## Code: R7 210201

B.Tech II Year I Semester (R07) Supplementary Examinations, May 2012

## MATHEMATICS - III

(Common to EEE, ECE, EIE, E.Con.E and ECC)
Time: 3 hours
Max Marks: 80
Answer any FIVE questions

## All questions carry equal marks

1 (a) Evaluate $\int_{0}^{1} x^{4}\left(\log \frac{1}{x}\right)^{3} d x$.
(b) Prove that $\int_{0}^{1} \frac{x d x}{\sqrt{1-x^{5}}}=\frac{1}{5} \beta\left(\frac{2}{5}, \frac{1}{5}\right)$.
(c) Explain $x^{3}+2 x^{2}-x-3$ in terms of leqender polynomials.

2 (a) Show that $\left(\frac{\partial^{2}}{\partial x^{2}}+\frac{\partial^{2}}{\partial y^{2}}\right) \log \left|f^{1}(z)\right|=0$ where $f(z)$ is an analytic function.
(b) Find the analytic function $\mathrm{f}(\mathrm{z})=4+\mathrm{u}$ iv if $\mathrm{u}+\mathrm{v}=\frac{\sin 2 x}{\cos h 2 y-\cos 2 x}$.

3 (a) Find all the values of $z$ which satisfy (i) $e^{z}=-2$ (ii) $e^{z}=1+\mathrm{i}$.
(b) Find the real and imaginary parts of $e^{z^{3}}$.

4 (a) Evaluate $\int_{(0,0)}^{(1,1)}\left(3 x^{2} 4 x y+i x^{2}\right) \mathrm{dz}$ along $\mathrm{X}=x^{2}$.
(b) Evaluate $\int_{c} \frac{z+4}{z^{2}+2 z+5} \mathrm{~d} z$ where C is the circle $|\mathrm{z}|=1$.

5 (a) Expand $f(z)=\frac{z^{2}-4}{z^{2}+5 z+4}$ valid for $|z|<1$.
(b) Find the current's series expression of the function $f(z)=z^{2}-6 z-1 /(z-1)(z-3)(z+2)$ in the region $3<|z+2|<5$.

6 (a) Find the poles and the corresponding residue of
(i) $\frac{z+1}{z^{2}(z-2)}$ (ii) $\frac{1-e^{2 z}}{z^{4}}$
(b) Evaluate $\int_{c}^{2 \Pi} \frac{d \theta}{2+\cos \theta}$

7 Show that the equation $z^{4}+4(1+i) z+1=0$ has one root in each quadrant.
8 (a) Find the image of the infinite strip $0<y<\frac{1}{2}$ under the transformation $\omega=1 / z$.
(b) Show that the transformation $\omega=\frac{2 z+3}{z-4}$ changes the circle $x^{2}+y^{2}-4 \mathrm{x}=0$.

