

Total No. of Pages: **3****5386**

Register Number:

Name of the Candidate:

**B.Sc. DEGREE EXAMINATION, May 2015****(COMPUTER SCIENCE)****(FIRST YEAR)****(PART-III)****130/140: SCIENTIFIC COMPUTING**

(Common with B.Sc I.T and B.C.A)

Time: Three hours

Maximum: 100 marks

**Answer any FIVE questions****(5×20=100)**

1. a) Solve for a positive root of  $x - \cos x = 0$  by regular falsi method. (10)
- b) Using Gauss-Seidal method, solve the following system. Start with  $x=1, y=2, z=3$  (10)

$$x + 3y + 52z = 173.61$$

$$x - 27y + 2z = 71.31$$

$$41x - 2y + 3z = 65.46$$

2. a) Apply Gauss-Jordan method, to solve the system. (10)

$$8x - 3y + 2z = 20$$

$$4x + 11y - z = 33$$

$$6x + 3y + 12z = 35$$

- b) Find the least positive root of the equation  $\tan x = x$  to an accuracy of 0.0001 by Newton-Raphson method. (10)
3. a) Compute  $f'(0)$  and  $f''(4)$  from the data. (10)

x	0	1	2	3	4
y	1	2.718	7.381	20.086	54.598

- b) Find the value of y at  $x=21$  from the following data. (10)

x	20	23	26	29
y	0.3420	0.3907	0.4384	0.4848

**5386**

2

4. a) Find the First, Second and Third derivatives of  $f(x)$  at  $x=1.5$  if, (10)

x	1.5	2.0	2.5	3.0	3.5	4.0
F(x)	3.375	7.000	13.625	24.000	38.875	59.000

- b) Evaluate (10)

$$\int_0^5 \frac{dx}{4x+5}$$

by Simpson's one-third rule and hence find the value of  $\log_e 5 (n=10)$

5. a) Using Taylor's series method find  $y$  at  $x=1.1$  and  $1.2$  by solving, (10)

$$\frac{dy}{dx} = x^2 + y^2 \text{ given } y(1)=2.3$$

- b) Find an approximate solution of the initial value problem, (10)

$$y' = 1 + y^2, y(0) = 0$$

by Picard's method

6. a) Using Euler's method. (10)

$$\text{Solve } \frac{dy}{dx} = 1 + xy \text{ with } y(0) = 2$$

Find  $y(0.1)$ ,  $y(0.2)$  and  $y(0.3)$

- b) Compute  $y(0.1)$  and  $y(0.2)$  by Runge-Kutta 4<sup>th</sup> order for the (10)

$$\frac{dy}{dx} = xy + y^2, y(0) = 1$$

7. a) Classify the equations. (10)

$$\text{i) } U_{xx} + 2U_{xy} + U_{yy} = 0$$

$$\text{ii) } x^2 f_{xx} + (1 - y^2) f_{yy} = 0$$

- b) Solve, (10)

$$\frac{\partial^2 u}{\partial x^2} - 2 \frac{\partial u}{\partial t} = 0$$

Given  $u(0, t) = 0$ ,  $u(4, t) = 0$

$$U(x, 0) = x(4 - x)$$

Assume  $h=1$

Find the values of  $u$  up to  $t=5$

8. a) Solve the Laplace equation at the interior points of the square region (10)  
given below:

500	1000	1000	1000	500	
	47	48	49		
0		44	45	46	0
0		41	42	43	0
0					0
	0	0	0		

- b) Compare Trapezoidal rule and Simpson's 1/3 rule for evaluating numerical integration. (5)

\*\*\*\*\*

www.FirstRanker.com