

Code: R7411008

R7

## IV B.Tech I Semester (R07) Supplementary Examinations, May 2012 DIGITAL CONTROL SYSTEMS (Common to EIE and EConE)

Time: 3 hours Max Marks: 80

## Answer any FIVE questions All questions carry equal marks

- 1. With neat diagrams explain various types of analog to digital converters and its operation in detail.
- 2. (a) Find z-transform of the following functions.

(i) 
$$f(s) = \frac{2(s+1)}{s9s+5}$$

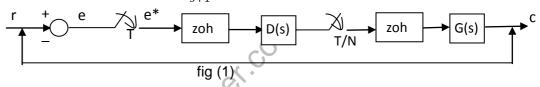
(ii) 
$$f(s) = \frac{10}{s(s^2+s+2)}$$

(b) Find inverse z-transform of the following functions

(i) 
$$f(z) = \frac{2z}{z^2 - 1.2z + 0.5}$$

(ii) 
$$f(z) = \frac{1}{z(z-0.2)}$$

- 3. (a) Obtain the pulse transfer function of the zero-orer hold circuit.
  - (b) The block diagram of a multirate discrete data control system is shown in fig(i). Find the closed loop transfer function c(z)/R(z) of the system. The sampling period is 1 sec, N is an unspecified integer  $\geq 1$ .  $D(s) = \frac{1}{s+1}$ , G(s) = K/S.



- 4. (a) Derive the relation between state equations and transfer functions.
  - (b) Obtain state transition matrix for the state equations;

$$\begin{bmatrix} \dot{x}_1(t) \\ \dot{x}_2(t) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1(t) \\ x_1(t) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t), c(t) = x_1(t)$$

- 5. (a) Explain in detail how can you find out controllability and observiability for a given system.
  - (b) Obtain the controllability of a system given by

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ -1 & -2 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u, y = \begin{bmatrix} 1 & 1 \end{bmatrix} x$$

- 6. Determine the stability of the following characteristic equations using Jury's stability test.
  - (a)  $z^3 + z^2 + 3z + 0.2 = 0$
  - (b)  $z^4 1.2 z^3 + 0.22 z^2 + 0.066 z 0.008 = 0$
  - (c)  $z^3 1.4 z^2 + 0.53 z 0.04 = 0$
- 7. Design the digital PID controller by using three rectangular integration schemes.
- 8. Consider the digital control system:

$$x[(K+1)^T] = \begin{bmatrix} 0 & 1 \\ -1 & -2 \end{bmatrix} x(KT) + \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} u(KT).$$

The pair (A, B) is controllable. Determine state feedback matrix 'G', such that u(KT) = -G.x(KT) places the closed loop eigen values at  $z_1 = 0.1$  and  $z_2 = 0.2$ .