

Code: R5 102305

R5

B.Tech I Year (R05) Supplementary Examinations, May 2012

MATHEMATICS FOR BIOTECHNOLOGISTS

(Biotechnology)

Time: 3 hours

Max Marks: 80

Answer any FIVE questions

All questions carry equal marks

- 1 (a) If $A = (1, 2, 3)$ $B = (x, y, z)$ $f(1) = x$, $f(2) = y$, $f(3) = z$ then find f is an injection, surjection or bijection.
(b) Find $\frac{d}{dx} \left(\frac{\cos 3x}{x^2} \right)$.
- 2 (a) Evaluate $\int \frac{dx}{3 \cos x + 4 \sin x + 6}$.
(b) Find the area bounded by $y = \sin x$, $y = \cos x$ between any two successive intersections.
- 3 (a) Solve the following system of equations $x+y+4z = 6$, $3x + 2y - 2z = 9$, $5x + y + 2z = 13$. Using Cramer's rule.
(b) Find the rank of the matrix by reducing it to the normal form.

$$\begin{bmatrix} 1 & 0 & 1 & 0 \\ 3 & -1 & 2 & 1 \\ 2 & 1 & 2 & 1 \\ 2 & -2 & 1 & 0 \end{bmatrix}$$
- 4 (a) Solve $(e^y + 1) \cos x dx + e^y \sin x dy = 0$.
(b) Solve $\frac{dy}{dx} - \frac{\tan y}{1+x} = (1+x)e^x \sec y$.
- 5 (a) Solve the differential equation $y'' - y' - 2y = 3e^{2x}$ $y(0) = 0$, $y'(0) = 2$
(b) Find the orthogonal trajectories of the family of circles $x^2 + y^2 = ax$.
- 6 (a) Find out the square root of 25 given $x_0 = 2.0$, $x_1 = 7$ using bisection method.
(b) Using the Newton-Raphson method find the root of equation $f(x) = e^x - 3x$ that lies between 0 and 1.
- 7 (a) Construct difference table for the following data:

X	0.1	0.3	0.5	0.7	0.9	1.1	1.3
F(x)	0.003	0.067	0.148	0.248	0.370	0.518	0.697

And find $F(0.6)$ using a cube that fits at $x = 0.3, 0.5, 0.7$ and 0.9 using Newton's forward formula.
- (b) Evaluate $\int_0^5 e^{-x^2} dx$ using trapezoidal rule. Taking $h = 1$.
- 8 (a) Find $L \{ \cos 3t \}$.
(b) Find $L^{-1} \left\{ \frac{s^2 + 2s - 4}{(s^2 + 9)(s - 5)} \right\}$.
