



M.Tech I Semester Supplementary Examinations August/September 2018

ADVANCED OPTIMIZATION TECHNIQUES

(Common to PE & PEED)

(For students admitted in 2013, 2014, 2015 & 2016 only)

Time: 3 hours

Max. Marks: 60

Answer any FIVE questions
All questions carry equal marks

- 1 (a) Write the procedure involved in converting inequality constraints (both \leq and \geq) into equality constraints in linear programming problems.
(b) Write the dual of the problem:

$$\text{Maximize } Z = 5a - 2b$$

$$\text{Subject to: } 2a + b \leq 9$$

$$a - 2b \leq 2$$

$$-3a + 2b \leq 3$$
Where $a, b, \geq 0$

- 2 A salesman wants to visit A, B, C, D and E. He does not want to visit any city twice before completing his work. Find the least cost route.

	A	B	C	D	E
A	-	2	5	7	1
B	6	-	3	8	2
C	8	7	-	4	7
D	12	4	6	-	5
E	1	3	2	8	-

- 3 Using the method of Lagrange multipliers:

$$\text{Minimize } f(x) = \frac{1}{2}(x_1^2 + x_2^2 + x_3^2)$$

$$\text{Subject to: } g_1(x) = x_1 - x_2$$

$$g_2(x) = x_1 + x_2 + x_3 - 1$$
- 4 Calculate the gradient of the following function at the given point by the central difference approach with a 1 percent change in the point and compare them with the exact gradient:

$$f(x) = 12.096x_1^2 + 21.504x_2^2 - 1.732x_1 - x_2 \text{ at } (5,6)$$
- 5 (a) Write the steps involved in writing a sample genetic algorithm.
(b) Explain the Roulette wheel analogy for the reproduction procedure in genetic algorithms.
- 6 Explain the concept of genetic programming (GP) and write the procedure for solving differential equations using GP.
- 7 (a) Explain the terms population, generation and niche used in genetic algorithms.
(b) Explain the applications of multi objective GA problems.

- 8 A beam of rectangular cross section is subjected to a maximum bending moment of M and a maximum shear of V . The allowable bending and shearing stresses are σ and τ , respectively. The bending stress in the beam is calculated as:

$$\sigma = \frac{6M}{bd^2}$$

And average shear stress in the beam is calculated as:

$$\tau = \frac{3V}{2bd}$$

Where d is the depth and b is the width of the beam. It is also desired that the depth of the beam shall not exceed twice its width. Formulate the design problem for minimum cross-sectional area using the following data:

$$M = 140 \text{ kN m}, V = 24 \text{ kN}, \sigma = 165 \text{ MPa}, \tau = 50 \text{ MPa}.$$

