) = f(x)$$
 for every  $x$ .

[Option ID = 8534]

F is not differentiable at x = 2 and x = 5. [Option 10 = 8535]

F is differentiable everywhere on [0, 10].

F is not differentiable at x = 2 and x = 5. [Option ID = 8535]

The Maclaurin series expansion

$$ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \cdots$$

is valid

[Question ID = 2136]

only if 
$$x \in [-1,1]$$
.

[Option ID = 8543]

$$_{2.}$$
 if  $x > -1$ . [Option ID = 8541]

only if 
$$x \in (-1,1]$$
. [Option ID = 8542]

for every  $x \in \mathbb{R}$ . [Option ID = 8544]

only if  $x \in (-1,1]$ . [Cotion ID = 8542]

19) If  $4x \equiv 2 \pmod{6}$  and  $3x \equiv 5 \pmod{8}$  then one of the value of x is

[Question ID = 2115]

1. 32 [Option ID = 8460]

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4. 23 [Option ID = 8458]

Correct Answer :-

23 [Option ID = 8458]

20)

If  $f(x) = \lim_{n\to\infty} S_n(x)$ , where

$$S_n(x) = \frac{x}{(x+1)(2x+1)} + \frac{x}{(2x+1)(3x+1)} + \dots + \frac{x}{(nx+1)((n+1)x+1)}$$

# then the function f is

[Question ID = 2131]

- 1. continuous nowhere. [Option ID = 8524]
- 2. continuous everywhere. [Option ID = 8521]
- 3. continuous everywhere except at countably many points. [Option ID = 8522]
- continuous everywhere except at one point. [Option ID = 8523]

Correct Answer :-

continuous everywhere except at one point. [Option ID = 8523]

21)

The rate of change of  $f(x, y) = 4y - x^2$  at the point (1, 5) in the direction from (1, 5) to the point (4, 3) is

[Question ID = 2130]

$$\frac{-19}{\sqrt{13}}$$

Correct Answer :-

$$\frac{-14}{\sqrt{13}}$$
. [Option ID = 8518]

Let 
$$G = \{a_1, a_2, \dots, a_{25}\}$$
 be a group of order 25. For  $b, c \in G$  let

$$bG = \{ba_1, ba_2, \dots, ba_{25}\}, Gc = \{a_1c, a_2c, \dots, a_{25}c\}.$$

Then

[Question ID = 2119]

$$bG = Gc$$
 only if  $b = c$ . [Option ID = 8475]

$$bG = Gc \ \forall b, c \in G.$$
 [Option ID = 8473]

$$bG = Gc$$
 only if  $b^{-1} = c$ . [Option ID = 8476]

$$bG \neq Gc$$
, if  $b \neq c$ . [Option ID = 8474]

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 $bG = Gc \ \forall b, c \in G.$  [Option ID = 8473]

If  $(x_n)$  is a sequence such that  $x_n \ge 0$ , for every  $n \in \mathbb{N}$  and if  $\lim_{n \to \infty} ((-1)^n x_n)$  exists then which one of the following statements is true?

[Question ID = 2141]

- The sequence  $\langle x_n \rangle$  is a Cauchy sequence. [Option ID = 8562]
- The sequence  $\langle x_n \rangle$  is not a Cauchy sequence. [Option 1D = 8564]
- The sequence  $\langle x_n \rangle$  is unbounded. [Option ID = 8563]
- The sequence  $\langle x_n \rangle$  is divergent. [Option ID = 8561]

The sequence  $\langle x_n \rangle$  is a Cauchy sequence.

If n > 2, then  $n^5 - 5n^3 + 4n$  is divisible by

[Question ID = 2113]

- 1.80 [Option ID = 8449]
- 2. 120 [Option ID = 8451]
- 100 [Option ID = 8450]
- 4. 125 [Option ID = 8452]

Correct Answer :-

- 120 [Option ID = 8451]
- 25) Let

$$S = \bigcap_{n=1}^{\infty} \left[ 2 - \frac{1}{n}, 3 + \frac{1}{n} \right].$$

Then S equals

[Question ID = 2140]

- (2, 3]. [Option ID = 8558]
- 2. [2, 3]. [Option ID = 8560]
- [2, 3). [Option ID = 8557]
- 4. (2, 3). [Option ID = 8559]

Correct Answer :-

- [2, 3]. [Option ID = 8560]
- If  $a_n = n^{\sin(\frac{n\pi}{2})}$  then

[Question ID = 2137]

 $\lim \sup a_n = +\infty$ ,  $\lim \inf a_n$ 

 $\limsup a_n = +\infty, \liminf a_n = 0.$  [Option ID = 8548]

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\limsup a_n = +\infty, \liminf a_n = -\infty. [Option ID = 8546]
  \limsup a_n = 1 , \liminf a_n = -1 . [Option ID = 8545]
  \limsup a_n = +\infty, \liminf a_n = 0. [Option ID = 8548]
Let f: \mathbb{R}^2 \to \mathbb{R} be defined as f(x,y) = |x| + |y|. Then which one of the following statements is
[Question ID = 2129]
f is continuous at (0, 0) and f_x(0,0) \neq f_y(0,0).
  f is continuous at (0, 0) and f_x(0,0) = f_y(0,0).
  f is discontinuous at (0, 0) and f_x(0,0) = f_y(0,0).
  f is continuous at (0,0) but f_x and f_y does not exist at (0,0).
  f is continuous at (0, 0) but f_x and f_y does not exist at (0, 0).
28)
Let A and B be two subsets of a metric space X. If intA denotes the interior A of then which one of
the following statements is not true?
[Question ID = 2146]
A \subseteq B \Rightarrow \text{int} A \subseteq \text{int} B. [Option ID = 8584]
 int(A \cup B) = intA \cup intB._{[Option ID = 8581]}
int(A \cap B) = intA \cap intB._{[Option 1D = 8583]}
  int(A \cup B) \supseteq intA \cup intB.
[Option ID = 8582]
  int(A \cup B) = intA \cup intB. [Option ID = 8581]
Which one of the following statements is false?
[Question ID = 2123]
A subring of a field is a subfield. [Coston ID = 8490]
A subring of the ring of integers Z, is an ideal of Z. [Option ID = 8489]
A commutative ring with unity is a field if it has no proper ideals.
  A field has no proper ideals.
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Correct Answer :-

A subring of a field is a subfield.

Let  $\sigma = (37125)(43216) \in S_7$ , the symmetric group of degree 7. The order of  $\sigma$  is

[Question ID = 2120]

- 1. 7 [Option ID = 8480]
- 2. 4 [Option ID = 8478]
- 3. 5 [Option ID = 8479]
- 4. 2 [Option ID = 8477]

Correct Answer :-

- 4 [Option ID = 8478]
- 31) Let

$$S = \bigcap_{n=1}^{\infty} \left[ 0, \, \frac{1}{n} \right].$$

Then which one of the following statements is true?

[Question ID = 2143]

- inf S > 0. [Option ID = 8571]
- sup S = 1 and inf S = 0. [Option ID = 8572]
- $\sup S > 0$ . [Option ID = 8569]
- $\sup S = \inf S = 0.$

$$\sup S = \inf S = 0.$$
 [Option ID = 85.70]

32) The characteristics of the partial differential equation

$$36\frac{\partial^2 z}{\partial x^2} - y^{14}\frac{\partial^2 z}{\partial y^2} - 8x^{12}\frac{\partial z}{\partial x} = 0$$

when it is of hyperbolic type are given by

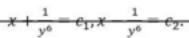
[Question ID = 2160]

$$x + \frac{36}{y^6} = c_1, x - \frac{36}{y^6} = c_2.$$
 [Option ID = 8638]

$$x + \frac{1}{y^6} = c_1$$
,  $x - \frac{1}{y^6} = c_2$ . [Option ID = 8637]

$$x + \frac{1}{y^7} = c_1, x - \frac{1}{y^7} = c_2.$$
 [Option ID = 8637]

$$x + \frac{36}{y^7} = c_1, x - \frac{36}{y^7} = c_2.$$
[Option ID = 8640]





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A bound for the error for the trapezoidal rule for the definite integral \int_0^1 \frac{1}{1+x} dx is
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[Question ID = 2150]

- 1. 6 [Option ID = 8600]
- 2. 25 [Option ID = 8597]
- 3. 15 (Option ID = 8598
- 4. 20' [Option 1D = 8599]

Correct Answer :-

6 [Option ID = 8600]

Exact value of the definite integral  $\int_a^b f(x)dx$  using Simpson's rule

[Question ID = 2152]

- cannot be given for any polynomial. [Option 10 = 8608
- is given when f(x) is a polynomial of degree 4. [Option ID = 8605]
  - is given when f(x) is a polynomial of degree 5.
- is given when f(x) is a polynomial of degree 3.

[Option ID = 8606]

Correct Answer :-

is given when f(x) is a polynomial of degree 3.

Let p be a prime and let G be a non-abelian p-group. The least value of m such that  $p^m \setminus o\left(\frac{G}{Z(G)}\right)$  is

[Question ID = 2121]

- 1. 0 (Option ID = 8481)
- 2. 1 [Option ID = 8482]
- 3. 3 [Option ID = 8484]
- 4. 2 [Option ID = 8483]

Correct Answer :-

- . 0 [Option ID = 8481]
- If  $\varphi$  is Euler's Phi function then the value of  $\varphi(720)$  is

[Question ID = 2114]

- 1. 248 [Option ID = 8456]
- 2. 144 [Option ID = 8453]
- 3. 192 [Option ID = 8454]
- 4. 72 [Option ID = 8455]

Correct Answer :-

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192 [Option ID = 8454]

37

The total number of arithmetic operations required to find the solution of a system of n linear equations in n unknowns by Gauss elimination method is

[Question ID = 2153]

$$\frac{2}{3}n^3 + \frac{1}{2}n^2 - \frac{5}{6}n.$$
 [Option ID = 8609]

$$n^3 - \frac{1}{6}n$$
.

η - - - η. [Option ID = 8610]

$$\frac{2}{3}n^3 + \frac{3}{2}n^2 - \frac{7}{6}n$$
.

[Option ID = 8611]

$$\frac{1}{3}n^3 + \frac{1}{2}n^2 - \frac{5}{6}n$$

[Option ID = 8612]

Correct Answer :-

$$\frac{2}{3}n^3 + \frac{3}{2}n^2 - \frac{7}{6}n$$
. [Option ID = 8611

If  $(x_n)$  is a sequence defined as

$$x_n = \left\lceil \frac{5+n}{2n} \right\rceil$$
, for every  $n \in \mathbb{N}$ 

where [.] denotes the greatest integer function then  $\lim_{n \to \infty} x_n$ 

[Question ID = 2142]

- 1. 1. [Option ID = 8568]
- $\frac{1}{2}$ .
- 2. 2 [Option ID = 8566]

does not exist. [Option ID = 8565]

4. 0. [Option ID = 8567]

Correct Answer :-

. O. [Option ID = 8567]

39)

Let R be a ring with characteristic n where  $n \ge 2$ . If M is the ring of  $2 \times 2$  matrices over R then the characteristic of M is

[Question ID = 2125]

- 1. 1. [Option ID = 8500]
- 2. O. [Option ID = 8498]
- 3. n 1. [Option ID = 8499]
- n. [Option ID = 8497]

Correct Answer :-

n. TORROR ID = 8497



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If A = \begin{bmatrix} a & 2 \\ 1 & b \end{bmatrix} is a matrix with eigen values \sqrt{6} and -\sqrt{6}, then the values of a and b are
    respectively,
[Question ID = 2116]
1. 2 and -1. [Option ID = 8463]
2. 2 and -2. [Option ID = 8464]
3. 2 and 1. [Option ID = 8461]
4. -2 and 1. [Option ID = 8462]
Correct Answer :-

    2 and -2. [Option ID = 8464]

    The dimension of the vector space of all 6 × 6 real skew-symmetric matrices is
[Question ID = 2126]
1. 36 [Option ID = 8504]
2. 21 [Option ID = 8502]

 15 [Option ID = 8501]

Correct Answer :-

    15 [Option ID = 8501]

Let (x_0, f(x_0)) = (0, -1), (x_1, f(x_1)) = (1, a) and (x_2, f(x_2)) = (2, b). If the first order divided
differences f[x_0, x_1] = 5 and f[x_1, x_2] = c and the second order divided difference f[x_0, x_1, x_2] = c
-\frac{3}{2}, then the values of a, b and c are
[Question ID = 2148]
4, 2, 4. [Option ID = 8592]
2, 4, 6. [Option ID = 8590]
3. 4, 6, 2. [Option ID = 8589]
6, 2, 4. [Option ID = 8591]
Correct Answer :-
4, 6, 2. [Option ID = 8589]
43)
Let the polynomial f(x) = 3x^5 + 15x^4 - 20x^3 + 10x + 20 \in \mathbb{Z}[x], and f_0(x) be the
polynomial in \mathbb{Z}_3[x] obtained by reducing the coefficients of f(x) modulo 3. Which one of the
following statements is true?
[Question ID = 2124]
f(x) is reducible over \mathbb{Q}, f_0(x) is reducible over \mathbb{Z}_3.
f(x) is irreducible over \mathbb{Q}, f_0(x) is reducible over \mathbb{Z}_3.
 f(x) is reducible over \mathbb{Q}, f_0(x) is irreducible over \mathbb{Z}_3.
  f(x) is irreducible over \mathbb{Q}, f_0(x) is irreducible over \mathbb{Z}_3.
```

Correct Answer :-

f(x) is irreducible over  $\mathbb{Q}$ ,  $f_0(x)$  is reducible over  $\mathbb{Z}_3$ .

44) The general solution of the system of the differential equations

$$x_1' = 3x_1 - 2x_2$$
  
$$x_2' = 2x_1 - 2x_2$$

is given by

[Question ID = 2158]

$$\begin{pmatrix} c_1e^{-t} + 2c_2e^{2t} \\ 2c_1e^{-t} + c_2e^{2t} \end{pmatrix}.$$
[Option ID = 8632]
$$\begin{pmatrix} c_1e^t + 2c_2e^{-2t} \\ 2c_1e^t + 2c_2e^{-2t} \end{pmatrix}.$$
[Option ID = 8631]
$$\begin{pmatrix} c_1e^t + 2c_2e^{-2t} \\ c_1e^t + c_2e^{-2t} \end{pmatrix}.$$
3.
$$\begin{pmatrix} c_1e^{-t} + c_2e^{2t} \\ c_1e^{-t} - c_2e^{2t} \end{pmatrix}.$$
[Option ID = 8630]

Correct Answer :-

$$\binom{c_1e^{-t} + 2c_2e^{2t}}{2c_1e^{-t} + c_2e^{2t}}$$
.

45) The eigenvalues for the Sturm-Liouville problem

$$y'' + \lambda y = 0, 0 \le x \le \pi,$$
  
 $y(0) = 0, y'(\pi) = 0$ 

are [Question ID = 2155]

$$\lambda_n = n^2 \pi^2$$
,  $n = 1, 2, \dots$  [Option ID = 8619]  
 $\lambda_n = n^2$ ,  $n = 1, 2, \dots$  [Option ID = 8618]  
 $\lambda_n = n\pi$ ,  $n = 1, 2, \dots$  [Option ID = 8617]

$$\lambda_n = \frac{(2n-1)^2}{4}$$
 ,  $n=1,2,...$  [Option ID = 8617]

Correct Assesses

$$\lambda_n = rac{(2n-1)^2}{4}$$
 ,  $n=1,2,...$  [Option ID = 8620]

46)



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The initial value problem

$$x\frac{dy}{dx} - 2y = 0,$$
  
$$x > 0, y(0) = 0$$

has

[Question ID = 2157]

- 1. exactly two solutions [Option ID = 8626]
- 2. a unique solution. [Option ID = 8627]
- 3. no solution. [Option ID = 8628]
- 4. infinitely many solutions. [Option ID = 8625]

Correct Answer :-

- infinitely many solutions. [Option ID = 8625]
- 47) The partial differential equation

$$(x^2 - 1)\frac{\partial^2 z}{\partial x^2} + 2y\frac{\partial^2 z}{\partial x \partial y} - \frac{\partial^2 z}{\partial y^2} = 0$$

is

[Question ID = 2162]

- hyperbolic for  $\{(x,y) \in \mathbb{R}^2 : x^2 + y^2 < 1\}$ .
- parabolic for  $\{(x,y) \in \mathbb{R}^2 : x^2 + y^2 < 1\}$ .
- hyperbolic for  $\{(x,y) \in \mathbb{R}^2 : x^2 + y^2 > 1\}$ .
- elliptic for  $\{(x, y) \in \mathbb{R}^2 : x^2 + y^2 > 1\}$ . [Option ID = 8647]

Correct Answer :-

hyperbolic for  $\{(x, y) \in \mathbb{R}^2 : x^2 + y^2 > 1\}$ . [Option ID = 8648]

48)

Let f be a convex function with f(0) = 0. Then the function g defined on  $(0, +\infty)$  as  $g(x) = \frac{f(x)}{x}$ 

[Question ID = 2132]

- 1. is an increasing function. [Option ID = 8525]
- 2. is such that its monotonicity cannot be determined. [Option ID = 8528]
- 3. is neither increasing nor decreasing function. [Option ID = 8527]
- 4. is a decreasing function. [Option ID = 8526]

Correct Answer :-

- is an increasing function. [Option ID = 8525]
- 49) Which one of the statements is false? [Question ID = 2117]
- Every quotient group of a cyclic group is cyclic.

  [Option ID = 8465]

If G and H are groups and  $f: G \rightarrow H$  is a homomorphism then f induces an isomorphism of

 $\frac{g}{\operatorname{Ker}(f)}$  with H.

[Option ID = 8467]

Every quotient group of an abelian group is abelian.

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If G is a group and Z(G) is its centre such that the quotient group of G by Z(G) is cyclic, then G is abelian.

[Option ID = 8466]

Correct Answer :-

If G and H are groups and  $f: G \to H$  is a homomorphism then f induces an isomorphism of  $\frac{G}{\text{Ker}(f)}$  with H.

[Option ID = 8467]

- 50) For cubic spline interpolation which one of the following statements is true? [Question ID = 2149]
- 1. The second derivatives of the splines are continuous at the interior data points but not the first derivatives. [Option ID = 8594]
- 2. The third derivatives of the splines are continuous at the interior data points. [Option ID = 8596]
- 3. The first derivatives of the splines are continuous at the interior data points but not the second derivatives. [Option 1D = 8593]

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4. The first and the second derivatives of the splines are continuous at the interior data points. [Option ID = 8595]

#### Correct Answer :-

The first and the second derivatives of the splines are continuous at the interior data points. [Option ID = 8595]

