# B.Tech I Year (R07) Supplementary Examinations, May 2012 <br> MATHEMATICS - I <br> (Common to all branches) 

Time: 3 hours
Answer any FIVE questions
All questions carry equal marks
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1 (a) Solve $y d x-x d y+\left(1+x^{2}\right) d x+x^{2} \sin y d y=0$.
(b) Solve $y\left(2 x y+e^{x}\right) d x=e^{x} d y$.

2 (a) Solve: $\left(D^{2}-3 D+4\right) y=0$.
(b) Solve: $\mathrm{y}^{\prime \prime}-\mathrm{y}^{\prime}-2 \mathrm{y}=3 e^{2 x}$ given that $\mathrm{y}(0)=0, \mathrm{y}^{\prime}(0)=-2$.

3 (a) Verify Rolle's theorem for $f(x)=\frac{x^{2}-x-6}{x-1}$ in the interval $(-2,3)$.
(b) Verify if $u=x+2 y+z, V=x-2 y+3 z, W=2 x y-x z+4 y z-2 z^{2}$ are functionally related and if so, find the relation between them.

4 (a) Find the radius of curvature at the point $\left(\frac{3 a}{2}, \frac{3 a}{2}\right)$ of the curve $x^{3}+y^{3}=3 a x y$.
(b) Trace the curve: $y^{2}(a+x)=x^{2}(3 a-x)$.

5 (a) Evaluate $\iint_{R} x y d x d y$ where R is the region bounded by the line $x+2 y=2$, lying in the first quadrant.
(b) By changing the order of integration evaluate $\int_{0}^{1} \int_{0}^{\sqrt{1-x^{2}}} y^{2} d y d x$.

6 (a) Test for convergence of the series:
$\sum_{n=1}^{\infty}\left[\sqrt{n^{4}+1}-\sqrt{n^{4}-1}\right]$.
(b) Test the convergence of the series:
$\sum_{n=1}^{\infty} \frac{x^{2 n}}{(n+1) \sqrt{n}}$.
7 (a) Find the constants a,b,c so that $\vec{F}=(x+2 y+a z) \vec{\imath}+(b x-3 y-z) \vec{\jmath}+(4 x+c y+2 z) \vec{k}$ is irrotational.
(b) If $\vec{F}=(2 y+3) \vec{\imath}+x z \vec{\jmath}+(y z-x) \vec{k}$ evaluate $\int_{C} \vec{F} \cdot d \vec{r}$ along the line joining the origin and the point $(2,1,1)$.

8 (a) Find the Laplace transform of the function: (i) $e^{a t} \cosh b t$. (ii) $t^{2} . e^{-2 t}$.
(b) Find the inverse transform of the following functions:
(i) $\frac{1}{s^{2}\left(s^{2}+a^{2}\right)}$.
(ii) $\frac{1}{s(s+1)(s+2)}$.

