

Time: 3 hours

Answer any FIVE Questions All Questions carry equal marks \*\*\*\*\*

- 1. (a) Explain the terms Joint probability and Conditional probability.
  - (b) Show that Conditional probability satisfies the three axioms of probability.
  - (c) Two cards are drawn from a 52-card deck (the first is not replaced):
    - i. Given the first card is a queen. What is the probability that the second is also a queen?
    - ii. Repeat part (i) for the first card a queen and second card a 7.
    - iii. What is the probability that both cards will be the queen?
- 2. (a) What is gaussian random variable? Develop an equation for gaussian distribution function.
  - (b) Verify that the following is a distribution function:

 $\begin{aligned} F(x) &= 0 & \text{for } x < -a, \\ &= 1/2(x/a+1) & \text{for } -a < = x < = a, \text{ and} \\ &= 1 & \text{for } x > a. \end{aligned}$ 

- 3. (a) A discrete random variable X have values x = -1, 0, 1 and 2 with respective probabilities 0.1, 0.3, 0.4 and 0.2. X is transformed to  $Y = 2 X^2 + X^3/3$  (Find the density function of Y.
  - (b) If X is the number scored in a throw of a fair die, show that the Chebyshev's inequality gives P[|X m| > 2.5] < 0.47 where m is the mean of X, while the actual probability is zero. [8+8]

where in is the mean of A, while the actual probability is zero.

- 4. (a) Explain the conditional distribution and density function of two random variables X and Y.
  - (b) The joint probability density function of two random variables X and Y is given by f(x, y) = a(2x + y<sup>2</sup>), 0 ≤ x ≤ 2, 2 ≤ y ≤ 4 = 0, elsewhere
    Find:

    i. value of 'a'
    ii. P(X ≤ 1, Y > 3).
- 5. (a) Write the expression for expected value of a function of random variables and prove that the mean value of a weighted sum of random variables equals the weighted sum of mean values.
  - (b) X is a random variable with mean  $\bar{X} = 3$ , variance  $\sigma_X^2 = 2$ .

i. Determine the second moment of X about origin

- ii. Determine the mean of random variable y = where y = -6X + 22. [8+8]
- 6. (a) Prove that autocorrelation function of a random process is even function of  $\tau$ .
  - (b) Prove that  $R_{XX}(\tau) = R_{XX}(0)$ .

7. The auto correlation function of a random process X(t) is  $R_{XX}(\tau) = 3 + 2 \exp(-4\tau^2)$ .

- (a) Find the power spectrum of X(t).
- (b) What is the average power in X(t)
- (c) What fractional power lies in the frequency band  $\frac{-1}{\sqrt{2}} \le \omega \le \frac{1}{\sqrt{2}}$ . [6+4+6]
- 8. (a) Explain how the available noise power in an electronic circuit can be estimated.
  - (b) What are the different noise sources that may be present in an electron devices?

[8+8]

[8+8]

**R7** 

Max Marks: 80

4 + 6 + 6]

[10+6]